

Távolabbi csillagok: túl  
a parallaxison

# Túl a parallaxison

- szekuláris parallaxis
  - statisztikus parallaxis
- asztrometria  
+ spektroszkópia
- mozgási halmaz módszer
  - fősorozat-illesztés (izokrón-illesztés)
  - spektroszkópiai parallaxis
- HRD

# Radiális sebesség, térbeli sebesség

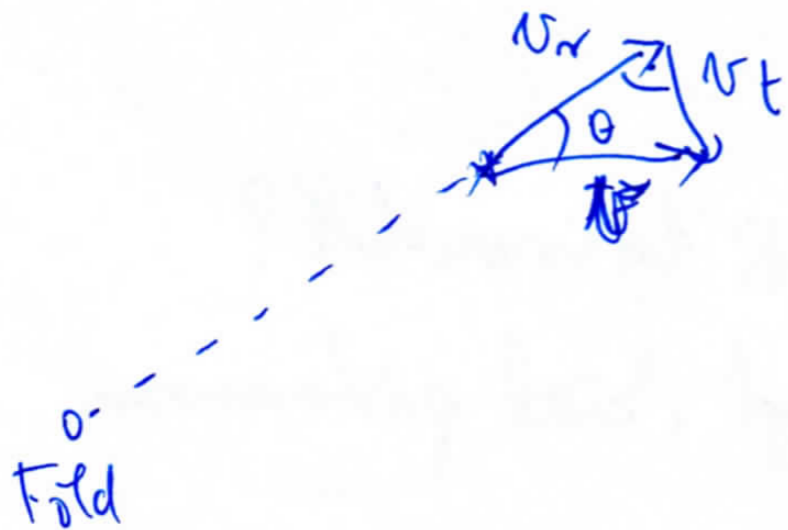
Csillag radiális sebessége:

$$z = \frac{\Delta \lambda}{\lambda} = \frac{v}{c} \text{ nem-relativisztikus közelítésben}$$

(csillag abszolút sebessége:  $\sim \text{km/s}$   
radális sebessége:  $\sim \text{m/s}$ )

A térbeli sebesség két komponensből áll:

- radiális sebesség
- transverzális sebesség



$\theta$ : látóiránygal bezárt szög

$$v_r = v \cos \theta$$

$$v_t = v \sin \theta$$

# Radiális sebesség, térbeli sebesség

Ha ismerjük a parallaxistól a távolságot, illetve ismerjük a sajátmozgását,  $v_f$  számukhoz

$$v_t (\text{km/s}) = d (\text{km}) \times \mu (\text{rad/s})$$

Mo'ndajozás átváltás után:  $[\mu] = ''/\text{év}$  (szokás a Barnard-egység;  $10''3/\text{év}$ )

$$1 \text{ rad} = 206265'' \quad 1 \text{ év} = 31 \cdot 10^6 \text{ s} \quad 1 \text{ pc} = 3.086 \cdot 10^{13} \text{ km}$$

Beírva, végigvonva  $v_t (\text{km/s}) = 4.74 \mu \cdot d$

$$[\mu] = ''/\text{év}; [d] = \text{pc}$$

Doppler-eltolódást  $v_r$

$$\pi, \mu \rightarrow v_t$$

$$v^2 = v_r^2 + v_t^2$$

Astrometric observations show that Barnard's star has a proper motion of  $10.3''$  per year and a parallax of  $0.55''$ . Spectroscopic studies show that the lines in its spectrum are shifted to the red by  $0.036\%$ . Calculate the space velocity of Barnard's star. When will the star make its closest approach to Earth? How far will it be from Earth at that time?

*Solution.* First, calculate the transverse velocity. A parallax of  $0.55''$  tells us that  $d = 1.82$  pc. So, from (6.9), we have

$$v_t = 4.74 \times 1.82 \times 10.3 = 88.8 \text{ km s}^{-1}.$$

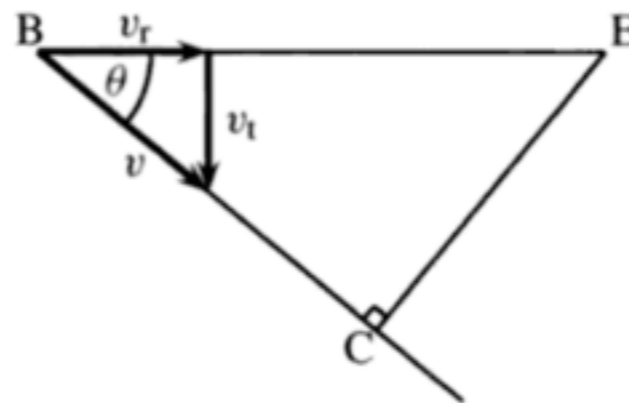
Second, calculate the radial velocity. Since the redshift is small, we can safely use the non-relativistic Doppler formula:

$$z = \frac{v_r}{c} = 3.6 \times 10^{-4} \longrightarrow v_r = 3.6 \times 10^{-4} \times 3 \times 10^5 \text{ km s}^{-1} \\ = 108 \text{ km s}^{-1}.$$

Finally, to calculate the space velocity we must combine  $v_r$  and  $v_t$  using Pythagoras:

$$v = \sqrt{v_r^2 + v_t^2} = 140 \text{ km s}^{-1}.$$

In the diagram below, E represents Earth, B represents the position of Barnard's star now, and C is Barnard's star at closest approach. We know that  $EB = 1.82$  pc. Furthermore,  $\theta = \tan^{-1}(v_t/v_r) = 39.4^\circ$ .



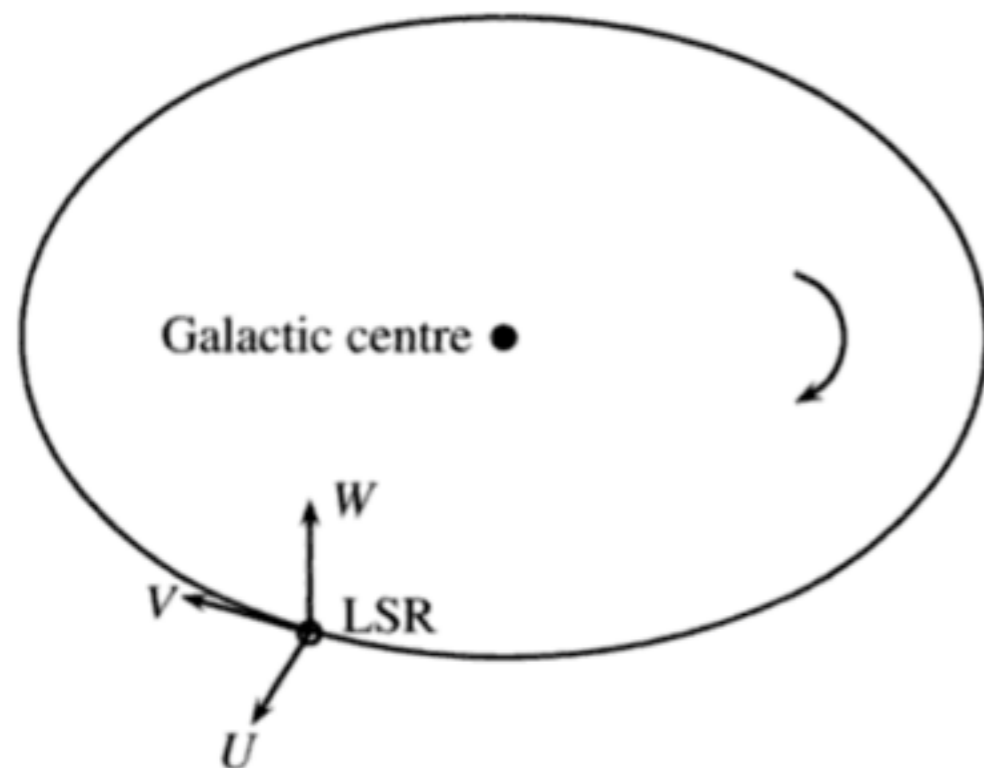
From the diagram,  $BC = EB \cos \theta = 1.4$  pc. If Barnard's star travels at  $140 \text{ km s}^{-1}$ , it will take roughly 100 centuries to cover this distance. At closest approach:

$$EC = EB \sin \theta = 1.16 \text{ pc}.$$

# LSR, apex

Hogyan növelhetjük a parallaxismérés bázisvonalát?

Local Standard of Rest (LSR):  
a közeli csillagok Naphoz  
viszonyított átlagsebessége 0.



$$U_{\odot} = -10.00 \pm 0.36 \text{ km s}^{-1}$$

$$V_{\odot} = 5.23 \pm 0.62 \text{ km s}^{-1}$$

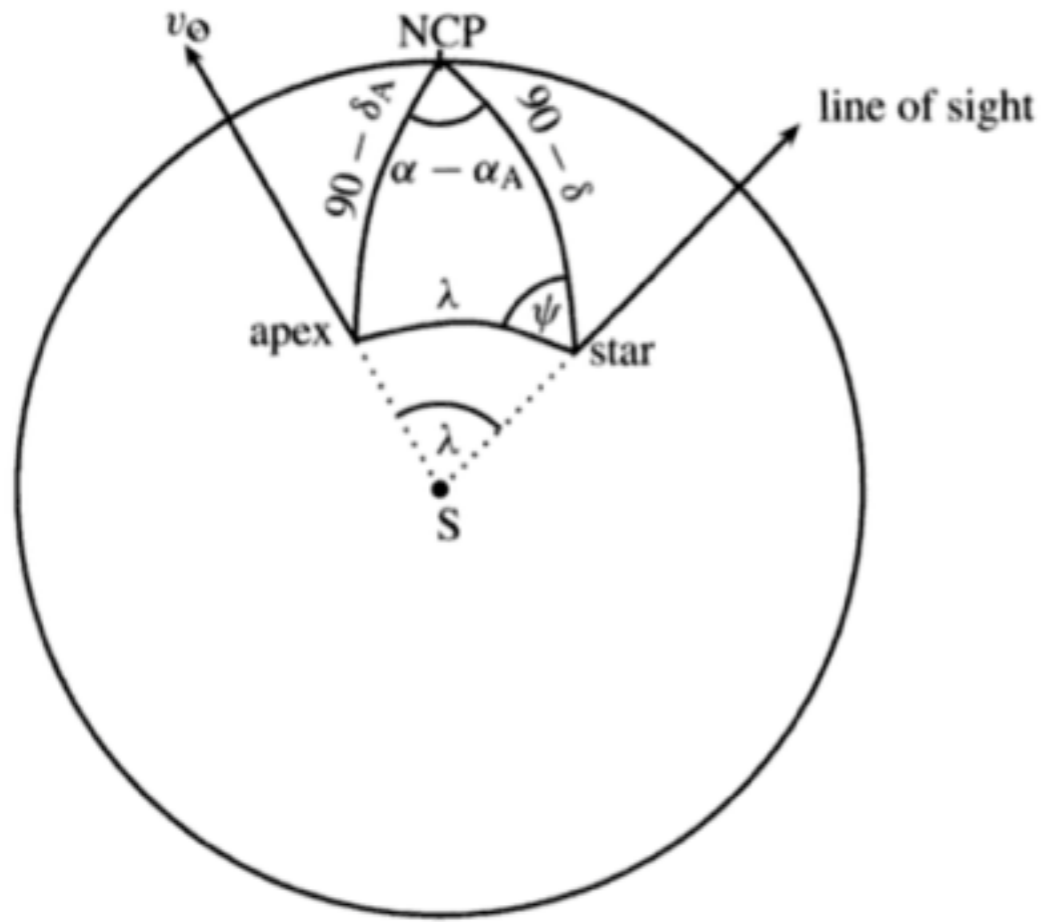
$$W_{\odot} = 7.17 \pm 0.38 \text{ km s}^{-1}.$$

Ebből a Nap LSR-hez viszonyított térbeli sebessége

$$|v_{Nap}| = 13,7 \pm 0,7 \text{ km/s} \sim 2,83 \text{ cs.e./év},$$

mozgása a Her csillagkép felé mutat (szoláris apex).

# Szekuláris parallaxis



Szférikus koszinusz-törvény alapján:

$$\cos \lambda = \sin \delta \sin \delta_A + \cos \delta \cos \delta_A \cos (\alpha - \alpha_A)$$

$$\sin \lambda \cos \psi = \cos \delta \sin \delta_A - \sin \delta \cos \delta_A \cos (\alpha - \alpha_A)$$

$\lambda, \psi$  közelednek 0-hoz mint a távolság növekszik.

# Szekuláris parallaxis

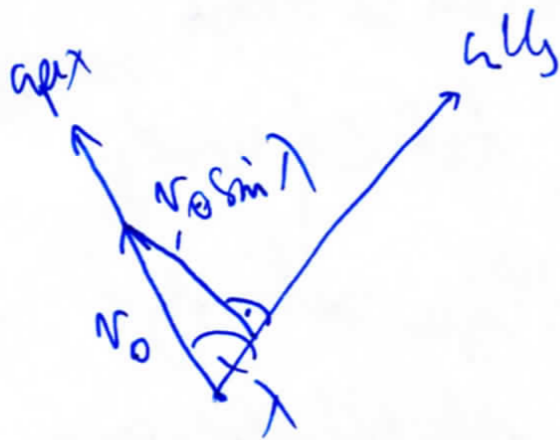
Bontás a sajátmozgást két komponensre:

$U$ : Sajátmozgás a apex felé mutató főcírcsere felé (pozitív, ha elfelé mutat)

$\tau$ :  $U$ - $\kappa$  merőleges

$$U = \mu_{\alpha} \cos \delta \sin \psi - \mu_{\delta} \cos \psi$$

$$\tau = \mu_{\delta} \sin \psi + \mu_{\alpha} \cos \delta \cos \psi$$



$v_0 \sin \lambda$ : a Nap mozgásának komponense a apex  
láthatóságuk növekedés.  
 $\rightarrow$  sajátmozgást okoz

$$v_0 \sin \lambda / 4.74 d = \pi'' v_0 \sin \lambda / 4.74$$

$\rightarrow$  ezt nevezhetjük  $v_0$ -nak

Emléttük a LSR-ben vizsgált mozgás is ~~ez~~  $v_*$ -t. Tehát

(1) 
$$U = v_* + \pi'' \frac{v_0 \sin \lambda}{4.74} \rightarrow$$
 ez minden  $*$ -ra igaz a miunkban



# Szekuláris parallaxis

Eredetileg a diffrakció = szövegszerkeztetés.

azonosítjuk be (1)-t  $\sin \lambda$ -val, majd összegezzük:

$$\sum_{i=1}^n v_i \sin \lambda_i = \sum_{i=1}^n v_{*i} \sin \lambda_i + \frac{\overline{\pi}'' \nu_0}{4.74} \sum_{i=1}^n \sin^2 \lambda_i$$

ahol  $\overline{\pi}''$  a minta átlagos parallaxisa.

Ha az egyes vektorok random elosztásban vannak LSR-keresés  $\rightarrow v_{*i}$  az átlagos értékek

Összeadva az  $n$ -et,  $\langle \rangle$  átlag:

$$\overline{\pi}'' = \frac{4.74 \langle v \sin \lambda \rangle}{\nu_0 \langle \sin^2 \lambda \rangle}$$

$\nu_0$ -t tudjuk; a távolságot  $\rightarrow$  ismerhetjük,  $\overline{\pi}''$  értékes lehet, ha jól választjuk a mintát.

# Statisztikus parallaxis

Feltétel: ha elég nagy a minta, akkor a nullához álló, radialis sebességhez képest a nullához álló, transzverzális sebességvel (hiszen nincs  $\langle v_x \rangle$  és  $\langle v_y \rangle$ ).

Gondosan megválasztott mintánál létszámuknál  $v_r$  álló, majd azt mondjuk, ez megfelel  $v_r$  álló, majd azt mondjuk, hogy a  $v_r$  sebességét a  $v_r$  be a minta álló, tehát megfigyelés.

Hasonló megfontolással, mint a radialis parallaxisnál:

$$\overline{\pi}'' = \frac{4.74 \langle |v| \rangle}{\langle |v_r + v_0 \cos \lambda| \rangle}$$

## SECULAR PARALLAX OF THE S STARS

C. B. STEPHENSON

Warner and Swasey Observatory, Case Western Reserve University, East Cleveland, Ohio 44112

*Received 23 January 1978; revised 24 March 1978*

## ABSTRACT

The available radial velocities for 27 S stars do not indicate any significant deviation in the solar motion from the basic solar motion, which has therefore been used to derive the group mean parallax from 23 AGK3 and Yale-Cape (Hoffleit 1967-1971) proper motions. Variable and nonvariable stars have been treated together. The solar motion is poorly reflected in the proper motions, as it was in earlier data. If apparent magnitudes at maximum are used for the variables, the indicated mean visual absolute magnitude for all the stars is  $+2.4 \pm 0.8$  (p.e.), the quoted p.e. being internal; if the space motion given by the radial velocities is adopted,  $\langle M_v \rangle$  rises to  $+1.7$ . Thus, newer data, representing somewhat more stars than earlier studies, confirm previous evidence that the S stars are not, on the average, highly luminous objects. The uncertainties, mainly in the proper motions, are great enough that this result is not in serious conflict with previous estimates of  $\langle M_v \rangle$  near  $-1$ . There is some evidence that the apex of solar motion determined from small AGK3 proper motions is influenced by color index, in the case of the reddest stars.

## THE ABSOLUTE MAGNITUDE OF RRc VARIABLES FROM STATISTICAL PARALLAX

JUNA A. KOLLMEIER<sup>1</sup>, DOROTA M. SZCZYGIEL<sup>2</sup>, CHRISTOPHER R. BURNS<sup>1</sup>, ANDREW GOULD<sup>2</sup>, IAN B. THOMPSON<sup>1</sup>,  
 GEORGE W. PRESTON<sup>1</sup>, CHRISTOPHER SNEDEN<sup>3</sup>, JEFFREY D. CRANE<sup>1</sup>, SUBO DONG<sup>4</sup>, BARRY F. MADORE<sup>1</sup>, NIDIA MORRELL<sup>1</sup>,  
 JOSÉ L. PRIETO<sup>1,5</sup>, STEPHEN SHECTMAN<sup>1</sup>, JOSHUA D. SIMON<sup>1</sup>, AND EDWARD VILLANUEVA<sup>1</sup>

<sup>1</sup> Observatories of the Carnegie Institution of Washington, 813 Santa Barbara Street, Pasadena, CA 91101, USA

<sup>2</sup> Department of Astronomy, The Ohio State University, 4051 McPherson Laboratory, Columbus, OH 43210, USA

<sup>3</sup> Department of Astronomy, University of Texas at Austin, TX 78712, USA

<sup>4</sup> Institute for Advanced Study, 500 Einstein Drive, Princeton, NJ 08540, USA

<sup>5</sup> Department of Astrophysical Sciences, Princeton University, Princeton, NJ 08544, USA

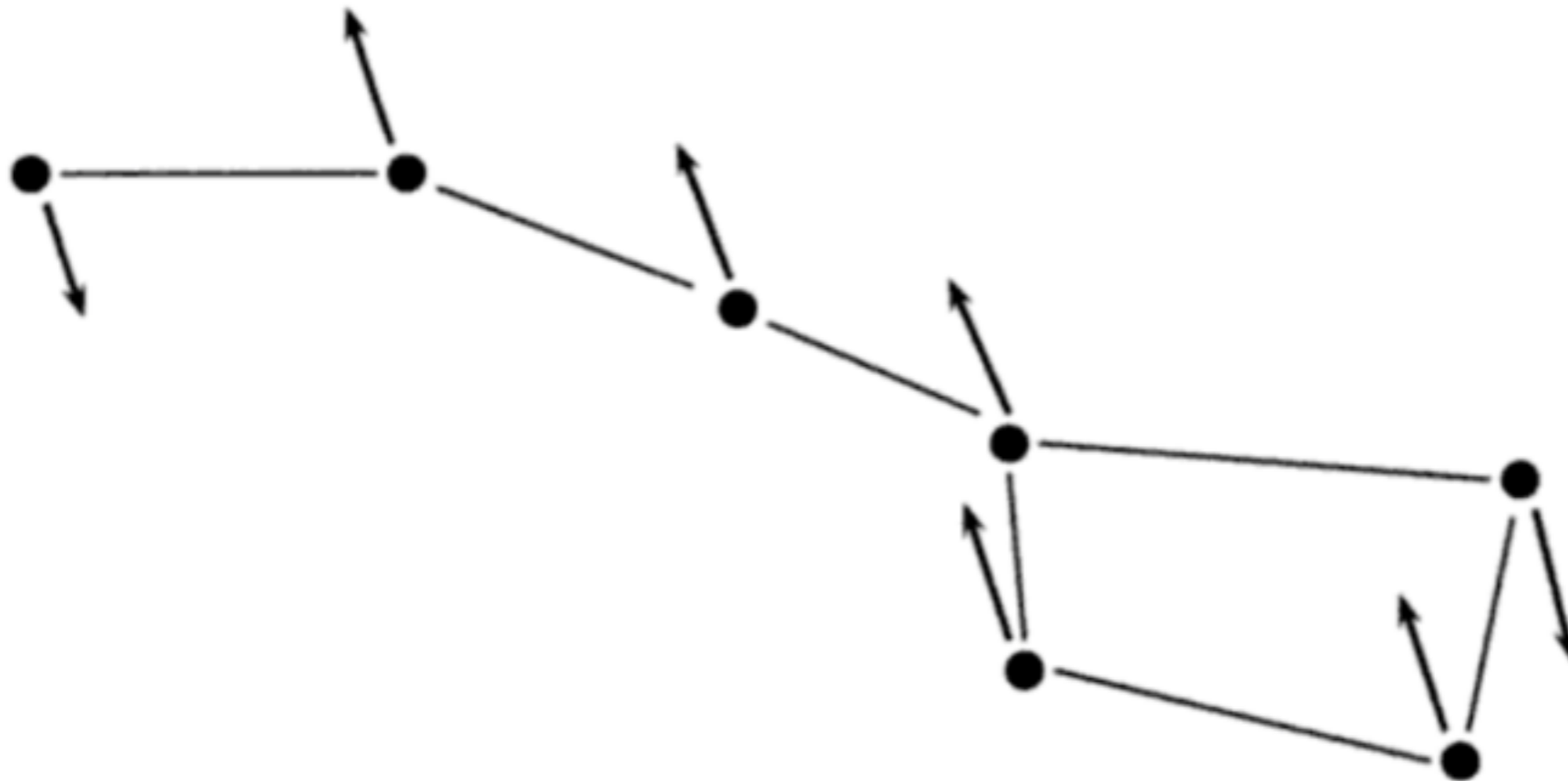
*Received 2012 August 13; accepted 2013 August 2; published 2013 September 4*

## ABSTRACT

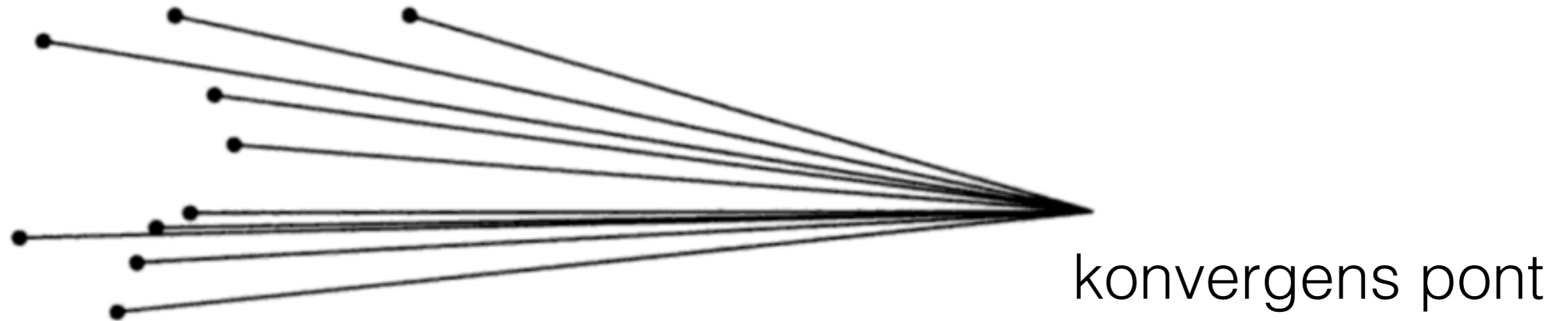
We present the first definitive measurement of the absolute magnitude of RR Lyrae c-type variable stars (RRc) determined purely from statistical parallax. We use a sample of 242 RRc variables selected from the All Sky Automated Survey for which high-quality light curves, photometry, and proper motions are available. We obtain high-resolution echelle spectra for these objects to determine radial velocities and abundances as part of the Carnegie RR Lyrae Survey. We find that  $M_{V,RRc} = 0.59 \pm 0.10$  at a mean metallicity of  $[Fe/H] = -1.59$ . This is to be compared with previous estimates for RRab stars ( $M_{V,RRab} = 0.76 \pm 0.12$ ) and the only *direct* measurement of an RRc absolute magnitude (RZ Cephei,  $M_{V,RRc} = 0.27 \pm 0.17$ ). We find the bulk velocity of the halo relative to the Sun to be  $(W_\pi, W_\theta, W_z) = (12.0, -209.9, 3.0) \text{ km s}^{-1}$  in the radial, rotational, and vertical directions with dispersions  $(\sigma_{W_\pi}, \sigma_{W_\theta}, \sigma_{W_z}) = (150.4, 106.1, 96.0) \text{ km s}^{-1}$ . For the disk, we find  $(W_\pi, W_\theta, W_z) = (13.0, -42.0, -27.3) \text{ km s}^{-1}$  relative to the Sun with dispersions  $(\sigma_{W_\pi}, \sigma_{W_\theta}, \sigma_{W_z}) = (67.7, 59.2, 54.9) \text{ km s}^{-1}$ . Finally, as a byproduct of our statistical framework, we are able to demonstrate that UCAC2 proper-motion errors are significantly overestimated as verified by UCAC4.

*Key words:* distance scale – Galaxy: fundamental parameters – Galaxy: kinematics and dynamics – Galaxy: structure – stars: distances – stars: variables: RR Lyrae

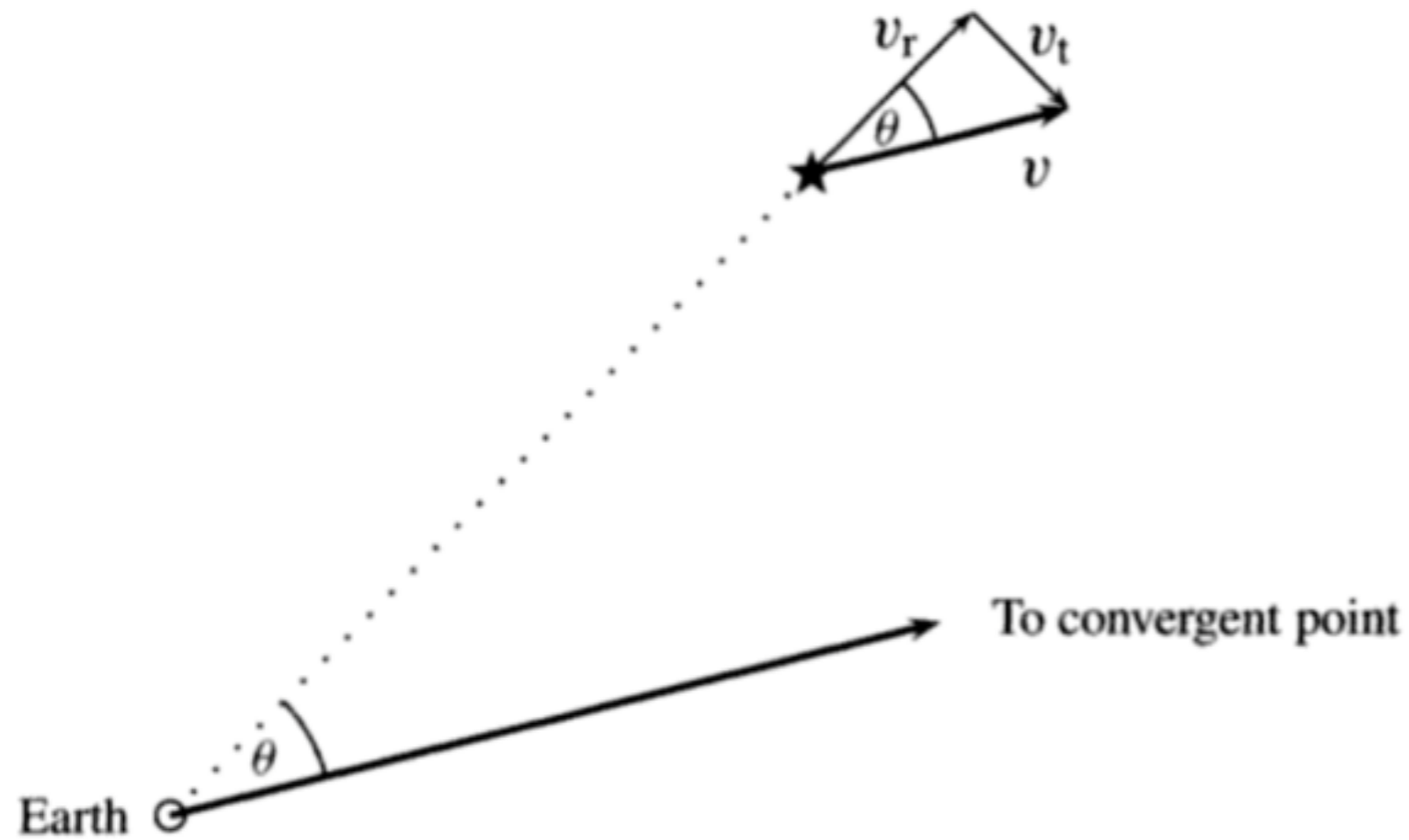
# Mozgási halmaz módszer (moving cluster)



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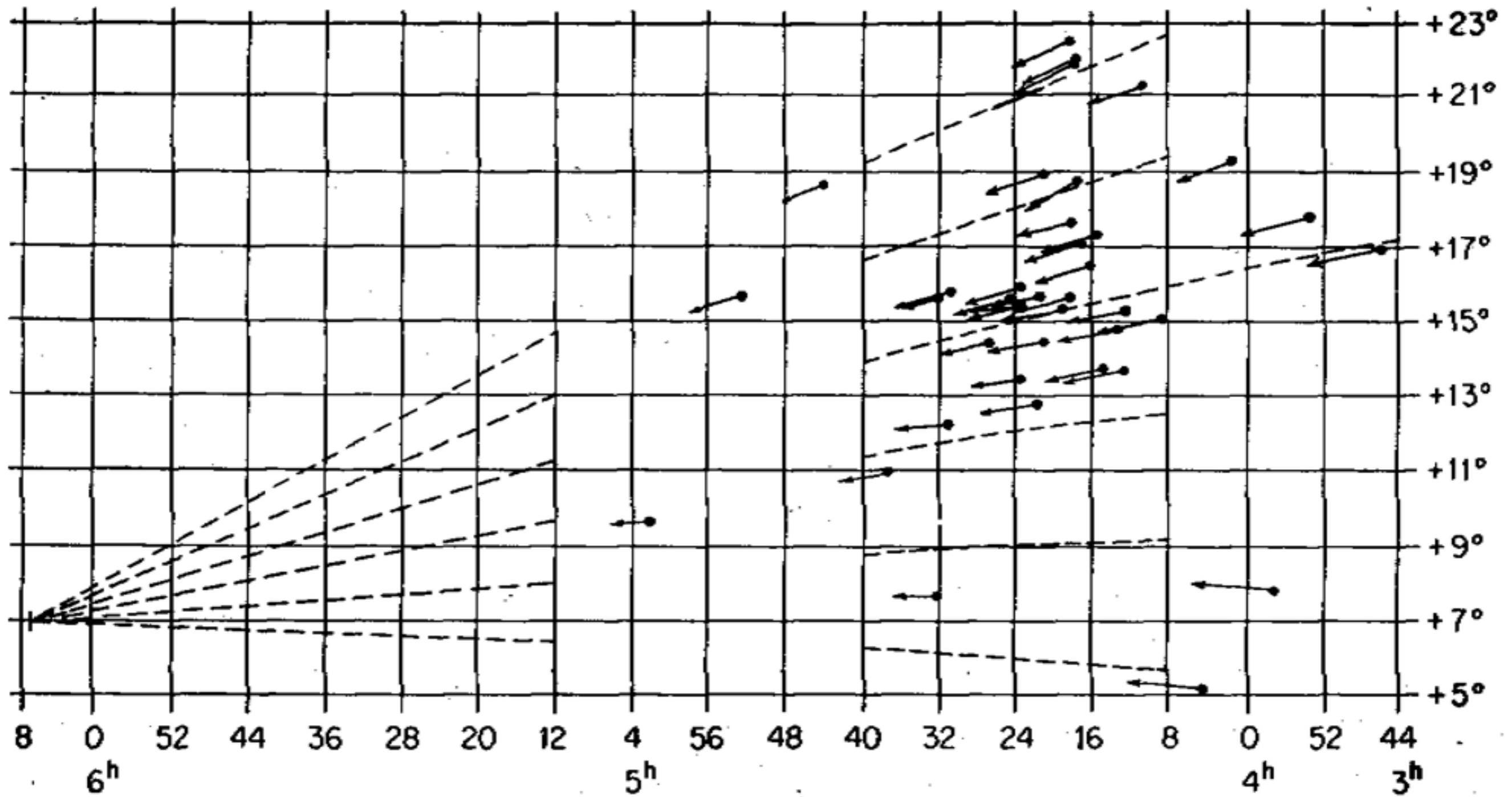


$$v_t = v_r \operatorname{tg} \theta$$

$\theta$  is  $v_r$  ismeretlen  $v_t$  adunkkal.  
 $\mu$  szögátmozgását mérve a távolság  
adódik

$$d = \frac{v_r \operatorname{tg} \theta}{4.74 \mu}$$

# Mozgási halmaz módszer (moving cluster)



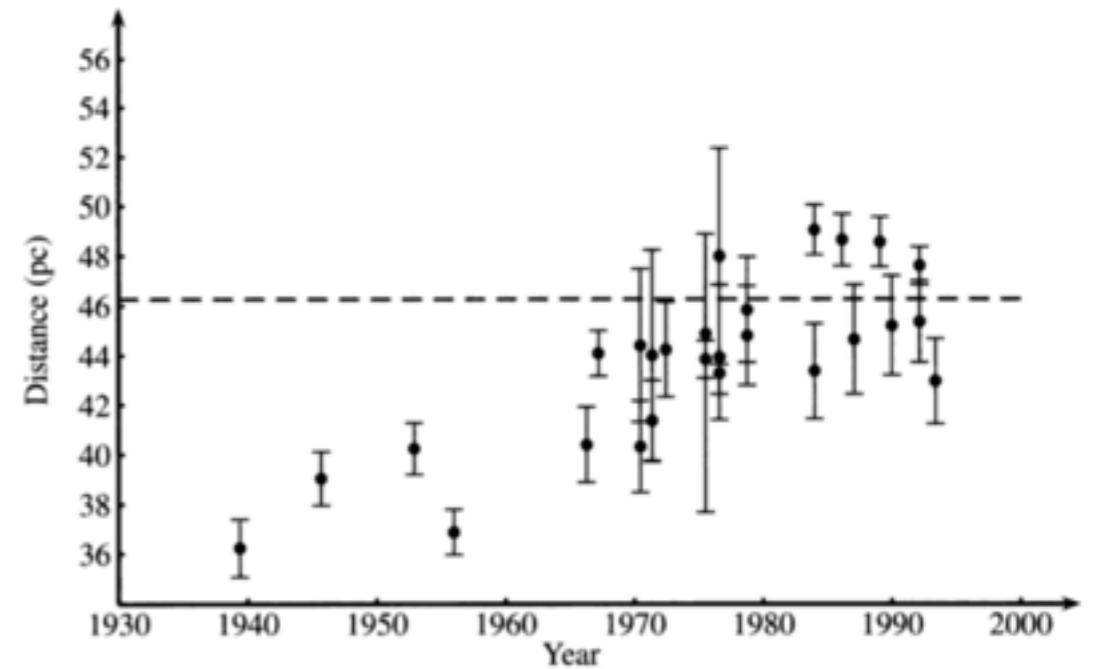


# Mozgási halmaz módszer (moving cluster)

UMa, ~60 csillag, 24 pc

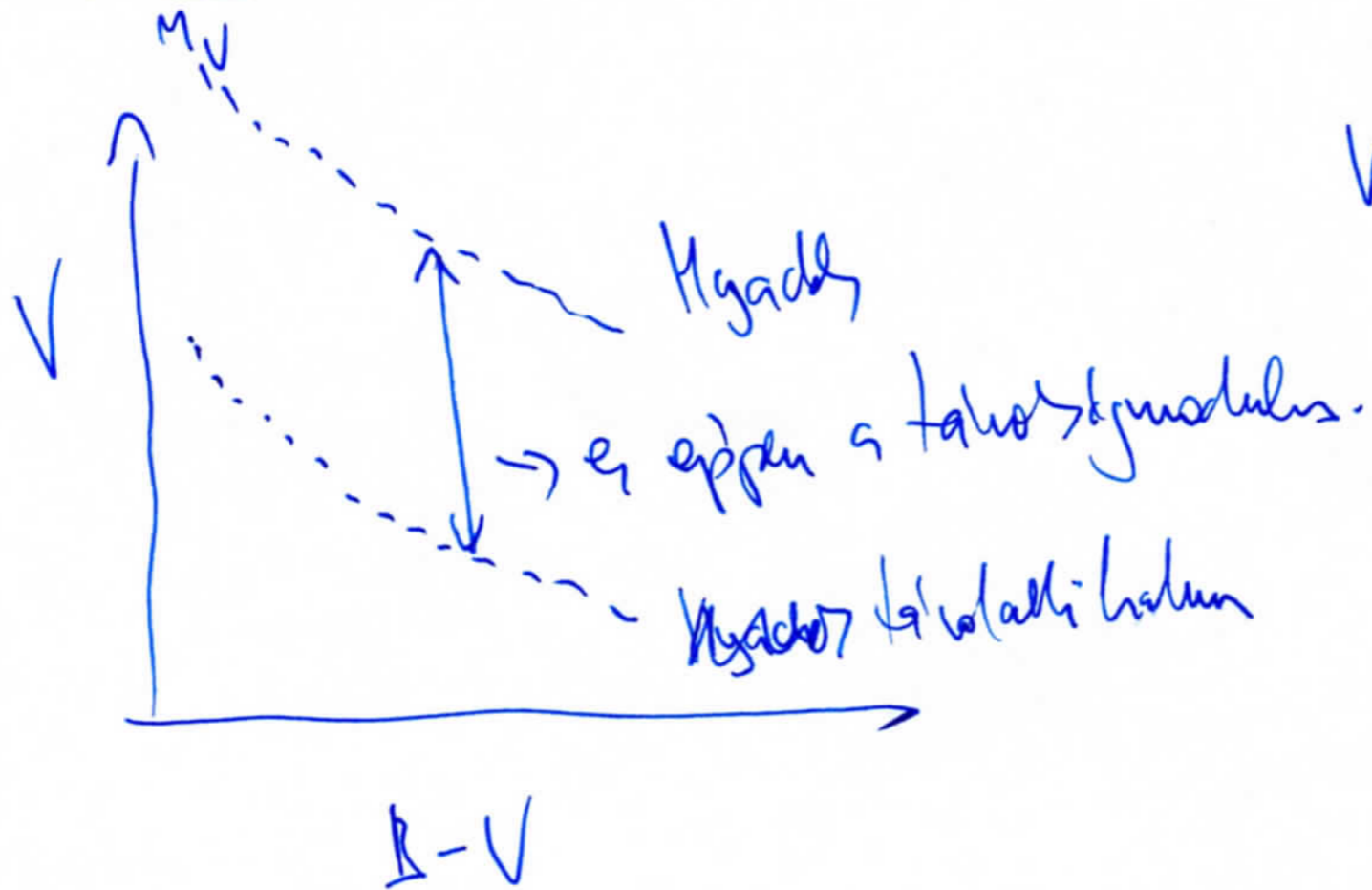
Sco-Cen, ~100 csillag, 170 pc

Hyadok, nyílthalmaz, ~46 pc



A Nyador f'rozvartalan tartas' mellezget fevaltolha leshetys'v'el'is a

f'rozvart' illes'te's'!



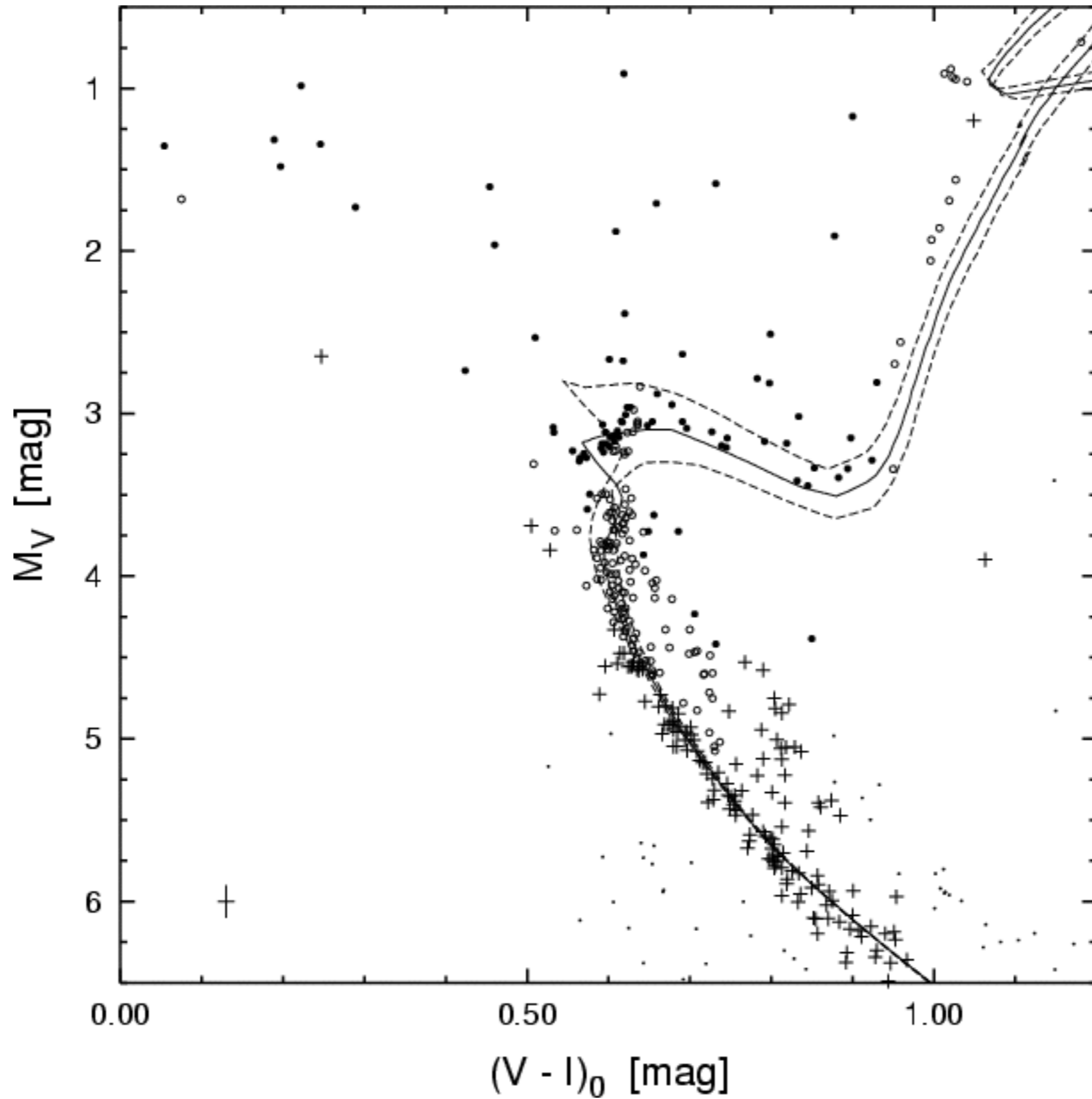
$$V - M_V = -5 + 5 \text{ keng'el}$$

ad'at' ~ 70 k'pe talos'gy'nos'ig  
k'ap'el'eg

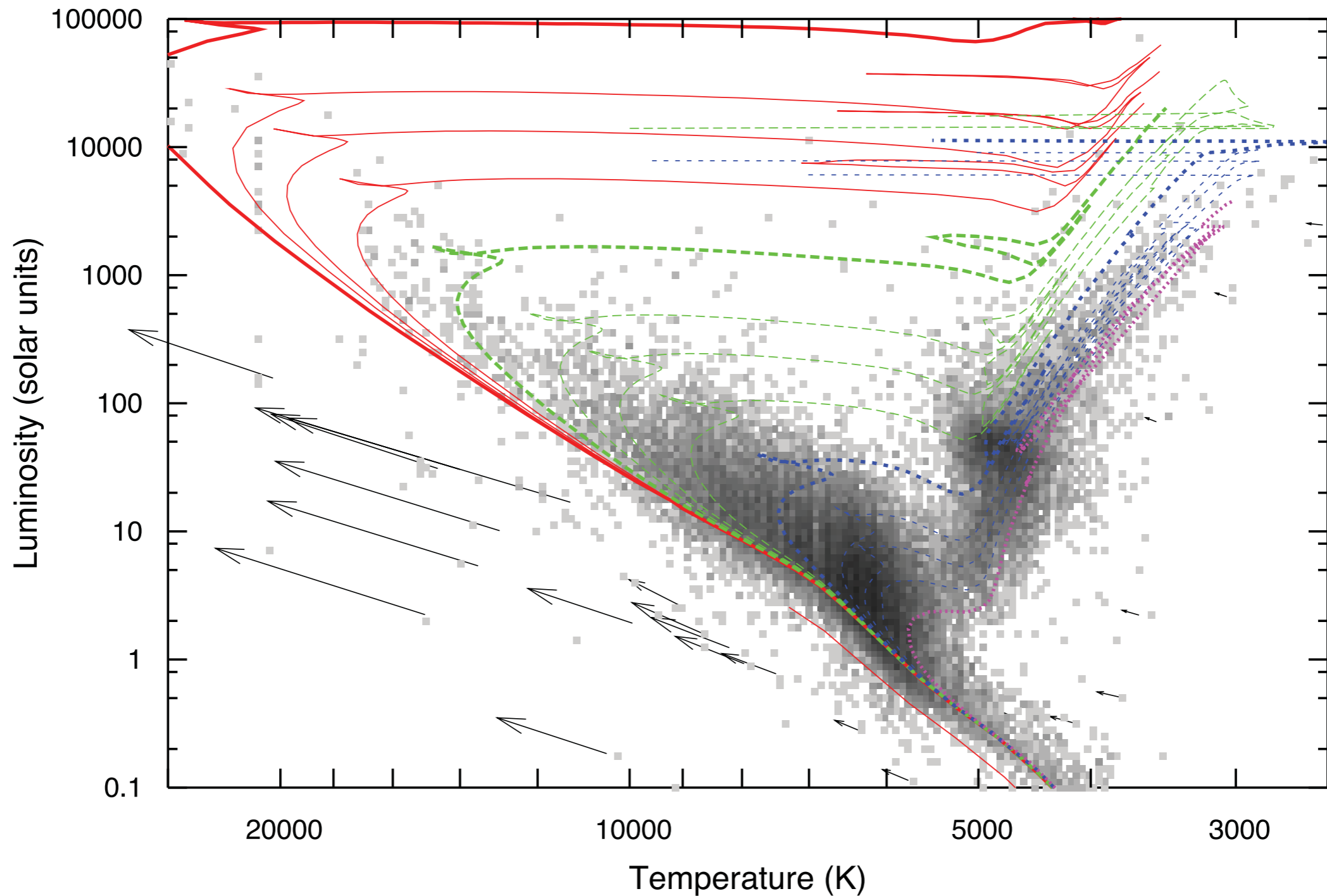
Spektrométer parallaxis ely pontatlan de nagyon gyors lehetőségek:  
a) szubtilis fraxozat alapján tárgyalás úgy mi az ömefizetés  
a) spektrométer is az abszolút frekvencia lezített.

$$\text{Sp. típus} \rightarrow \left. \begin{array}{l} M_v \\ v \end{array} \right\} \rightarrow \underline{\underline{d}}$$

Izokrón-illesztés (izokrón: azonos korú  
csillagmodellek eltérő tömegekre)



M67



**Figure 2.** Density-coded HR diagram for the 200-pc sample (grey-scale). Overplotted are solar-metallicity isochrones from the Padova models (Bertelli et al. 2008; Marigo et al. 2008) at 10, 20, 30 and 50 Myr (solid, red lines); 100, 200, 300 and 500 Myr (long-dashed green lines); 1, 2, 3 and 5 Gyr (short-dashed blue lines) and 10 Gyr (dotted magenta line). The thin red line to the left of the main sequence is a zero-age isochrone at  $[\text{Fe}/\text{H}] = -1$  to illustrate the blueward shift caused by decreasing metallicity. The black arrows show the effect of de-reddening individual sources by  $E(B - V) = 0.1$  mag.

(McDonald et al. 2012)

# Unveiling new members in five nearby young moving groups

A. Moór<sup>1\*</sup>, Gy. M. Szabó<sup>1,2,3</sup>, L. L. Kiss<sup>1,2,4</sup>, Cs. Kiss<sup>1</sup>, P. Ábrahám<sup>1</sup>, J. Szulágyi<sup>1</sup>

Á. Kóspál<sup>5</sup>, T. Szalai<sup>3</sup>

<sup>1</sup>*Konkoly Observatory, Research Centre for Astronomy and Earth Sciences, Hungarian Academy of Sciences, PO Box 67, H-1525 Budapest, Hungary*

<sup>2</sup>*ELTE Gothard-Lendület Research Group, 9700 Szombathely, Hungary*

<sup>3</sup>*Dept. of Experimental Physics and Astronomical Observatory, 6720 Szeged Dóm tér 9., Hungary*

<sup>4</sup>*Sydney Institute for Astronomy, School of Physics, University of Sydney, NSW 2006, Australia*

<sup>5</sup>*Research and Scientific Support Department, European Space Agency*

*(ESA-ESTEC, SRE-SA),*

*P.O. Box 299, 2200 AG, Noordwijk, The Netherlands ; ESA fellow.*

Accepted ... Received ...; in original form ...

## ABSTRACT

In the last decade many kinematic groups of young stars ( $< 100$  Myr) were discovered in the solar neighbourhood. Since the most interesting period of planet formation overlaps with the age of these groups, their well dated members are attractive targets for exoplanet searches by direct imaging. We combined astrometric, photometric and X-ray data, and applied strict selection criteria to explore the stellar content of five nearby moving groups. We identified more than 100 potential new candidate members in the  $\beta$  Pic moving group, and in the Tucana-Horologium, Columba, Carina, and Argus associations. In order to further assess and confirm their membership status, we analysed radial velocity data and lithium equivalent widths extracted from high-resolution spectra of 54 candidate stars. We identified 35 new probable/possible young moving group members: 4 in the  $\beta$  Pic moving group, 11 in the Columba association, 16 in the Carina association, and 4 in the Argus association. We found serendipitously a new AB Dor moving group member as well. For four Columba systems *Hipparcos* based parallaxes have already been available and as they are consistent with the predicted kinematic parallaxes, they can be considered as secure new members.

# A search for new members of the $\beta$ Pictoris, Tucana–Horologium and $\epsilon$ Cha moving groups in the RAVE data base

L. L. Kiss,<sup>1,2\*</sup> A. Moór,<sup>1</sup> T. Szalai,<sup>3</sup> J. Kovács,<sup>4</sup> D. Bayliss,<sup>5</sup> G. F. Gilmore,<sup>6</sup> O. Bienaymé,<sup>7</sup> J. Binney,<sup>8</sup> J. Bland-Hawthorn,<sup>2</sup> R. Campbell,<sup>9</sup> K. C. Freeman,<sup>5</sup> J. P. Fulbright,<sup>10</sup> B. K. Gibson,<sup>11</sup> E. K. Grebel,<sup>12</sup> A. Helmi,<sup>13</sup> U. Munari,<sup>14</sup> J. F. Navarro,<sup>15</sup> Q. A. Parker,<sup>16,17</sup> W. Reid,<sup>16</sup> G. M. Seabroke,<sup>18</sup> A. Siebert,<sup>7</sup> A. Siviero,<sup>14,19</sup> M. Steinmetz,<sup>19</sup> F. G. Watson,<sup>17</sup> M. Williams,<sup>19</sup> R. F. G. Wyse<sup>10</sup> and T. Zwitter<sup>20,21</sup>

<sup>1</sup>*Konkoly Observatory of the Hungarian Academy of Sciences, PO Box 67, H-1525 Budapest, Hungary*

<sup>2</sup>*Sydney Institute for Astronomy, School of Physics, University of Sydney, NSW 2006, Australia*

<sup>3</sup>*Department of Optics and Quantum Electronics, University of Szeged, 6720 Szeged, Dóm tér 9., Hungary*

<sup>4</sup>*Gothard Astrophysical Observatory, ELTE University, 9707 Szombathely, Hungary*

<sup>5</sup>*Research School of Astronomy and Astrophysics, The Australian National University, Canberra, Australia*

<sup>6</sup>*Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA*

<sup>7</sup>*Observatoire de Strasbourg, 11 Rue de L'Université, 67000 Strasbourg, France*

<sup>8</sup>*Rudolf Pierls Center for Theoretical Physics, University of Oxford, 1 Keble Road, Oxford OX1 3NP*

<sup>9</sup>*Western Kentucky University, Bowling Green, Kentucky, USA*

<sup>10</sup>*Johns Hopkins University, 3400 N Charles Street, Baltimore, MD 21218, USA*

<sup>11</sup>*Jeremiah Horrocks Institute for Astrophysics & Supercomputing, University of Central Lancashire, Preston, Lancashire PR1 2HE*

<sup>12</sup>*Astronomisches Rechen-Institut, Zentrum für Astronomie der Universität Heidelberg, D-69120 Heidelberg, Germany*

<sup>13</sup>*Kapteyn Astronomical Institute, University of Groningen, Postbus 800, 9700 AV Groningen, the Netherlands*

<sup>14</sup>*INAF Osservatorio Astronomico di Padova, Via dell'Osservatorio 8, Asiago I-36012, Italy*

<sup>15</sup>*University of Victoria, PO Box 3055, Station CSC, Victoria, BC V8W 3P6, Canada*

<sup>16</sup>*Macquarie University, Sydney, NSW 2109, Australia*

<sup>17</sup>*Australian Astronomical Observatory, PO Box 296, Epping, NSW 1710, Australia*

<sup>18</sup>*Mullard Space Science Laboratory, University College London, Holmbury St Mary, Dorking RH5 6NT*

<sup>19</sup>*Astrophysikalisches Institut Potsdam, An der Sternwarte 16, D-14482 Potsdam, Germany*

<sup>20</sup>*Faculty of Mathematics and Physics, University of Ljubljana, Jadranska 19, Ljubljana, Slovenia*

<sup>21</sup>*Center of excellence SPACE-SI, Ljubljana, Slovenia*

Accepted 2010 September 7. Received 2010 September 6; in original form 2010 July 6

## ABSTRACT

We report on the discovery of new members of nearby young moving groups, exploiting the full power of combining the Radial Velocity Experiment (RAVE) survey with several stellar age diagnostic methods and follow-up high-resolution optical spectroscopy. The results include the identification of one new and five likely members of the  $\beta$  Pictoris moving group, ranging from spectral types F9 to M4 with the majority being M dwarfs, one K7 likely member of the  $\epsilon$  Cha group and two stars in the Tucana–Horologium association. Based on the positive identifications, we foreshadow a great potential of the RAVE data base in progressing towards a full census of young moving groups in the solar neighbourhood.