

# Properties of circumstellar disks

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# Main literature

Jonathan P. Williams & Lucas A. Cieza  
Annu. Rev. Astron. Astrophys. 2011, 49:67–117  
(Chapter 4)



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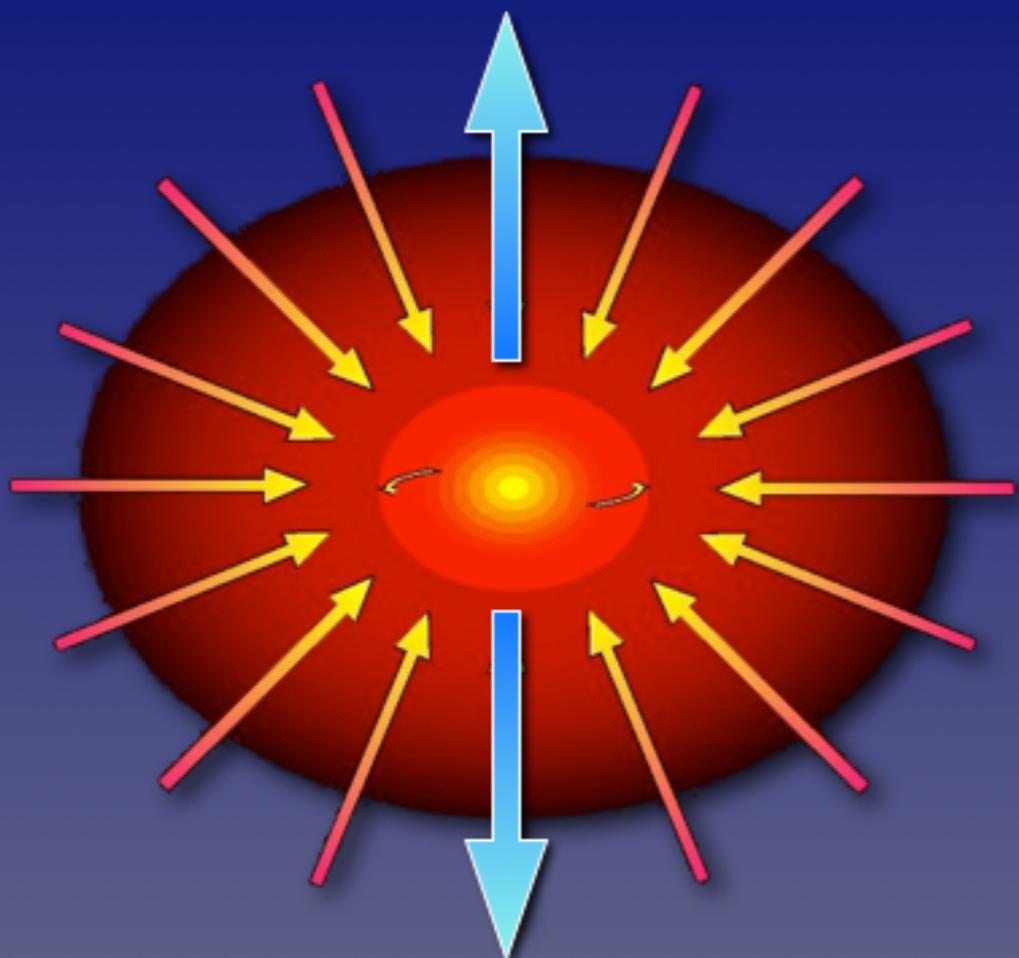
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## Protoplanetary Disks and Their Evolution

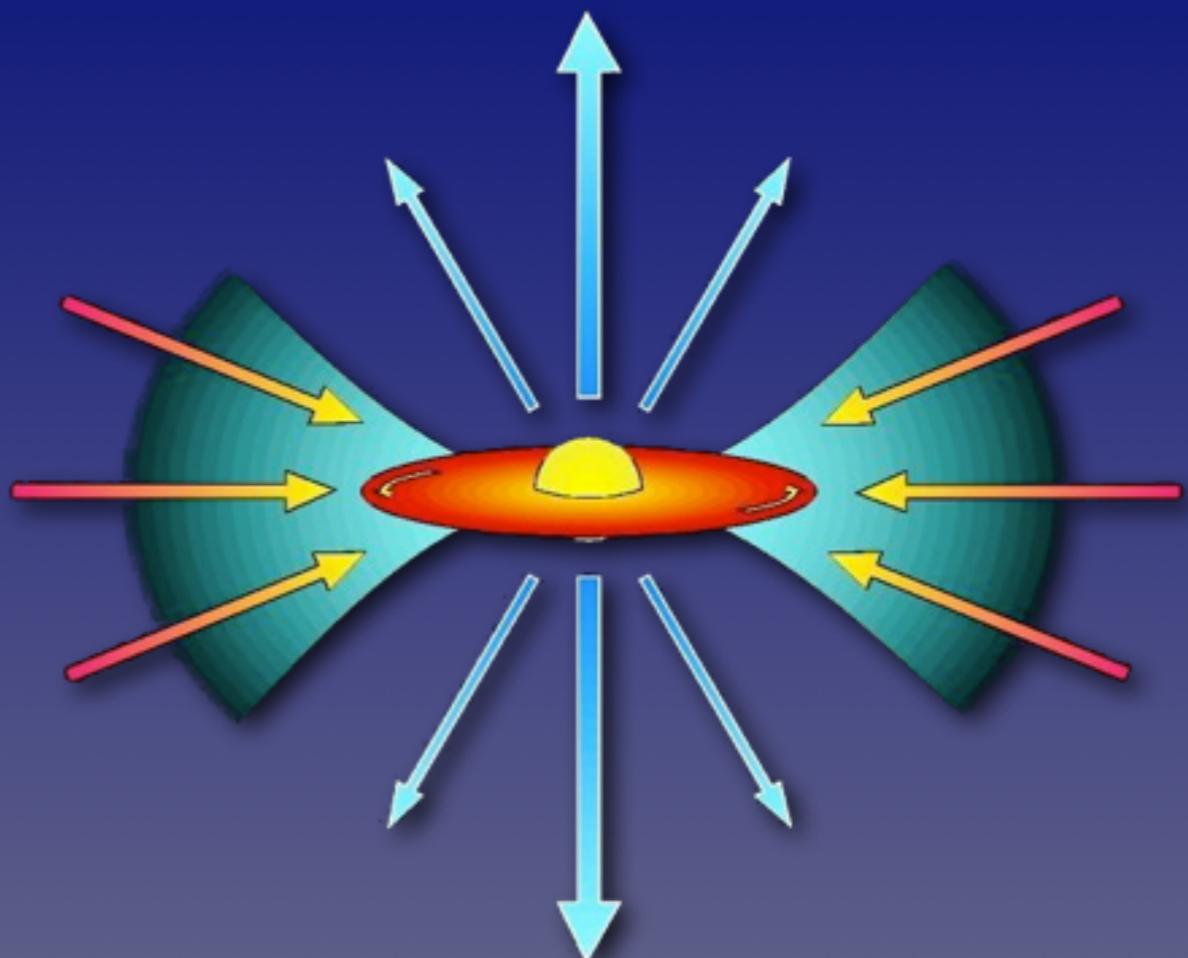
Jonathan P. Williams and Lucas A. Cieza

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email: [jpw@ifa.hawaii.edu](mailto:jpw@ifa.hawaii.edu), [cieza@ifa.hawaii.edu](mailto:cieza@ifa.hawaii.edu)

# The isolated star formation paradigm



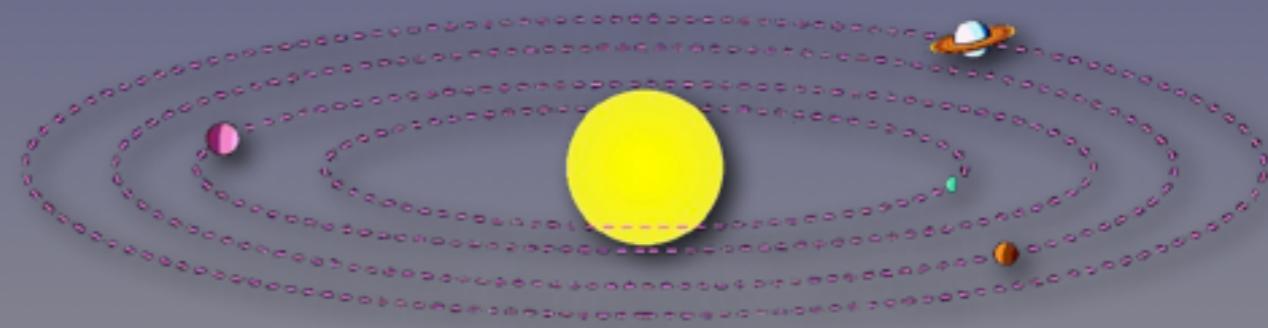
Class 0:  
 $10^4$  yrs; 10- $10^4$  AU; 10-300 K



Class I-II:  
 $10^{5-6}$  yrs; 1-1000 AU; 100-3000 K



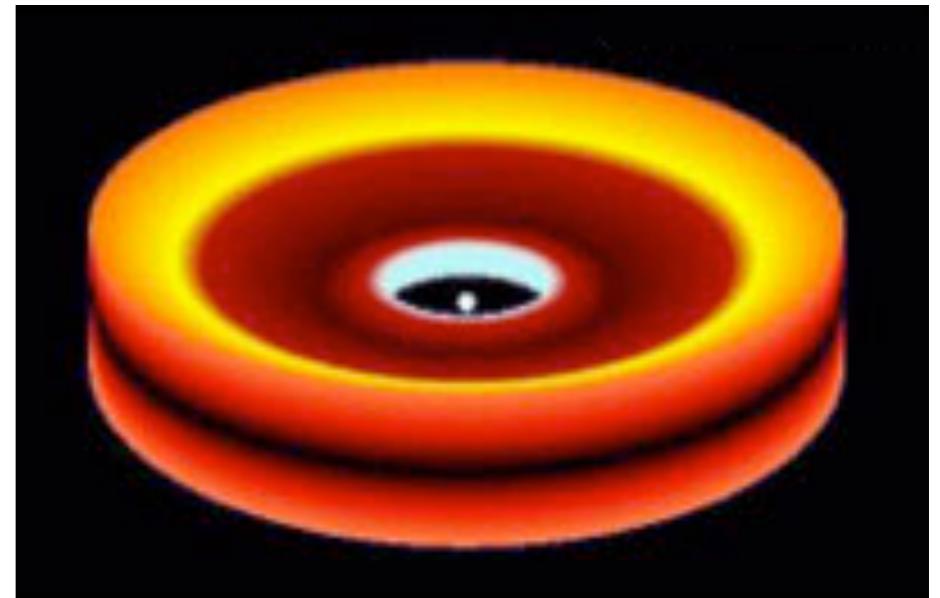
Class II-III:  
 $10^{6-7}$  yrs; 1-100 AU; 100-5000 K



Class IV:  
 $10^{7-9}$  yrs; 1-100 AU; 100-5000 K

# Class II disks

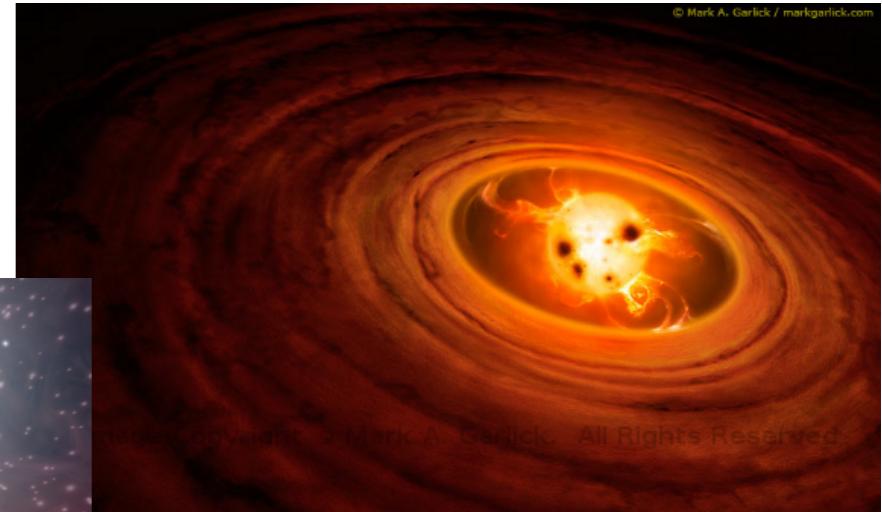
- Class 0 + Class I stage phase lasts about 0.5 Myr
- By the end of the Class I phase, the envelope disperses
- Star formation process is almost over (accretion may be still on-going at a low rate)
- Disk mass is typically only a few % of the stellar mass → **protoplanetary disk**, not protostellar disk



# Processes during disk evolution

Major processes that govern the disk evolution:

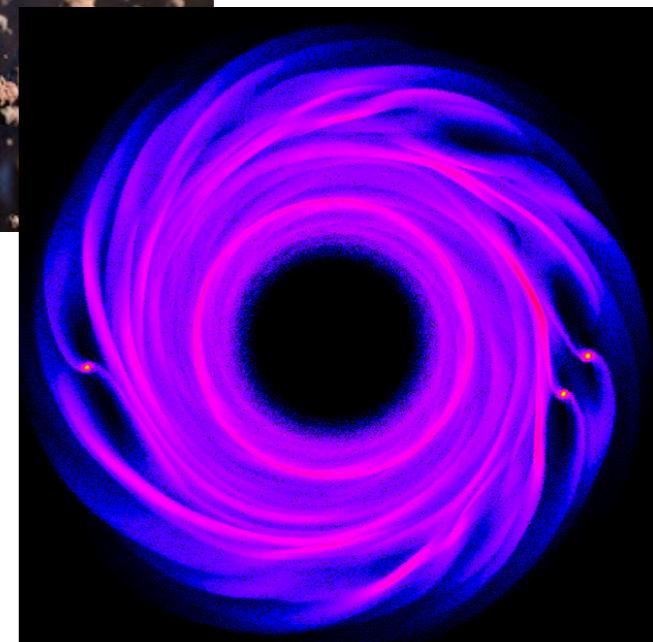
- accretion onto the star



- photoevaporation



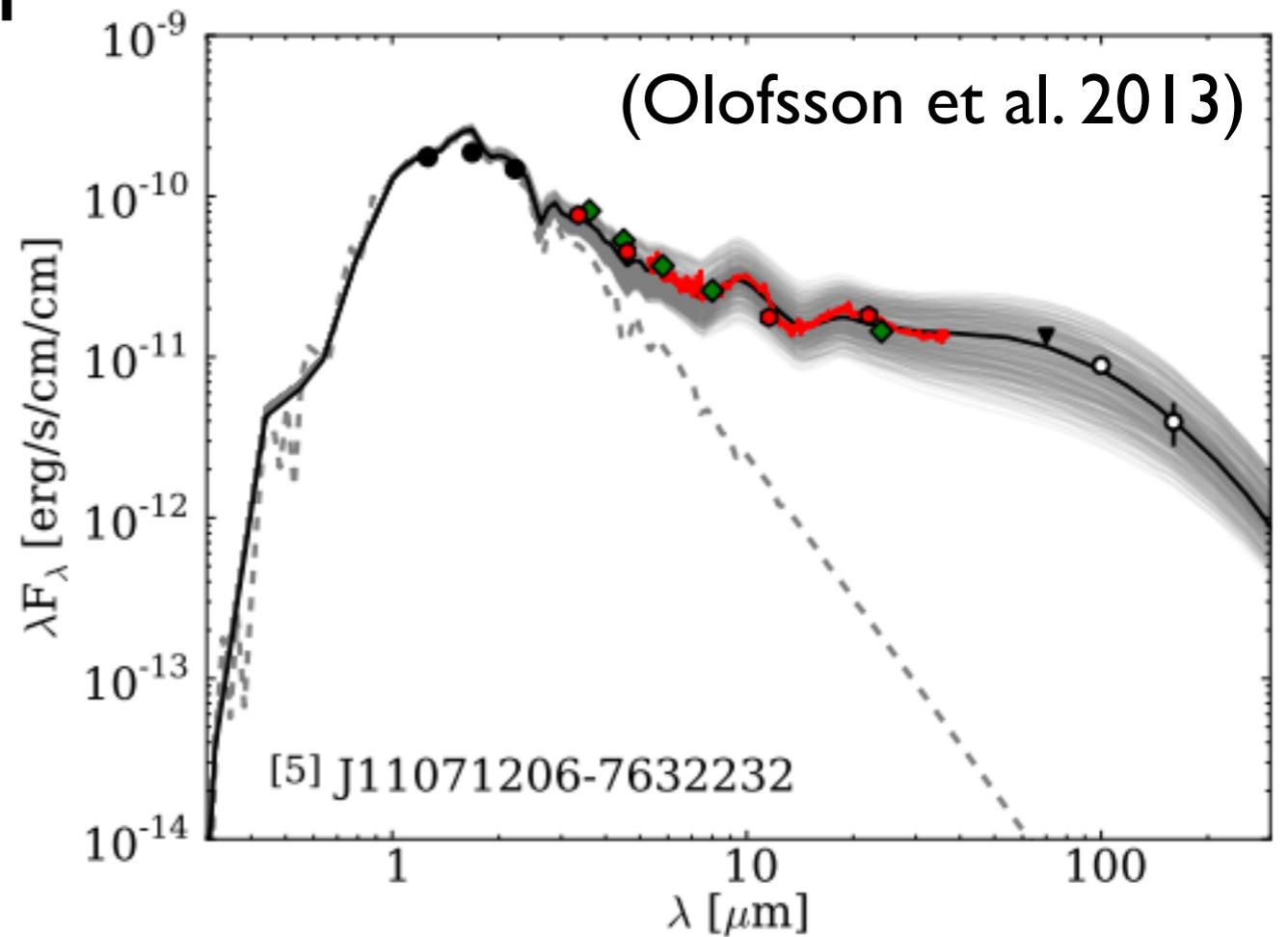
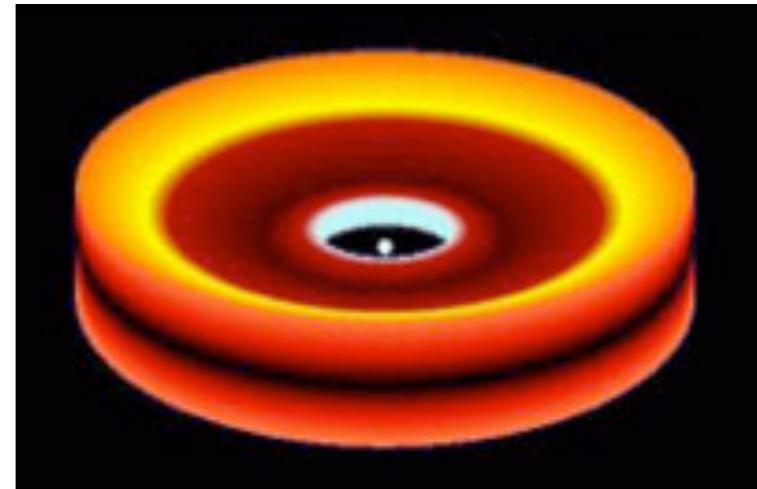
- agglomeration into larger bodies



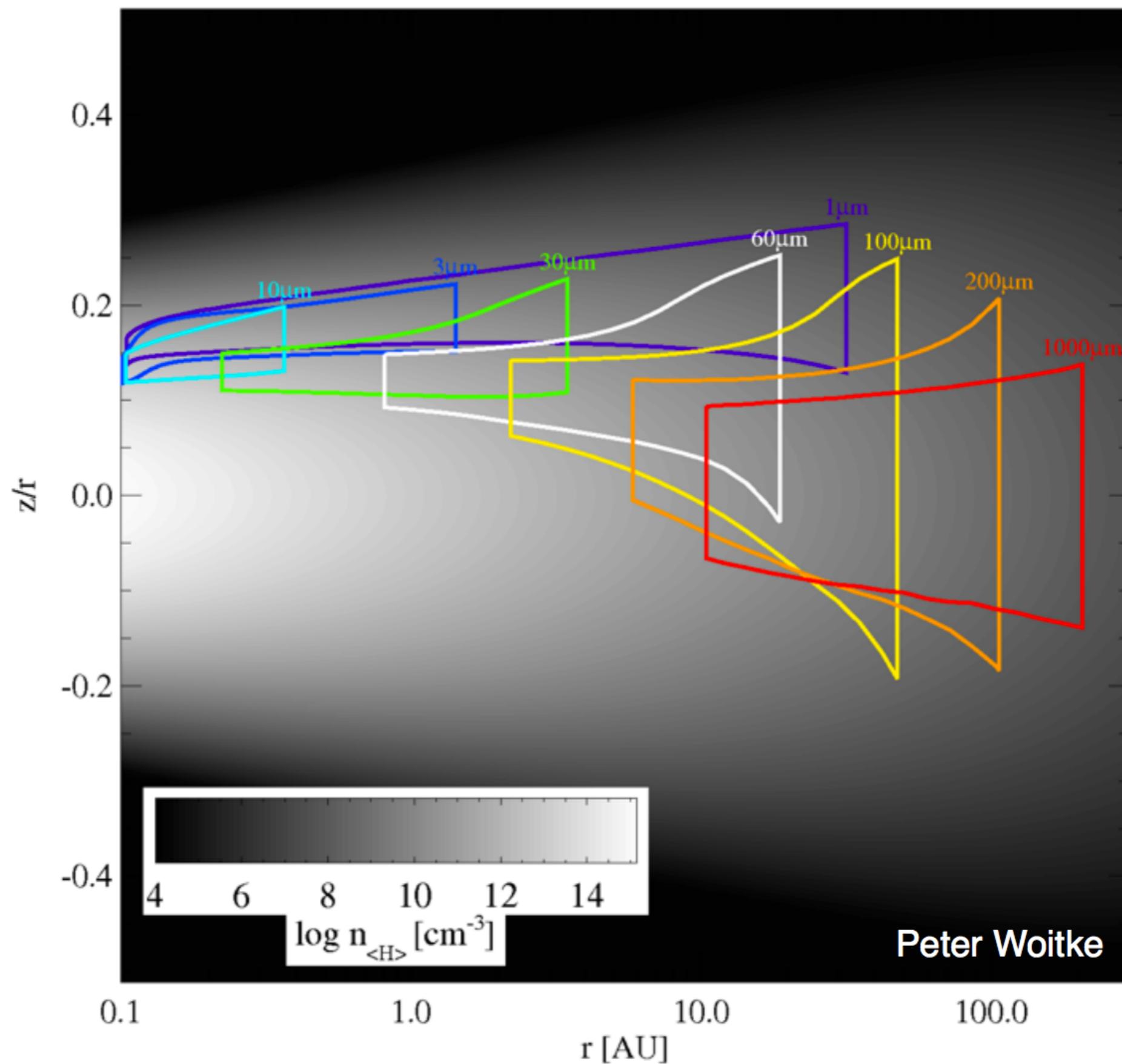
- dynamical interactions with stellar or planetary companions

# SED of Class II disks

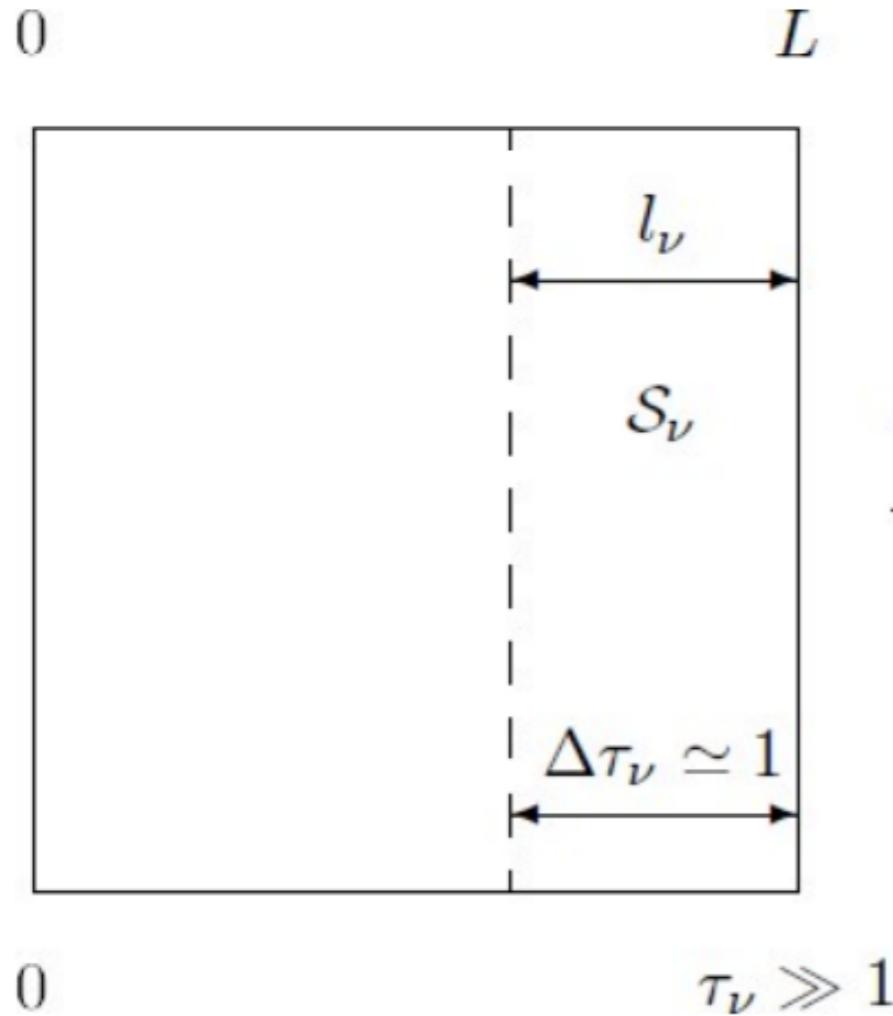
- Extinction is low → **stellar properties** can be observed in the optical/near-IR
- What other information can we get from the SED?
  - Disk mass?
  - Disk size?
  - Disk structure?
  - Disk composition?



# Origin of disk emission vs $\lambda$



# Disk mass: radiative transfer



(Robert Estalella)

$$I_\nu(\tau_\nu) = I_\nu(0) e^{-\tau_\nu} + \mathcal{S}_\nu (1 - e^{-\tau_\nu})$$

**Optically thin limit ( $\tau_\nu \ll 1$ ):**  
intensity is proportional to the optical depth i.e. to the column density of the emitting material

$$I_\nu \simeq I_\nu(0) + \mathcal{S}_\nu \tau_\nu$$

**Optically thick limit ( $\tau_\nu \gg 1$ ):**  
radiation is coming from a thin surface layer with  $\Delta\tau_\nu = 1$ ; no information on the inside of the source  $I_\nu \simeq \mathcal{S}_\nu$

( $S_\nu$  : source function)

# Disk mass: dust thermal emission

- Flux density of a source with thermal emission from dust, at temperature  $T_d$  and solid angle  $\Omega_s$ :

$$S_\nu = B_\nu(T_d) (1 - e^{-\tau_\nu}) \Omega_s$$

- Absorption coefficient (**opacity**) per unit mass density (gas + dust) and unit length:  $\kappa_\nu$

$$\tau_\nu = \kappa_\nu \int_{\text{visual}} \rho dl$$

- Approximation for  $\kappa_\nu$ : power law of frequency with exponent  $\beta$  ( $\beta$  is usually between 1 and 2, depending on the dust properties):

$$\left[ \frac{\kappa_\nu}{\text{cm}^2 \text{ g}^{-1}} \right] = 0.1 \left[ \frac{\nu}{1000 \text{ GHz}} \right]^\beta$$

# Disk mass: dust thermal emission

- We can assume optically thin emission at submm and mm wavelengths (usual observations at 870  $\mu\text{m}$  / 345 GHz, 1.3 mm / 230 GHz, 2.7 mm / 110 GHz)
- In the Rayleigh-Jeans approximation, the flux density can be expressed in terms of the mass of the source:

$$S_\nu = \frac{2k\nu^2}{c^2} T_{\text{d}} \tau_\nu \Omega_{\text{S}} = \frac{2k\nu^2}{c^2} T_{\text{d}} \kappa_\nu \frac{A}{D^2} \int \rho dl = \frac{2k\nu^2}{c^2} T_{\text{d}} \kappa_\nu \frac{M}{D^2}$$

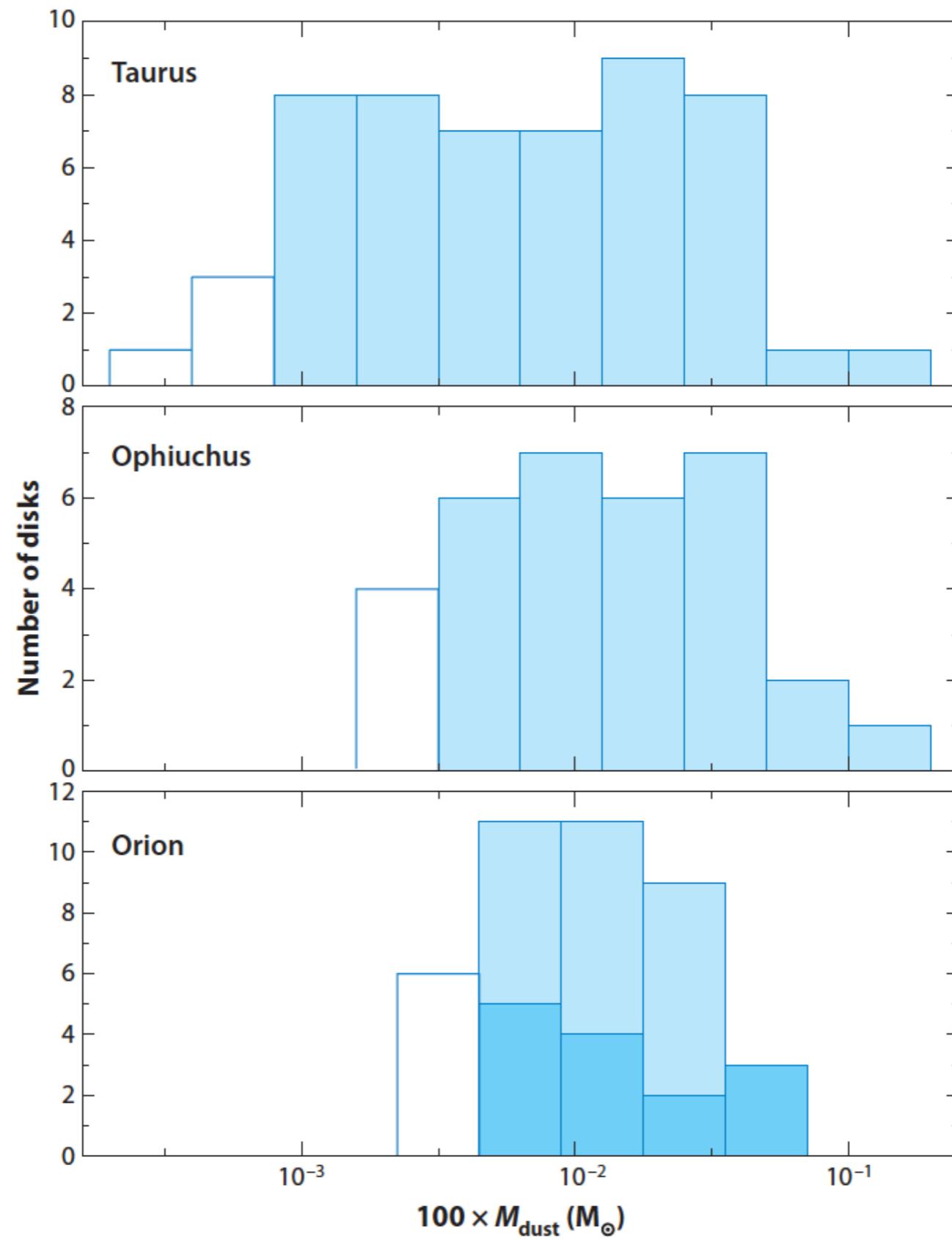
- In practical units:

$$\left[ \frac{M}{M_\odot} \right] = 1.6 \times 10^{-6} \left[ \frac{\nu}{1000 \text{ GHz}} \right]^{-(2+\beta)} \left[ \frac{S_\nu}{\text{Jy}} \right] \left[ \frac{T_{\text{d}}}{\text{K}} \right]^{-1} \left[ \frac{D}{\text{pc}} \right]^2$$

# Disk mass distribution

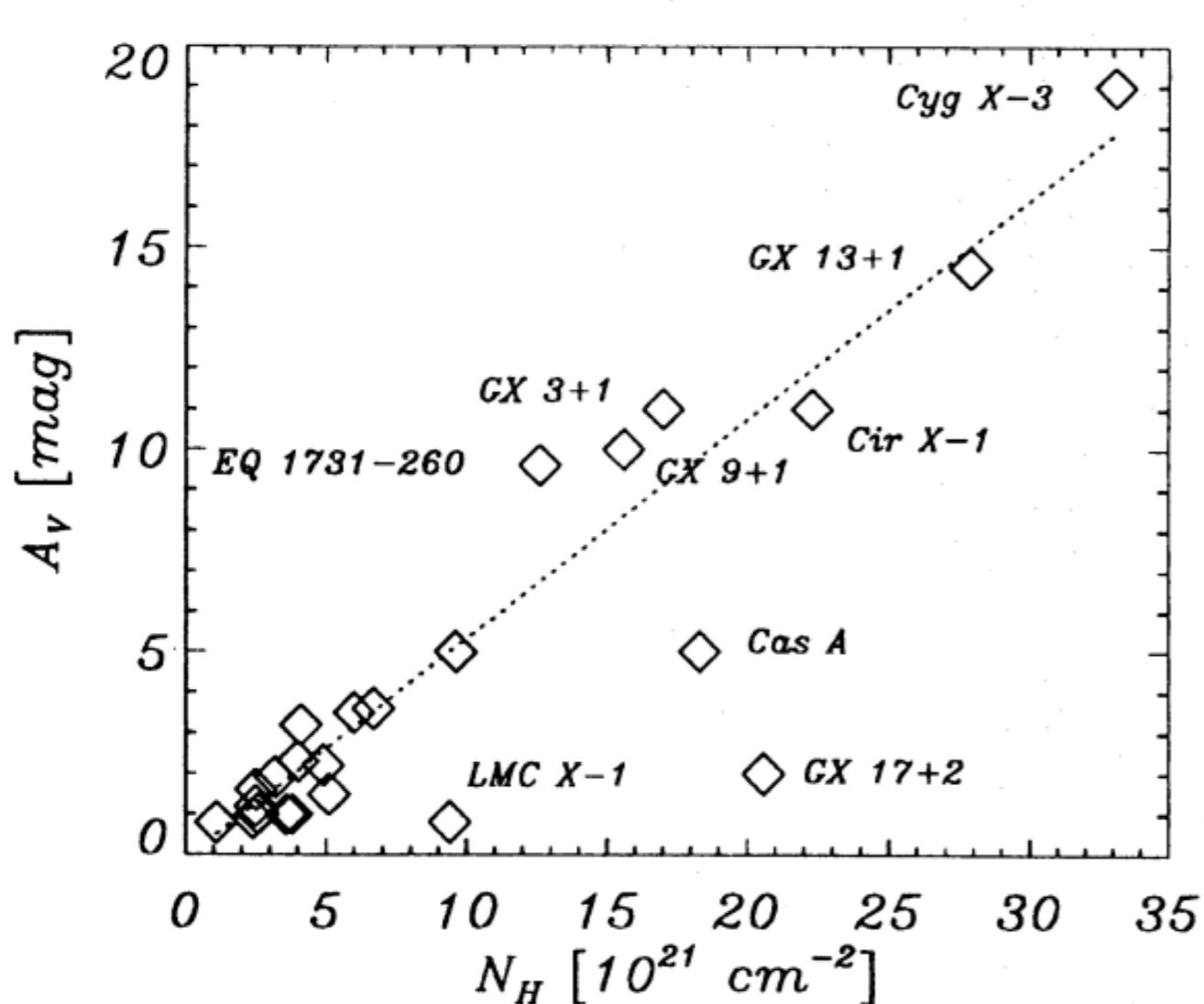
- Large mm surveys:  
Beckwith et al. (1990) for Taurus-Auriga  
André & Montmerle (1994) for Ophiuchus
- Andrews & Williams (2005, 2007)
- Median  $M_{\text{disk}} / M_{\text{star}} = 0.01$
- Mass distribution in log mass bins: flat until  $50 M_{\text{Jup}}$   
( $0.05 M_{\text{Sun}}$ )

# Disk mass distribution



# Uncertainties in disk mass

- Gas-to-dust ratio is **assumed** to be interstellar (100); in reality: ratio in disks may be  $< 100 \rightarrow$  if we assume 100, we **overestimate** disk mass!



(Predehl & Schmitt 1995)

$$\left[ \frac{\kappa_\nu}{\text{cm}^2 \text{ g}^{-1}} \right] = 0.1 \left[ \frac{\nu}{1000 \text{ GHz}} \right]^\beta$$

- H is **very difficult** to detect in disks, other molecules are used, e.g. CO (requires assumption on H<sub>2</sub>/CO ratio)

# Uncertainties in disk mass

- Hidden mass in large grains → **underestimation**
- Rule of thumb: observations at  $\lambda$  are sensitive to grains with sizes of  $< 3\lambda$  (Mie theory)

$$\left[ \frac{\kappa_\nu}{\text{cm}^2 \text{ g}^{-1}} \right] = 0.1 \left[ \frac{\nu}{1000 \text{ GHz}} \right]^\beta$$

- Optical properties of dust grains: Draine & Lee (1983)
- Dust opacities for protostellar cores: Ossenkopf & Henning (1994)

# Uncertainties in disk mass

- Indications for **severe underestimation**:
  - measured disk masses are lower than what is expected by integrating the accretion rate over the protostellar age
  - not enough massive disks to match the statistics on the incidence of exoplanets

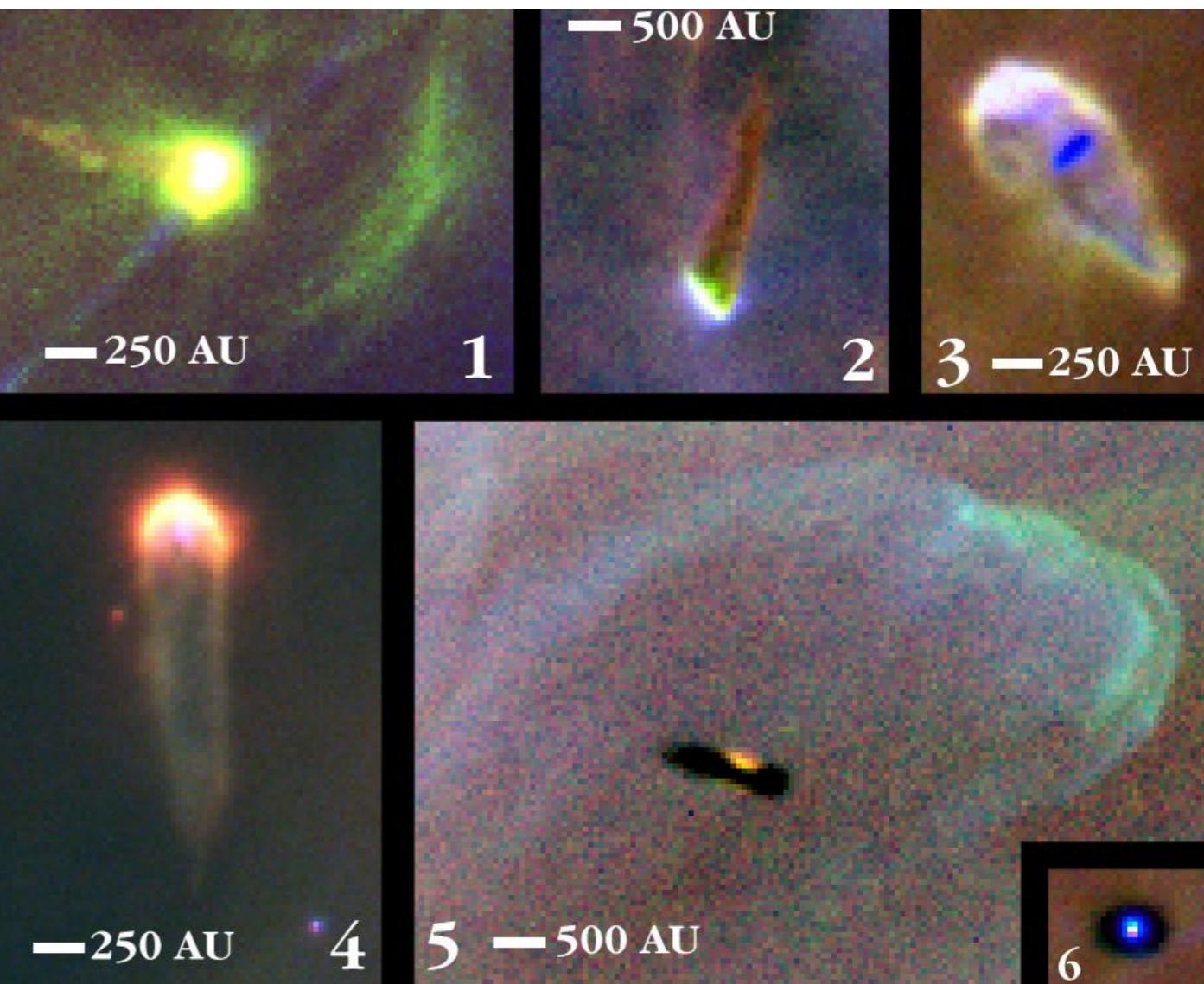
# Disk radius: direct measurement



NASA, ESA and L. Ricci (ESO)

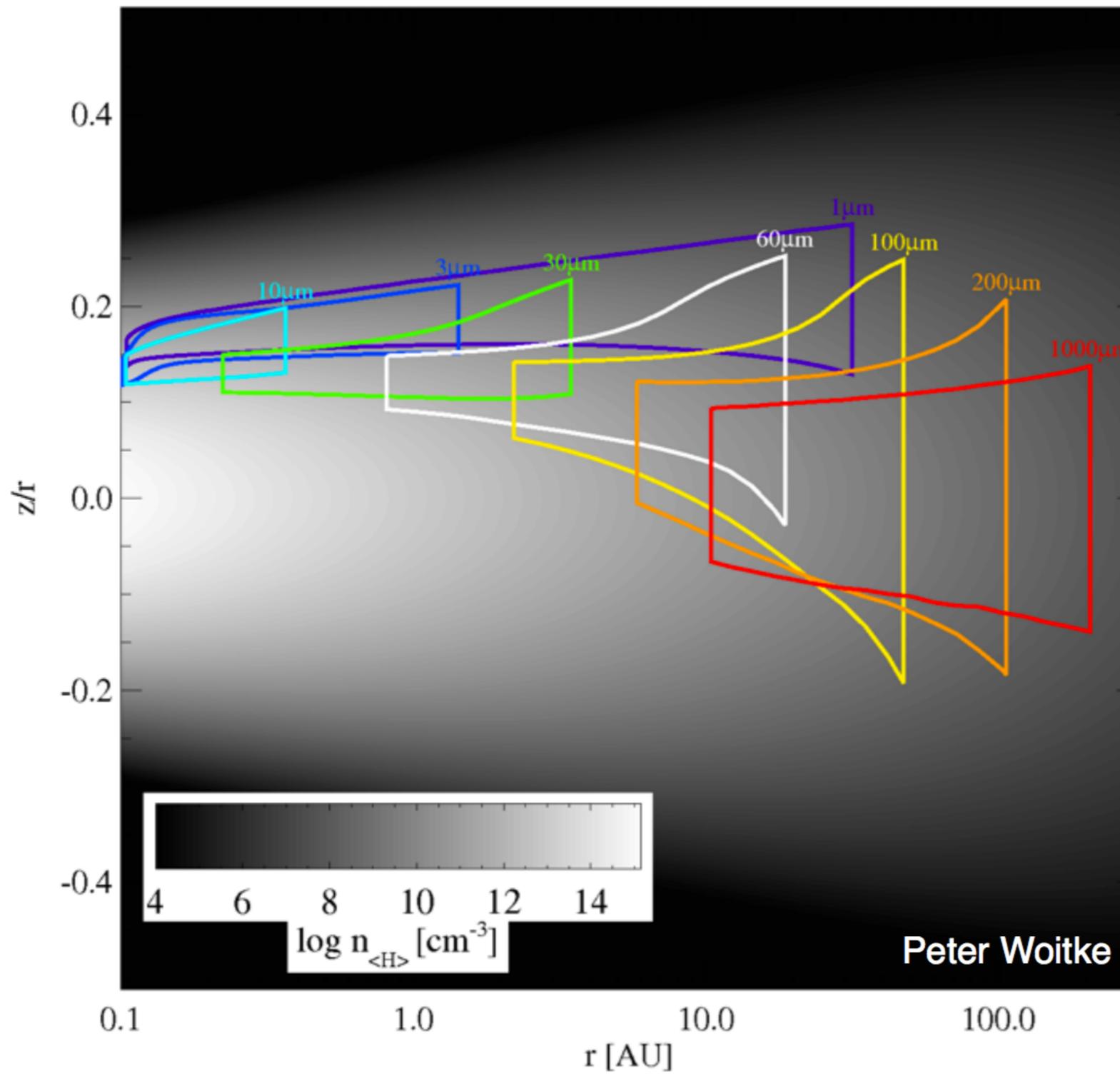
# Disk radii in Orion

- **Disk silhouettes** in Orion: disks are directly visible against a bright background
- Radii: between 50 and 194 au
- Median radius: 75 au
- Is this typical?



NASA, C.R. O'Dell and S.K. Wong (Rice University)

# Disk radius: detect resolved disk emission



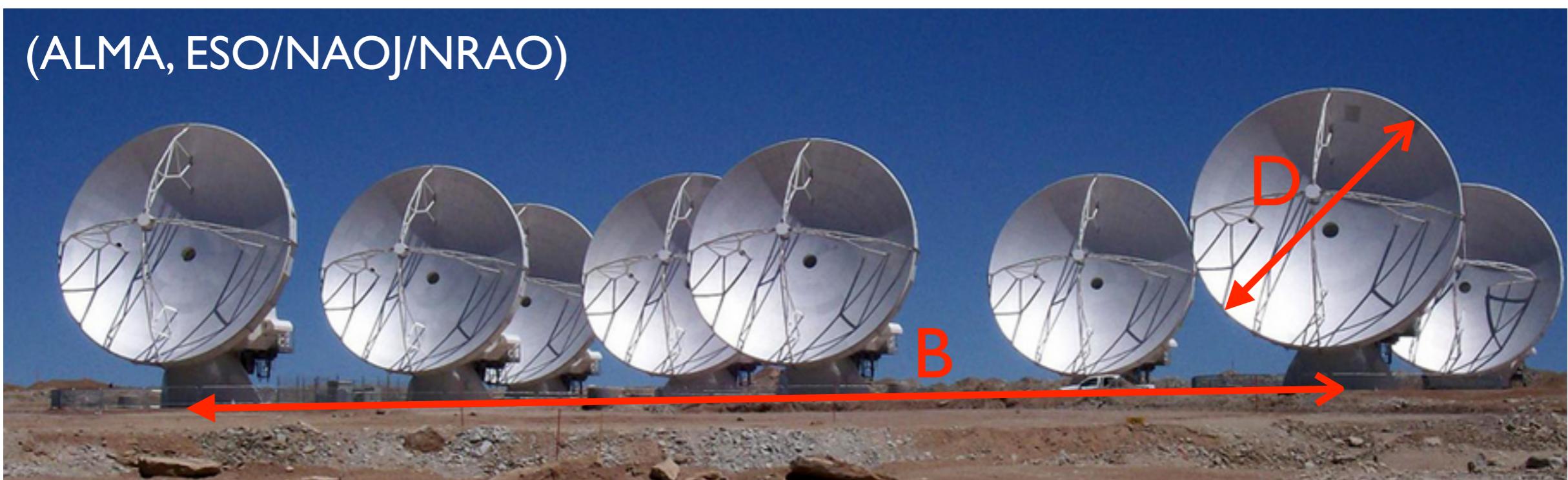
Difficult to  
measure, because  
outer parts are  
cold and faint

# Solution: interferometry

- **Angular resolution** of an antenna:  $\theta = k \lambda / D$   
 $\lambda$ : observing wavelength  
 $D$ : diameter of the antenna  
 $k = 70$  (if  $\theta$  is measured in degrees)  
 $k = 1.22$  (if  $\theta$  is measured in radians)
- If we want a resolution of 1" or better at 1 mm, we need a 800 m diameter antenna or larger!
- Not possible with a single dish, but possible with **interferometry**

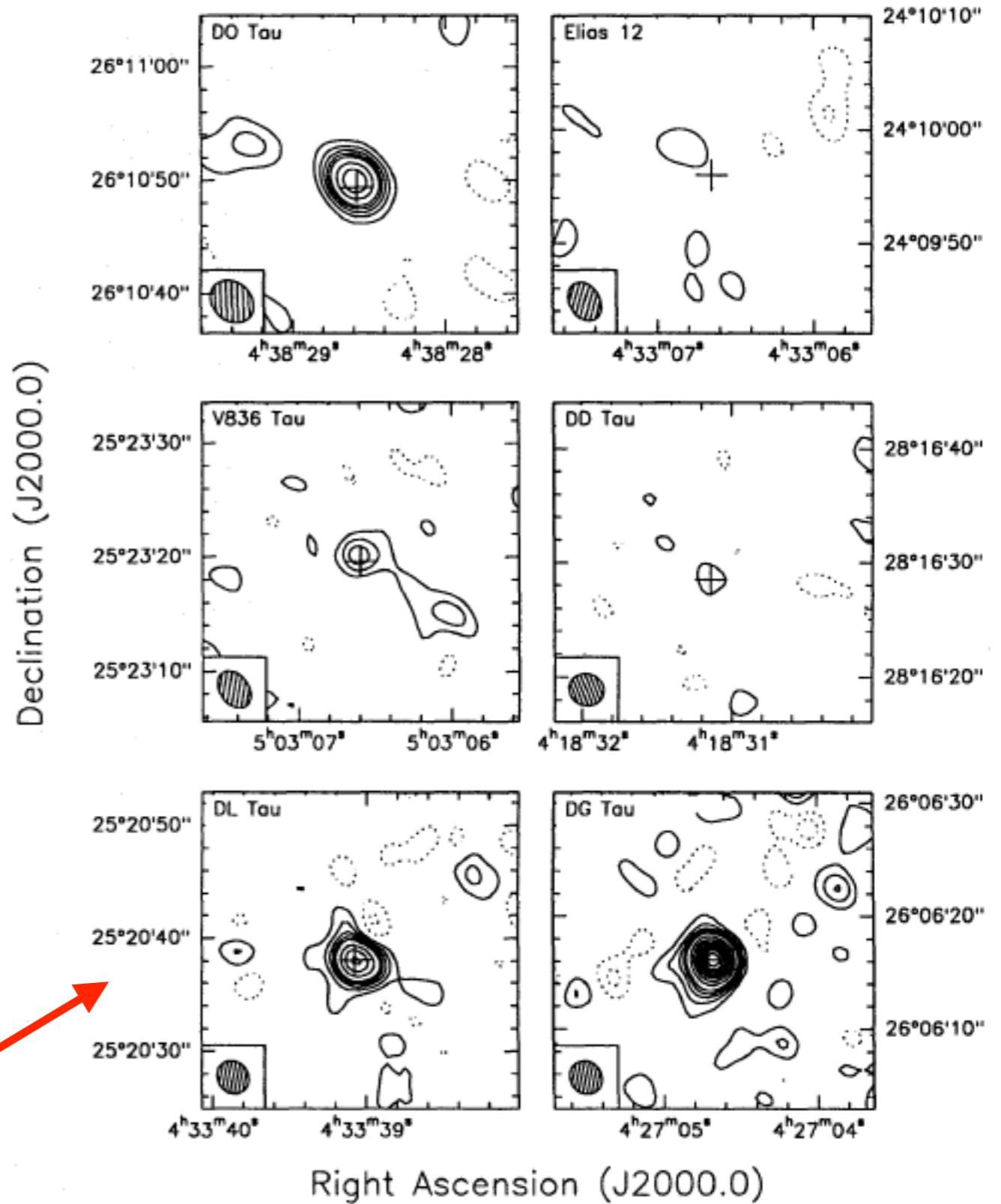
# Interferometry

- Interferometer: combines the signal from several telescopes/antennas
- Array works like a **giant telescope**
- Resolution is determined by the distance between the antennas (baseline) and not the diameter of the antennas



# Interferometric surveys

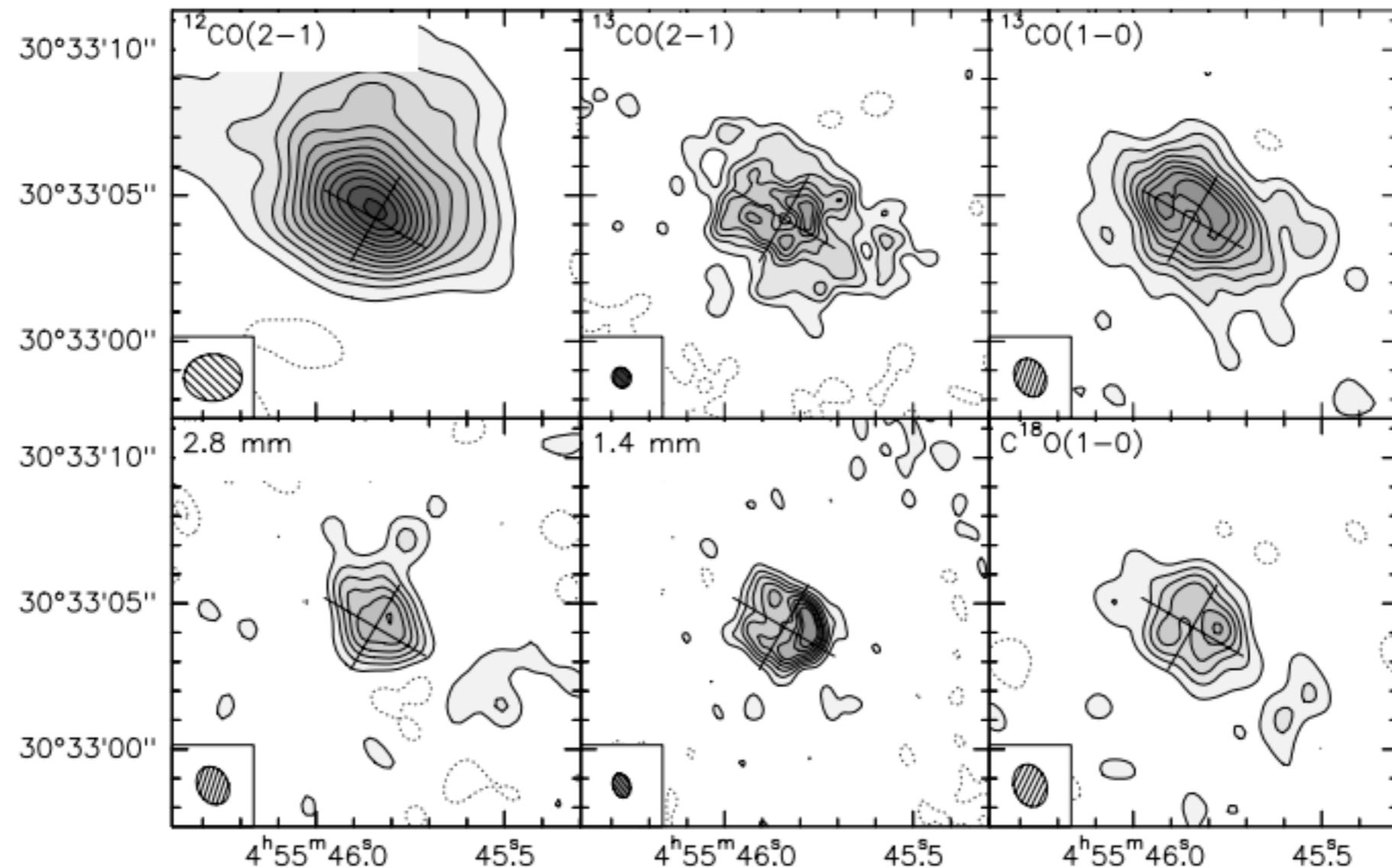
- First large interferometric survey:  
Dutrey et al. (1996)
- Typical disk sizes in Taurus ( $d=150$  pc):  
 $1 - 2''$   
( $r = 75 - 150$  au)



2.7 mm dust continuum

# Dust size vs. gas size

Problem: **dust sizes  $\neq$  gas sizes** (size from CO lines is larger than from dust continuum)

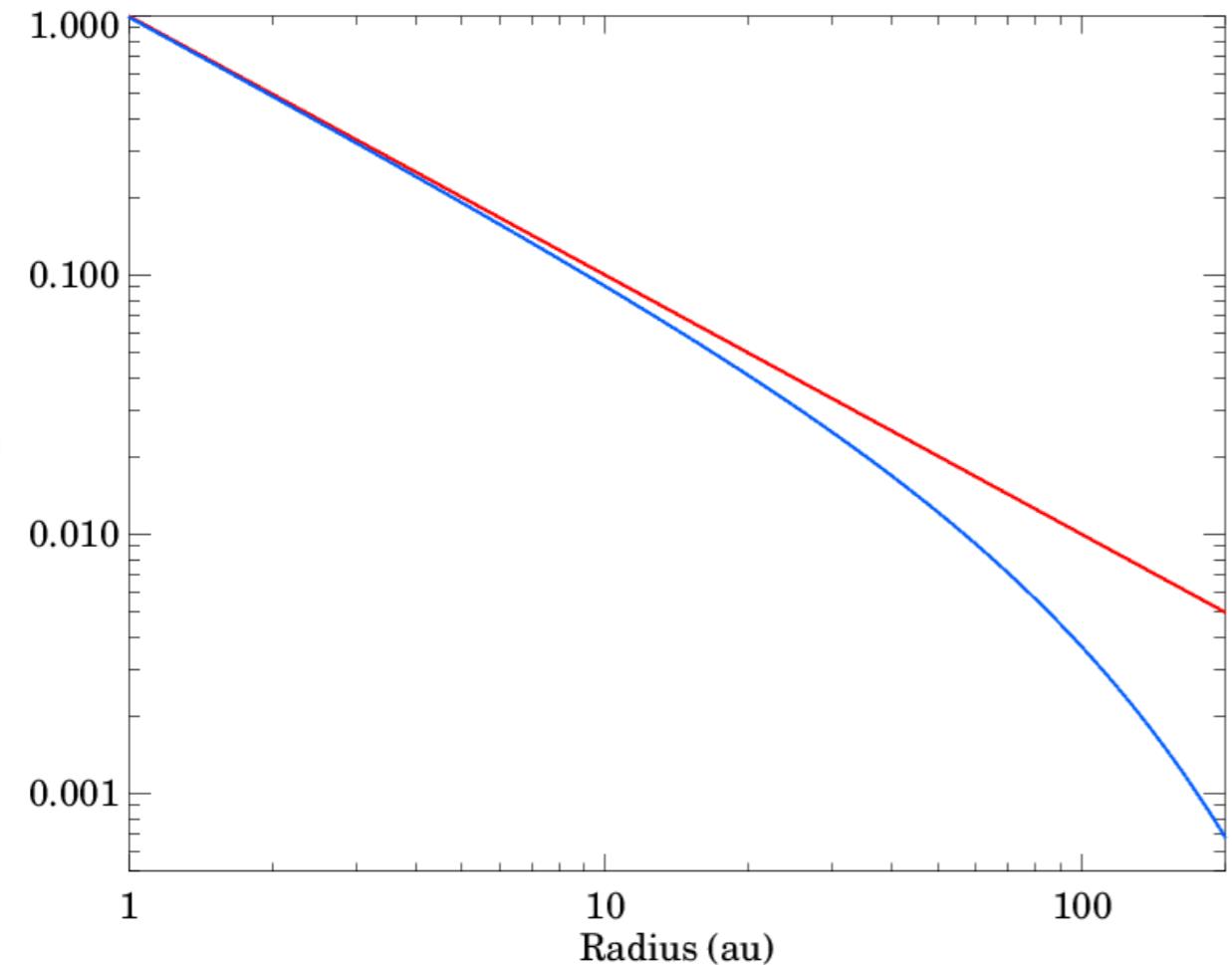


AB Aur (Pietu et al. 2005)

# Dust size vs. gas size

Possible solutions:

- Change in the gas-to-dust ratio or dust opacity at a certain radius
- Exponentially tapered density profile:



$$\Sigma(R) = (2-\gamma) \frac{M_d}{2\pi R_c^2} \left( \frac{R}{R_c} \right)^{-\gamma} \exp \left[ - \left( \frac{R}{R_c} \right)^{2-\gamma} \right]$$

# Dust size vs. gas size

Possible solutions:

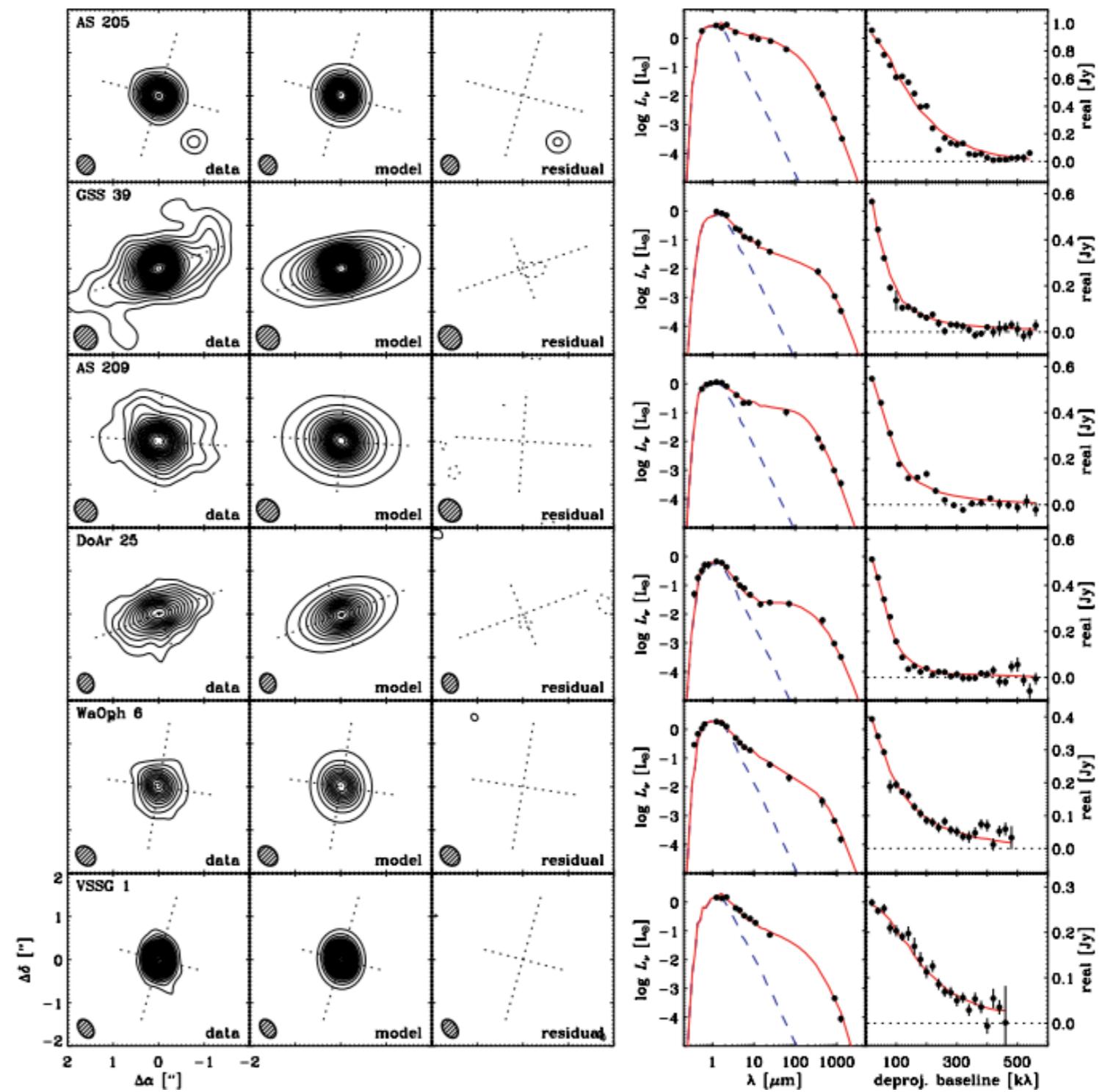
- Change in the gas-to-dust ratio or dust opacity at a certain radius
- Exponentially tapered density profile:

$$\Sigma(R) = (2-\gamma) \frac{M_d}{2\pi R_c^2} \left(\frac{R}{R_c}\right)^{-\gamma} \exp\left[-\left(\frac{R}{R_c}\right)^{2-\gamma}\right]$$

- $R_c$ : characteristic radius where the density profile begins to steepen significantly from a power law, typically  $R_c = 30 - 200$  au
- **Apparent size discrepancy!** mm continuum is optically thin, CO line emission is optically thick  
→ can be detected further out

# Parameter correlations

- Andrews et al. (2009, 2010): 16 disks in Ophiuchus
- $R_c = 14 - 198$  au
- Between disk size and disk mass:  
$$M_d \propto R_c^{1.6 \pm 0.3}$$
- Between disk size and stellar properties: no correlation



# Disk structure – $\Sigma$

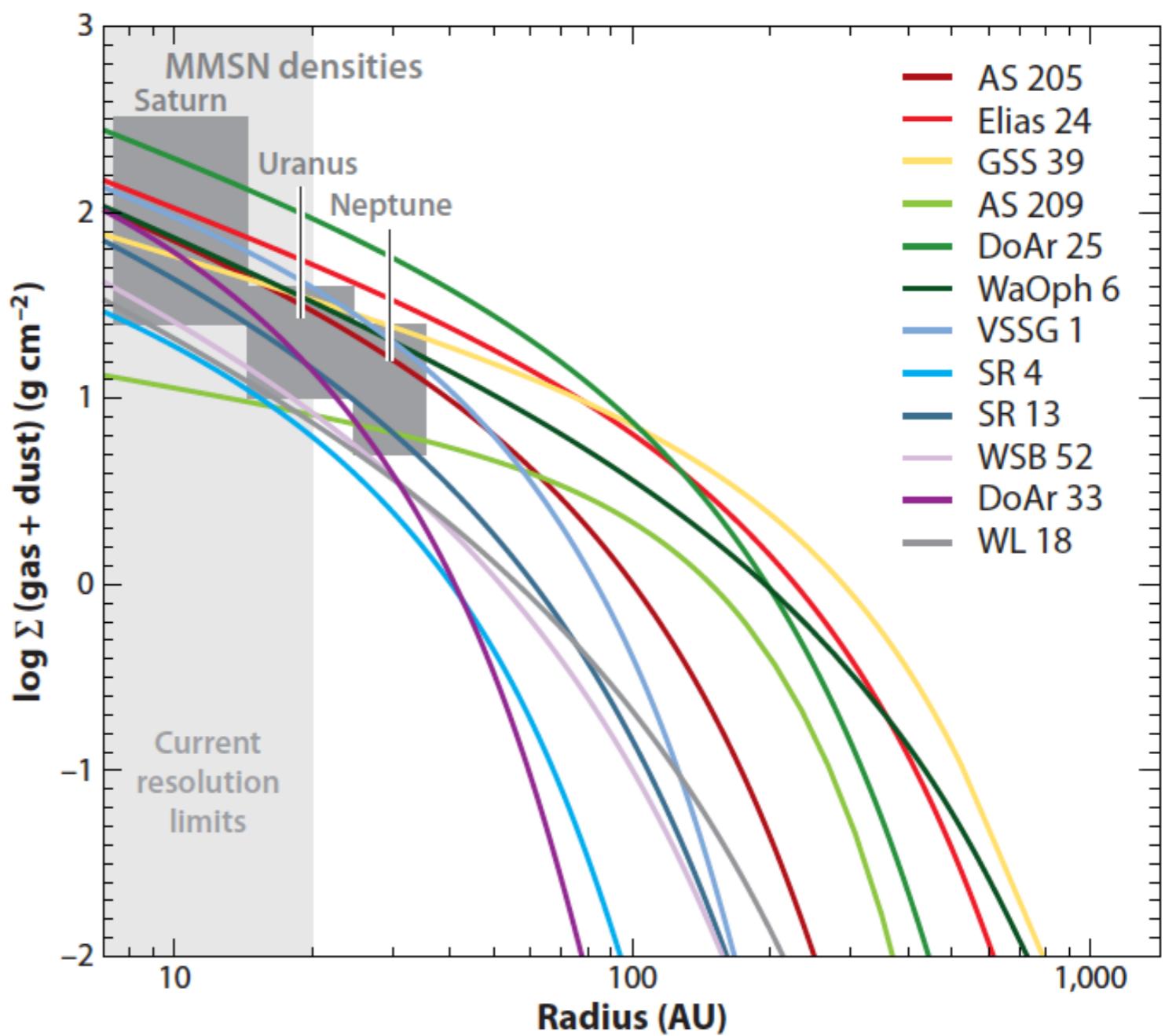
- Resolved mm image of the disk → total mass + radial mass distribution
- Usual parametrization: power law:  $\Sigma \sim R^{-p}$
- $p = 0 \dots 1$
- Exponentially tapered edge

$$\Sigma(R) = (2-\gamma) \frac{M_d}{2\pi R_c^2} \left(\frac{R}{R_c}\right)^{-\gamma} \exp\left[-\left(\frac{R}{R_c}\right)^{2-\gamma}\right]$$

- Approximates  $\Sigma \sim R^{-\gamma}$  for  $R \ll R_c$
- $\gamma = -0.8 \dots 0.8$  (mean 0.1)
- $\Sigma$  distribution is quite flat

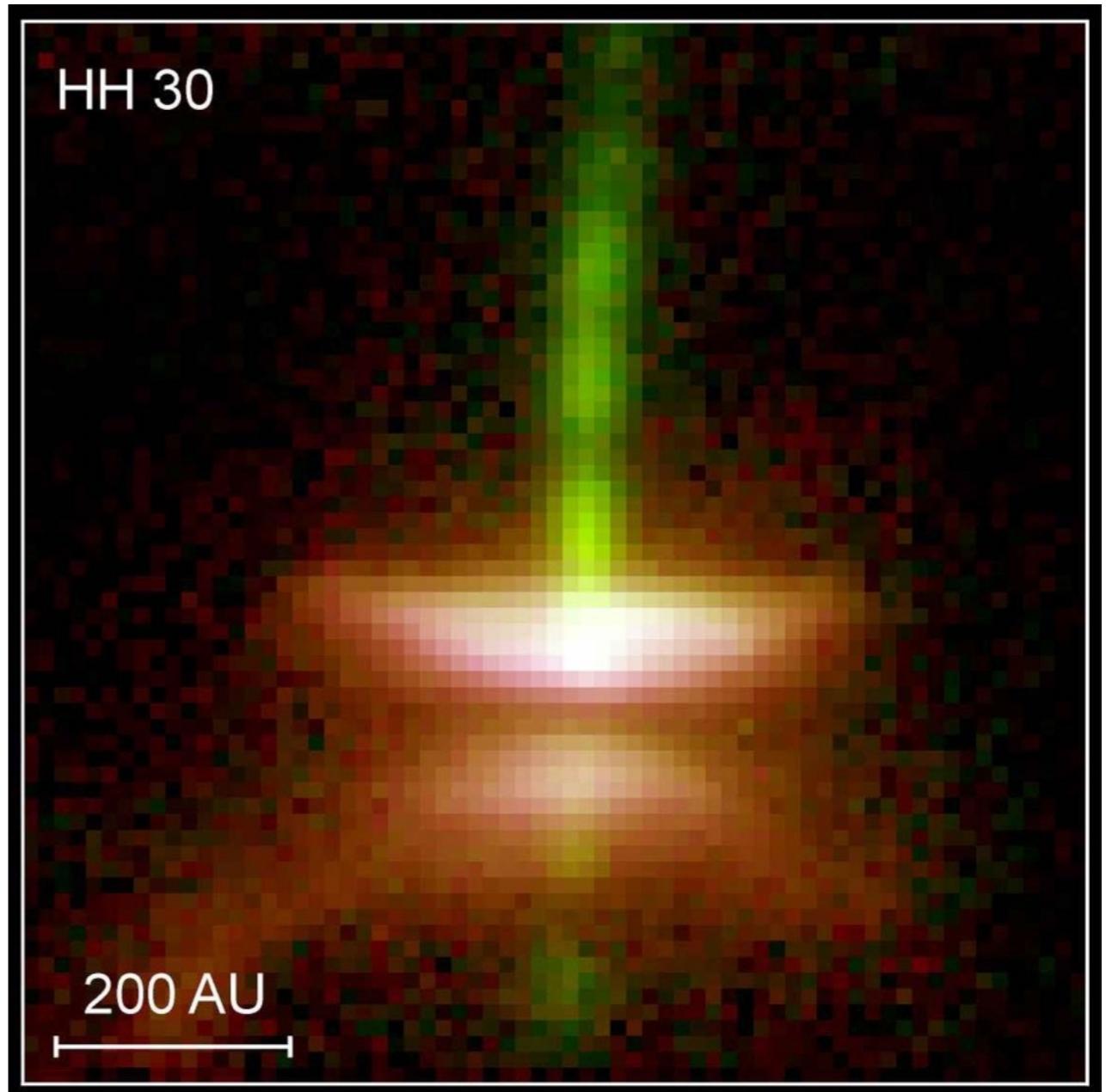
# $\Sigma$ distribution

- Let's compare directly the absolute value of  $\Sigma$  at different radial distances
- $\Sigma = 10 \dots 100 \text{ g cm}^{-2}$  at 20 au
- Good match
- Toomre parameter:  
$$Q(R) = c\Omega/\pi G\Sigma$$
- Class II are typically gravitationally stable



# Disk structure - H

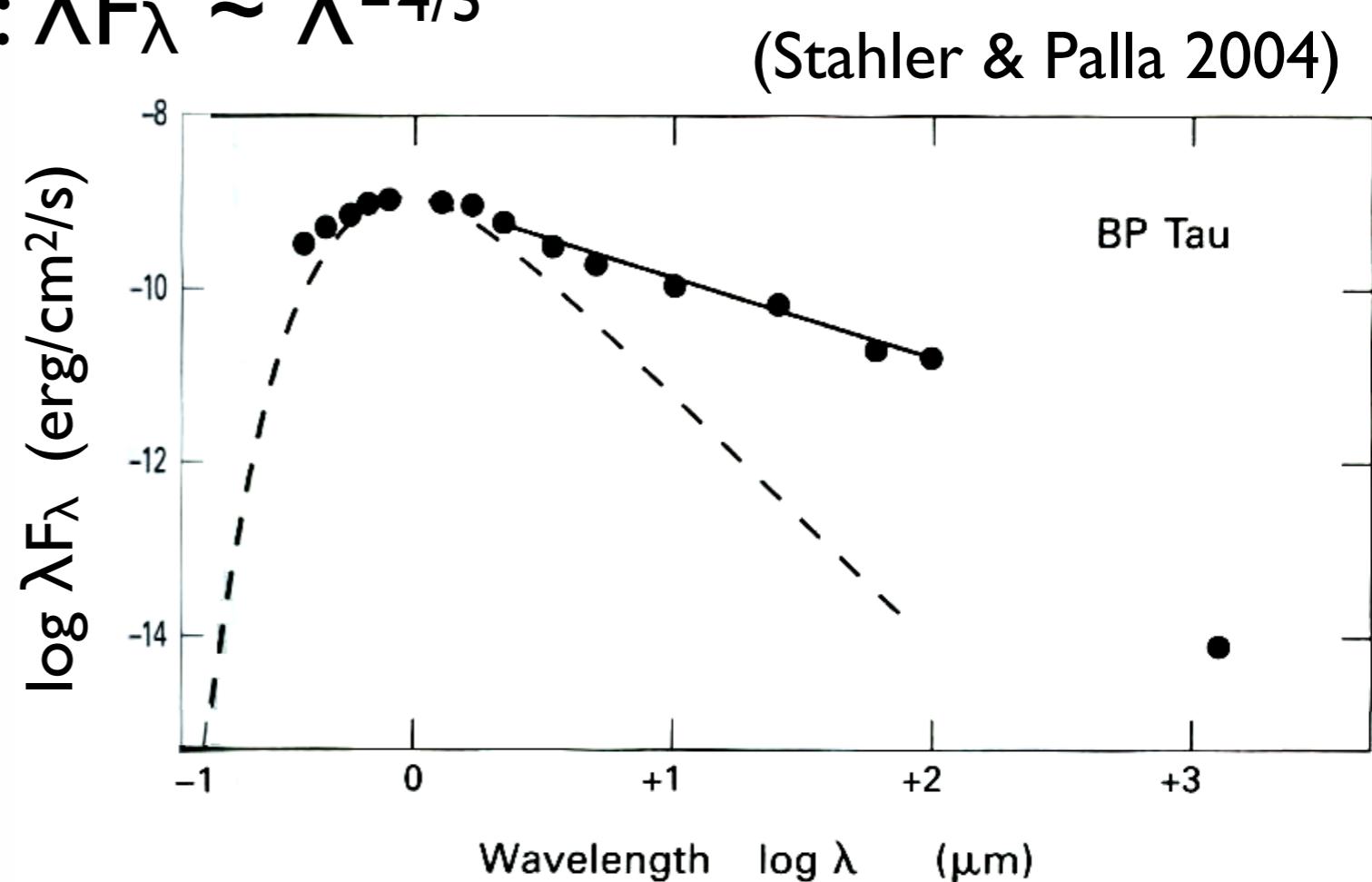
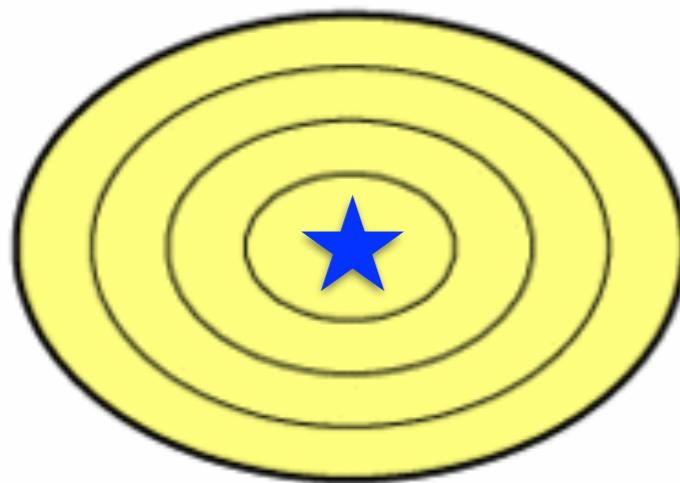
H – vertical scale height



(Burrows et al. 1996)

# Disk structure - H

- Disks were first assumed to be **flat**
- If  $T(r) \sim r^{-q} \rightarrow \lambda F_\lambda \sim \lambda^{(2-4q)/q}$
- For both a passive, flat irradiated disk, or an active accreting disk, theoretically  $q = 3/4$
- Resulting SED shape:  $\lambda F_\lambda \sim \lambda^{-4/3}$



# Disk structure - H

- Not all disks look like  $\lambda F_\lambda \sim \lambda^{-4/3}$
- First idea of a **flared disk**: Kenyon & Hartmann (1987)

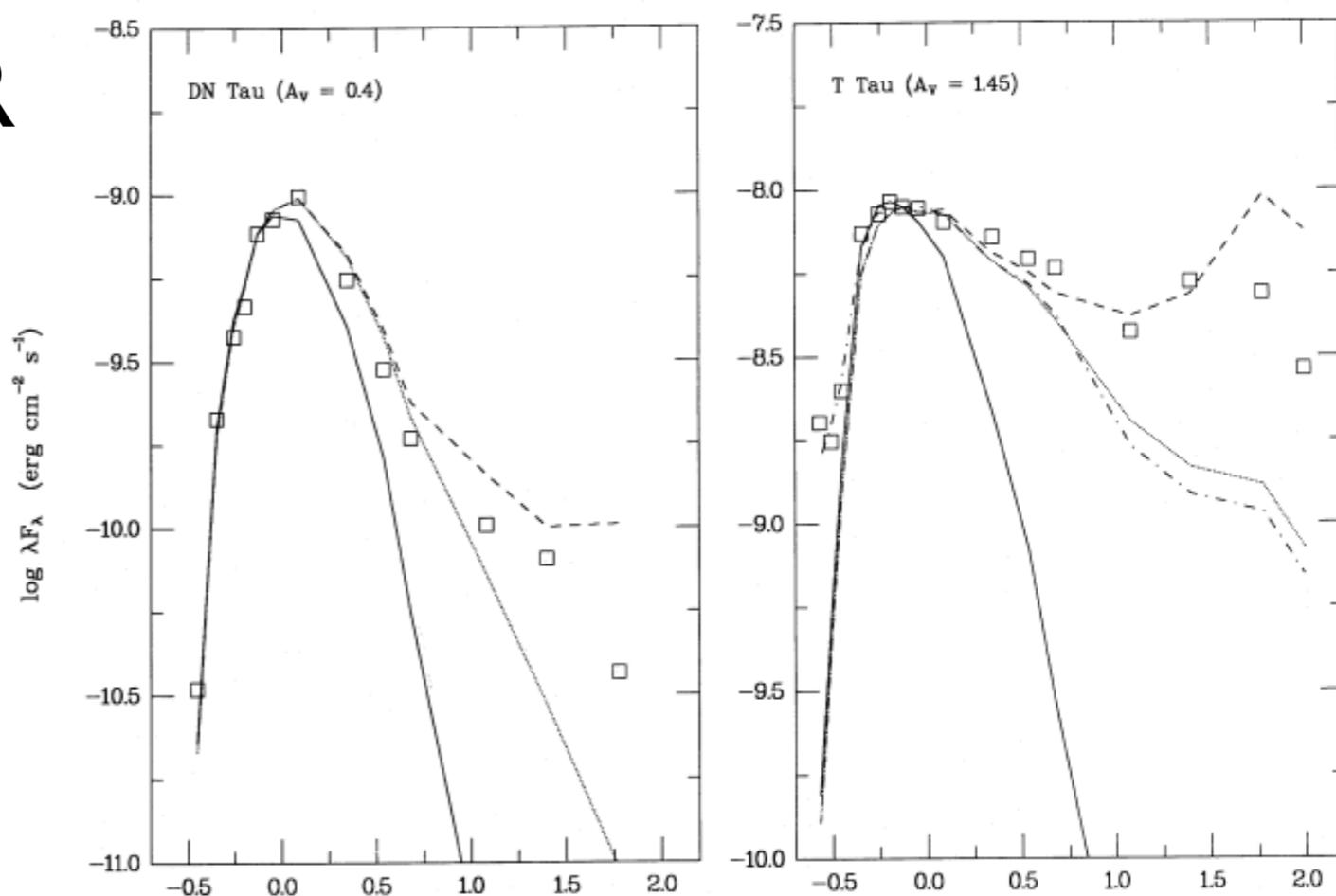
- $H$  must increase with  $R$

- Density:

$$\rho(R, Z) = \frac{\Sigma(R)}{\sqrt{2\pi}H} \exp\left(-\frac{Z^2}{2H^2}\right)$$

- Scale height is power-law:

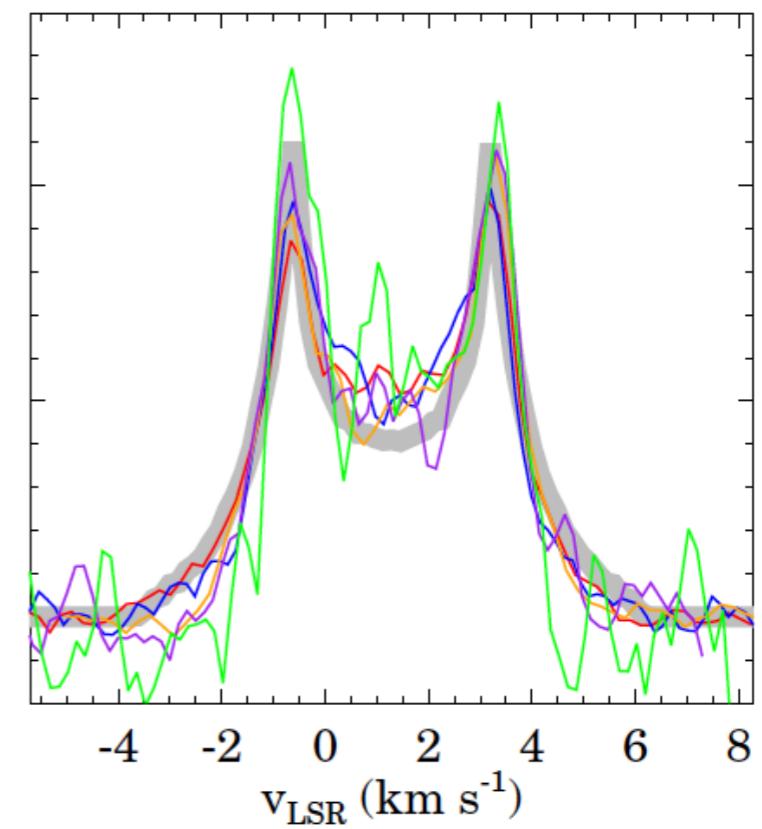
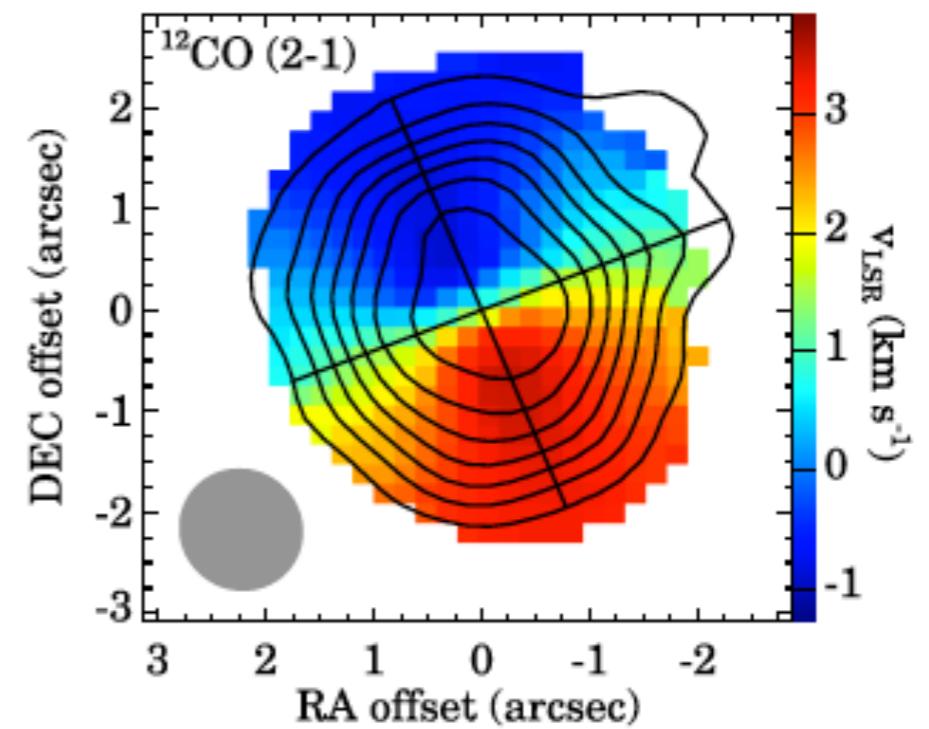
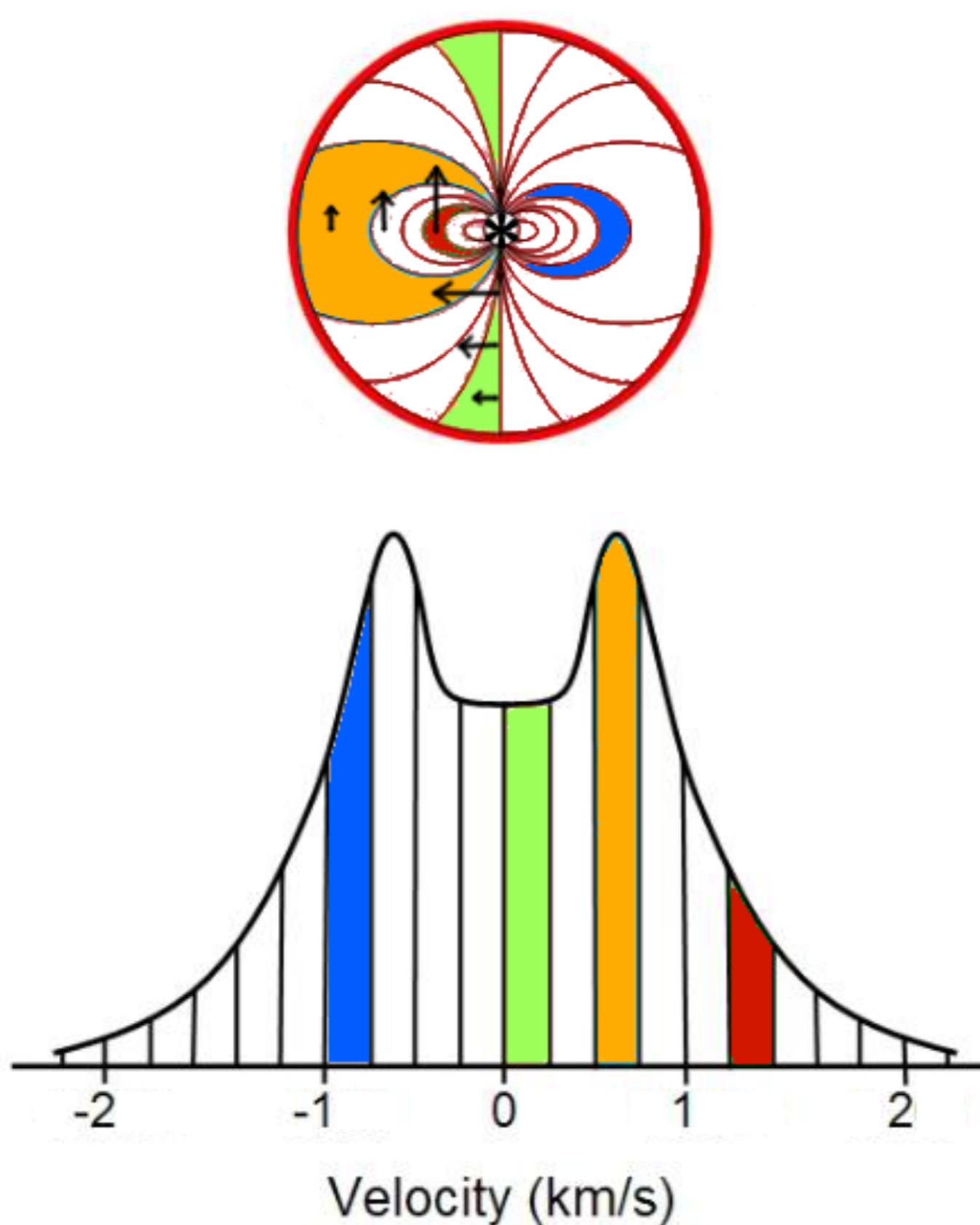
$$H \sim R^h, \text{ with } h = 1.3 \dots 1.5$$



# Disk structure – v

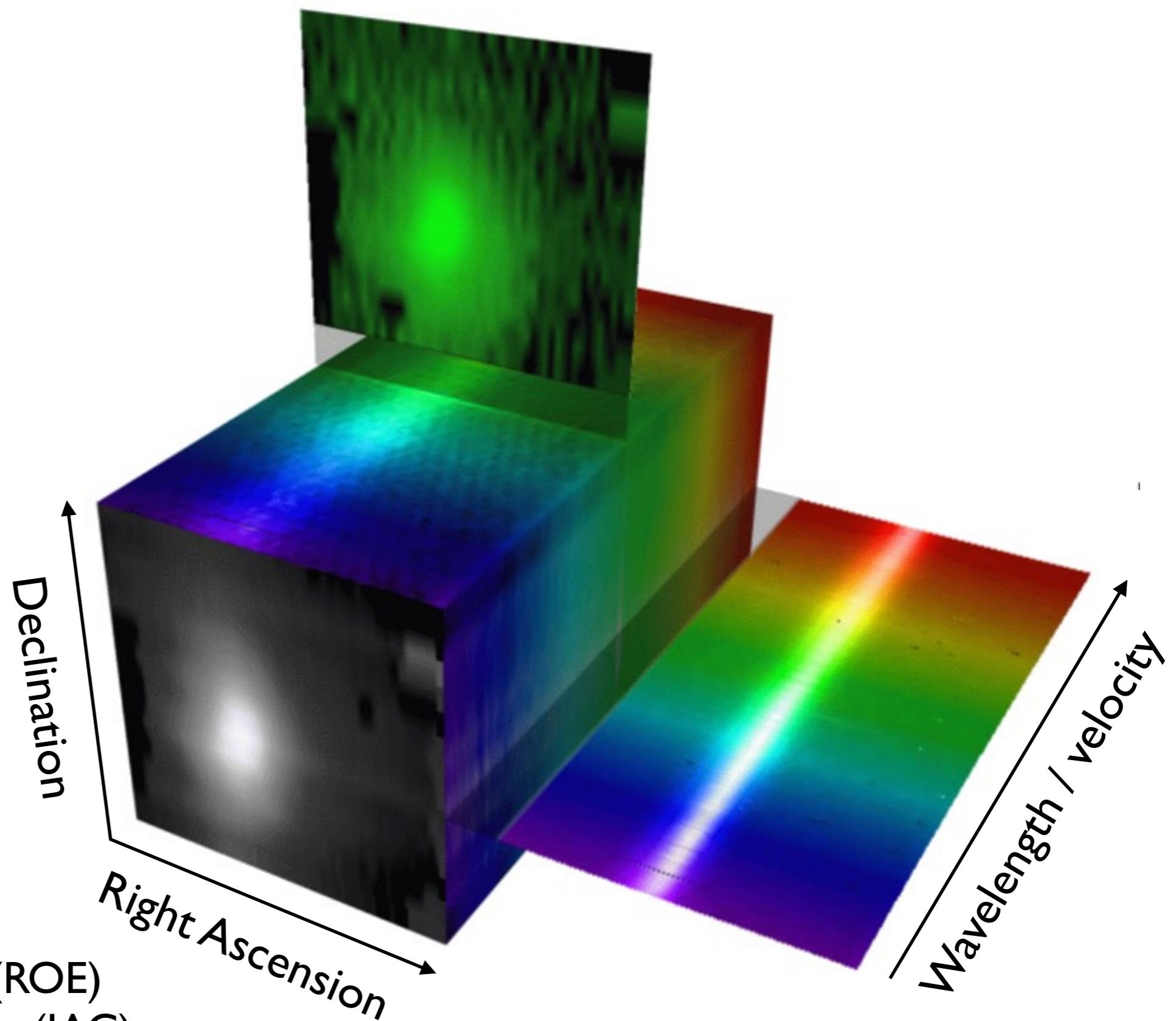
- In Class II:  $M_{\text{disk}} \ll M_{\text{star}}$
- Expectation: **Keplerian velocity field** ( $v \sim r^{-0.5}$ )
- Method: spectral line observations
- Challenge: target needs to be bright enough for the individual channel maps to have high S/N ratio; no background cloud / envelope contamination
- Done for a handful of disks
- Now almost routine task with ALMA

# Keplerian velocity profile



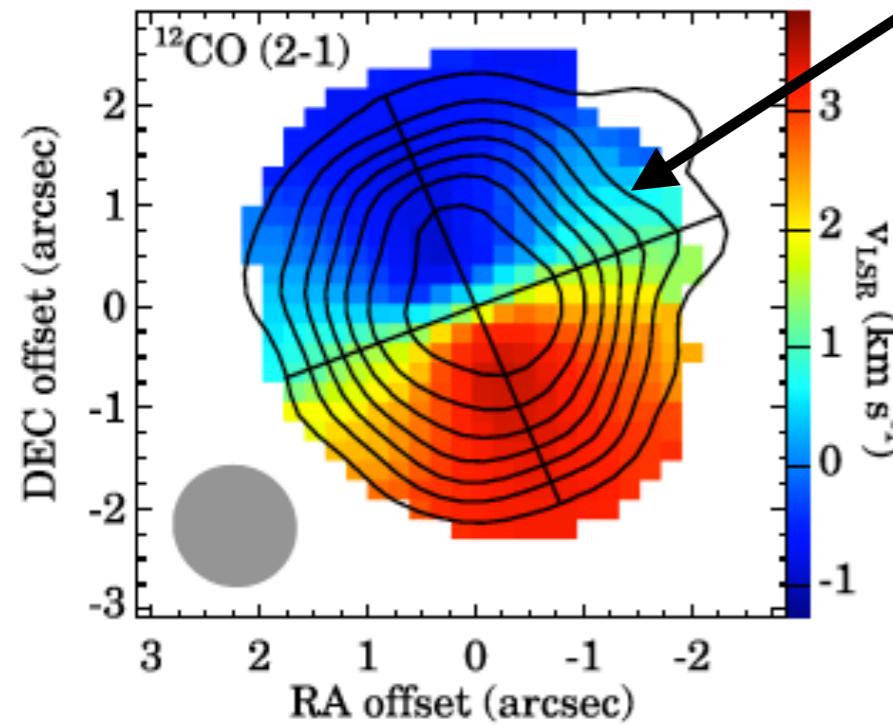
HD 21997 (Kóspál et al. 2013)

# Interferometric data cube



Credit: Stephen Todd (ROE)  
and Douglas Pierce-Price (JAC)

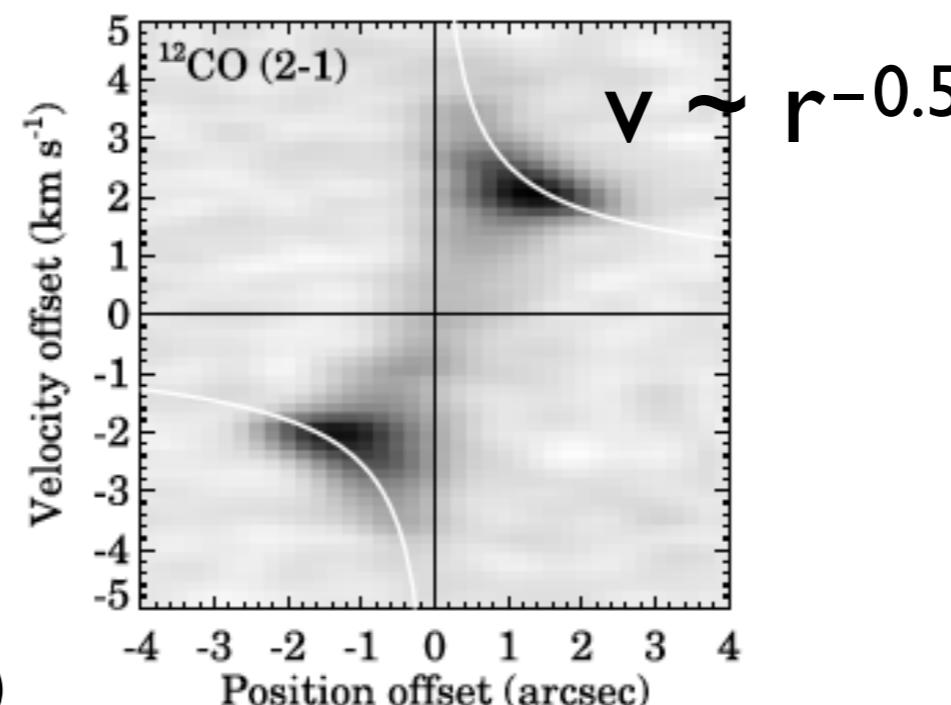
# Disk rotation



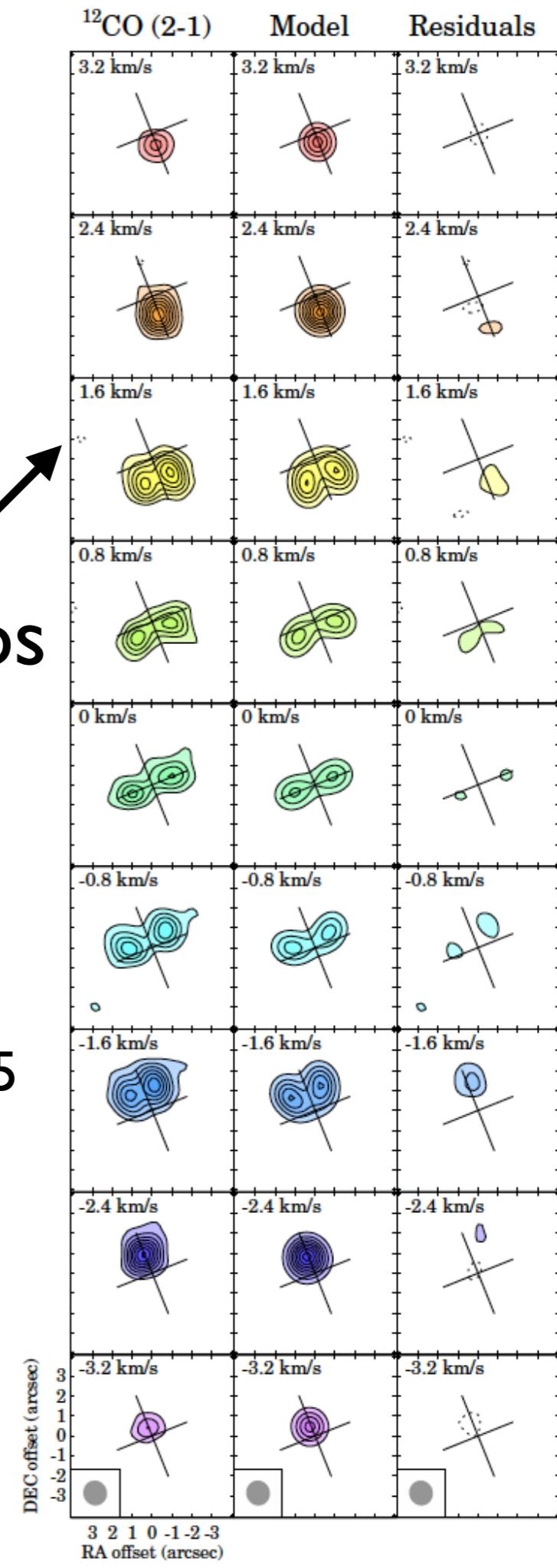
Velocity map  
(first moment map)

Channel maps

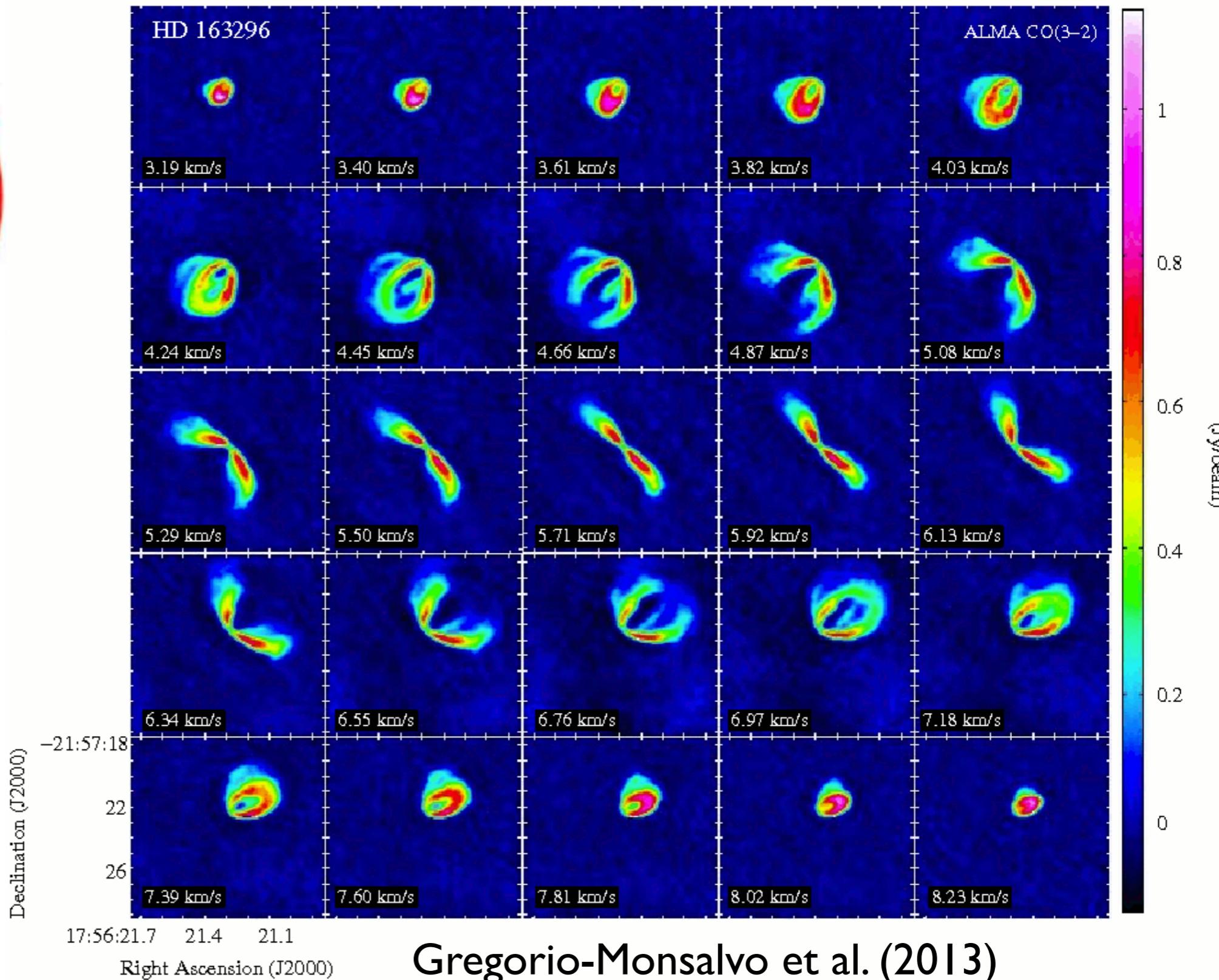
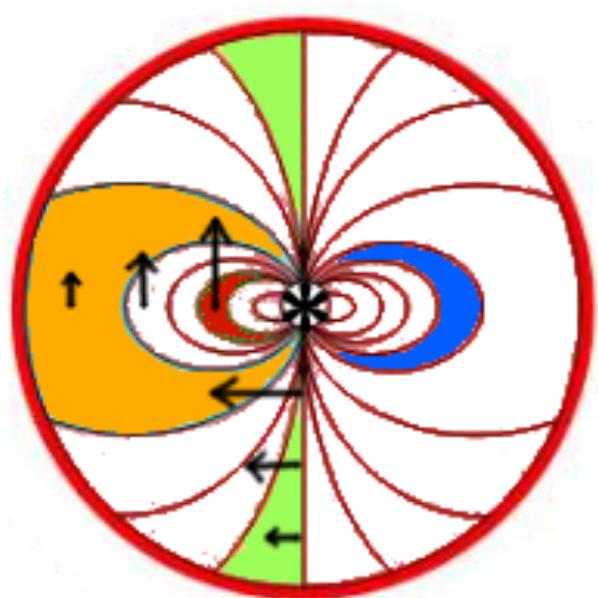
Position-velocity diagram



HD 21997, Kóspál et al. (2013)



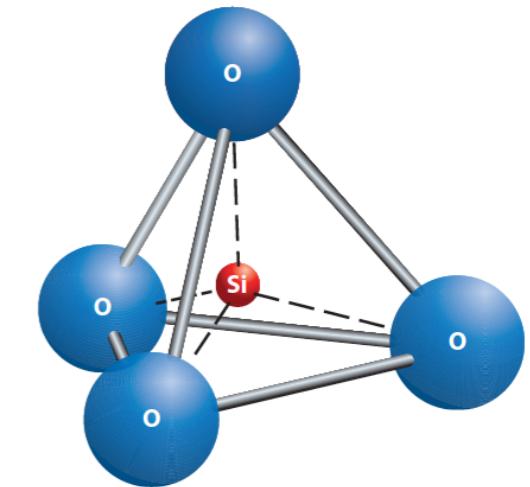
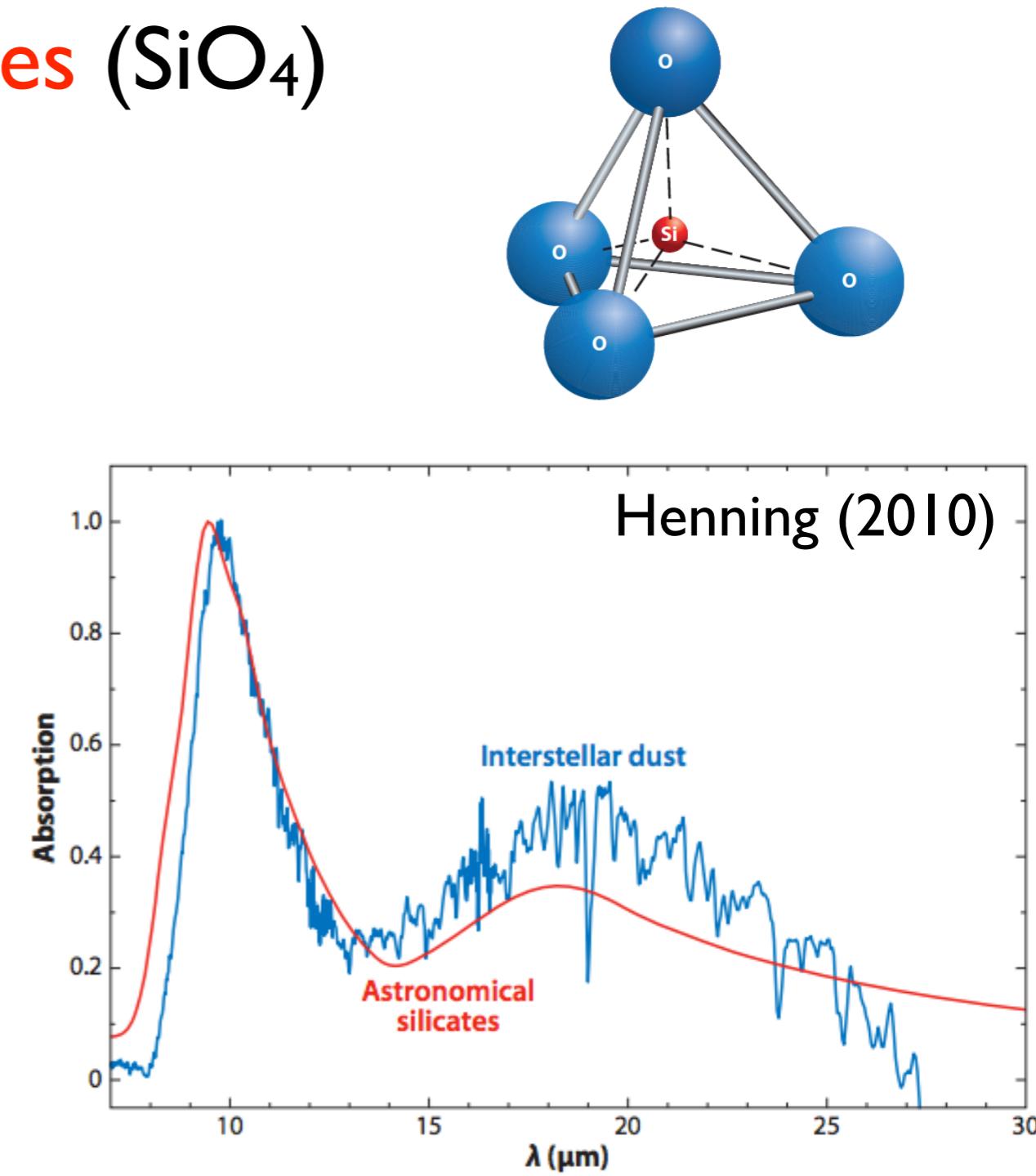
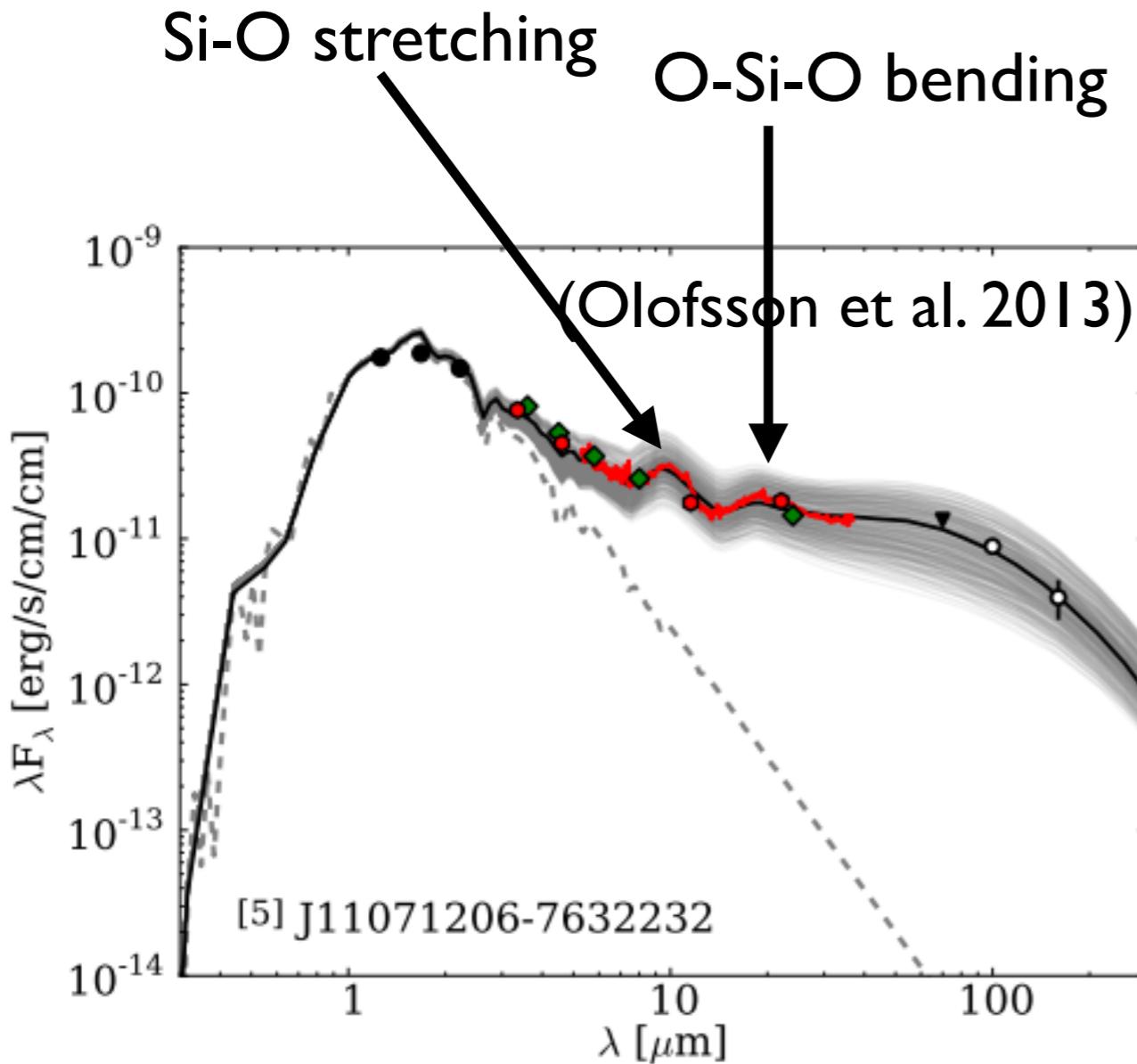
# Disk rotation



Gregorio-Monsalvo et al. (2013)

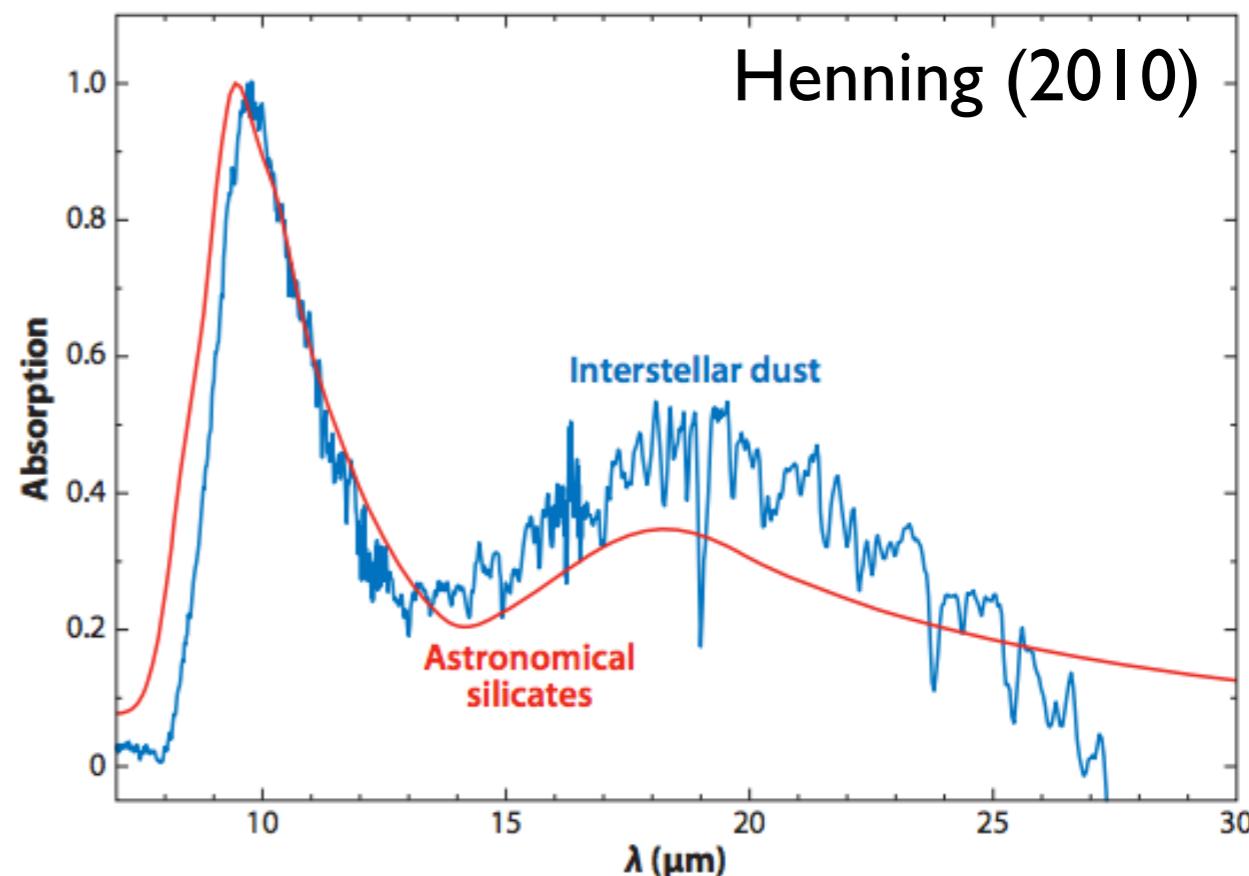
# Disk composition – dust

- Dust dominates the opacity + dust makes the planets
- Composition: mainly **silicates** ( $\text{SiO}_4$ )



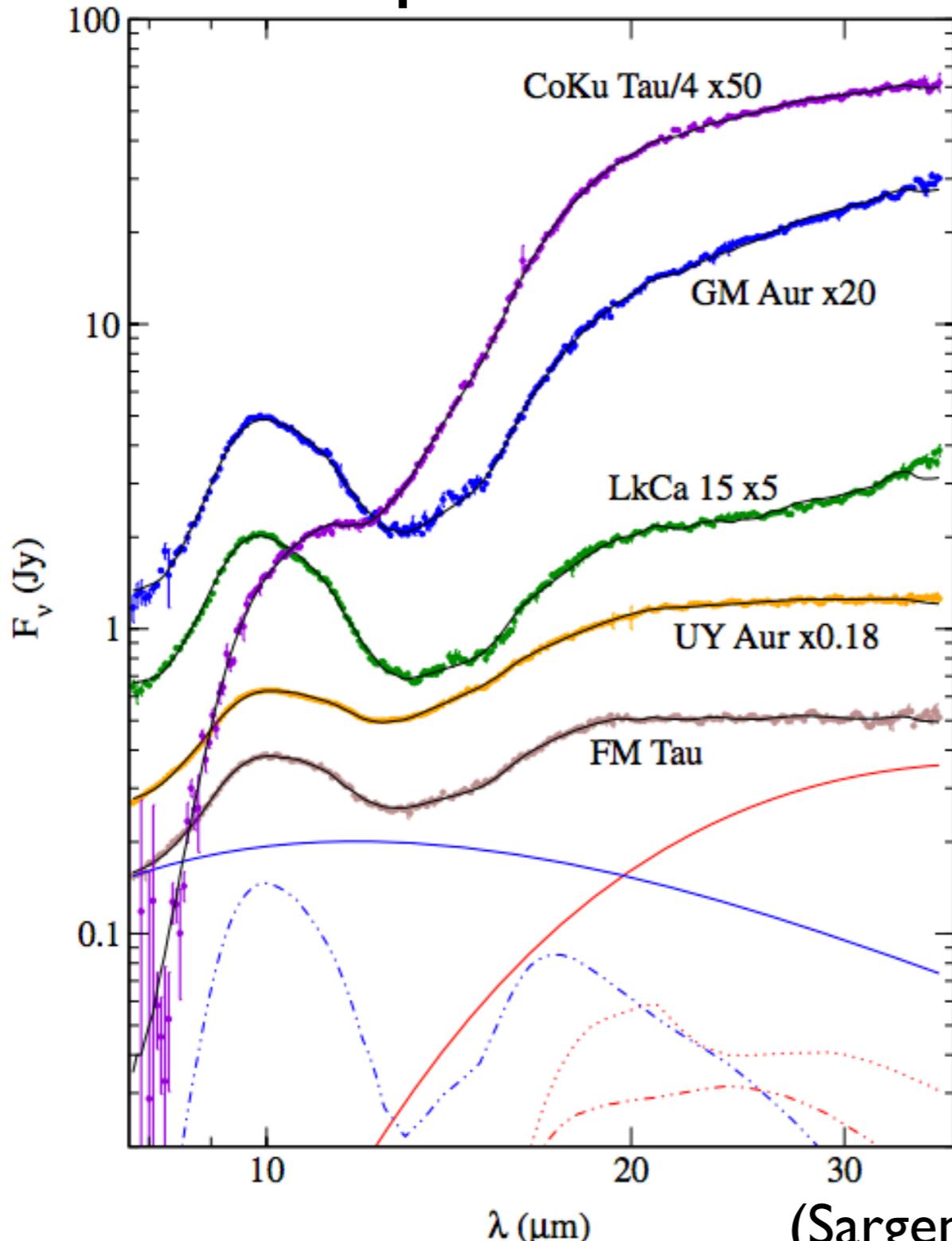
# Interstellar dust

- Dust in the ISM: small (submicron-size) and amorphous
- In young stellar objects, there is evidence for dust processing:
  - **Crystallization**  
(amorphous → crystalline)
  - **Grain growth**  
(submicron → mm)

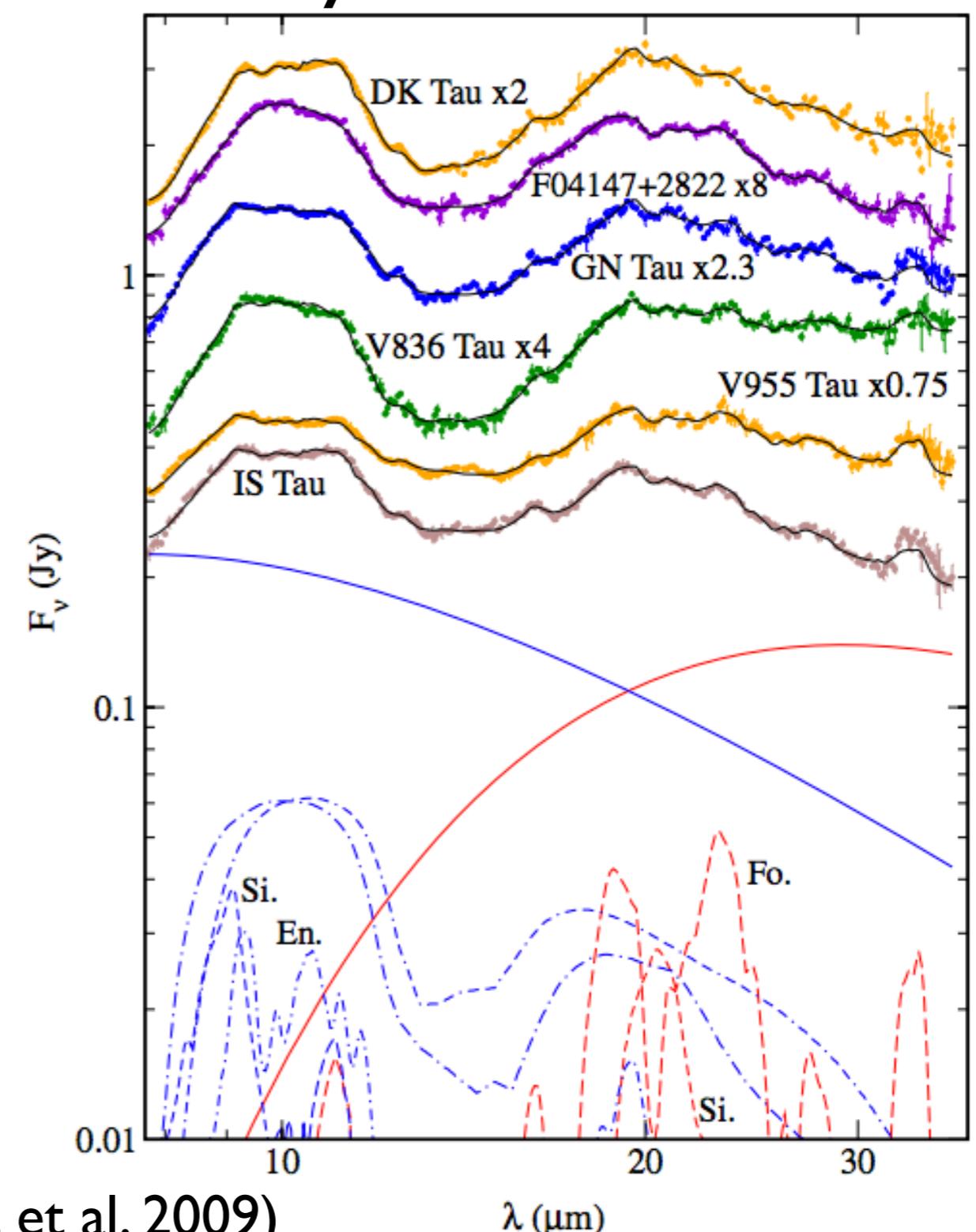


# Dust processing

## Amorphous silicates



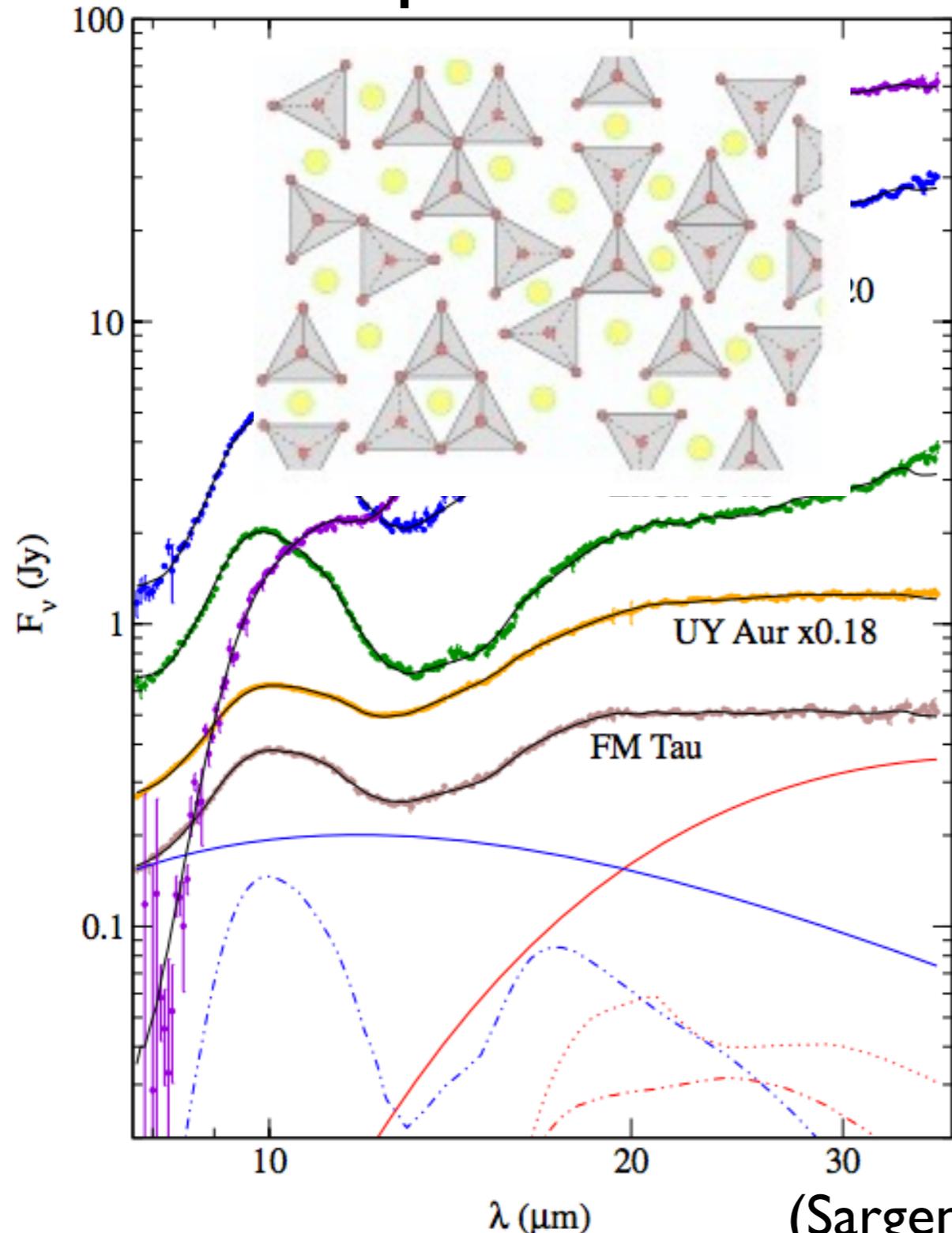
## Crystalline silicates



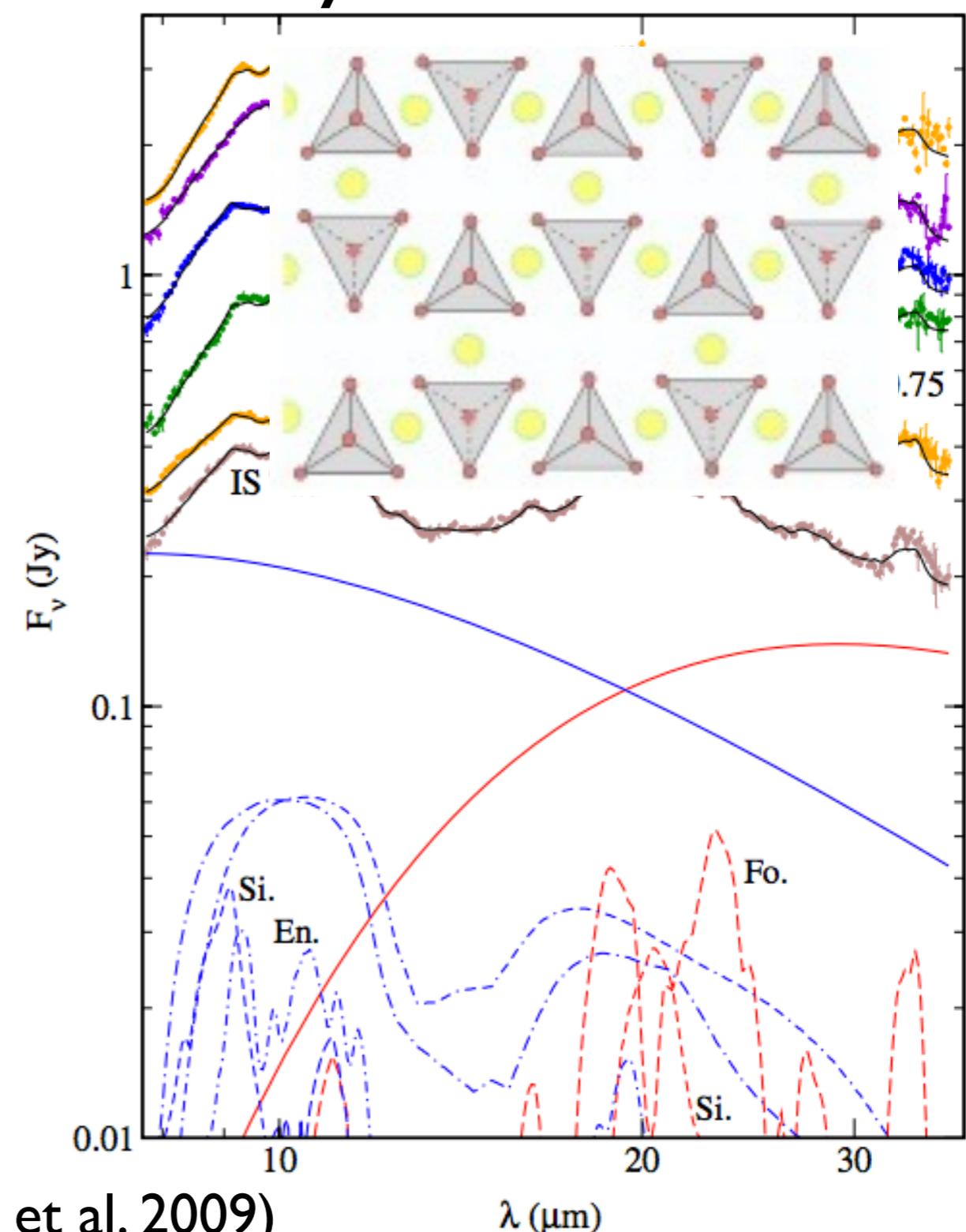
(Sargent et al. 2009)

# Dust processing

## Amorphous silicates

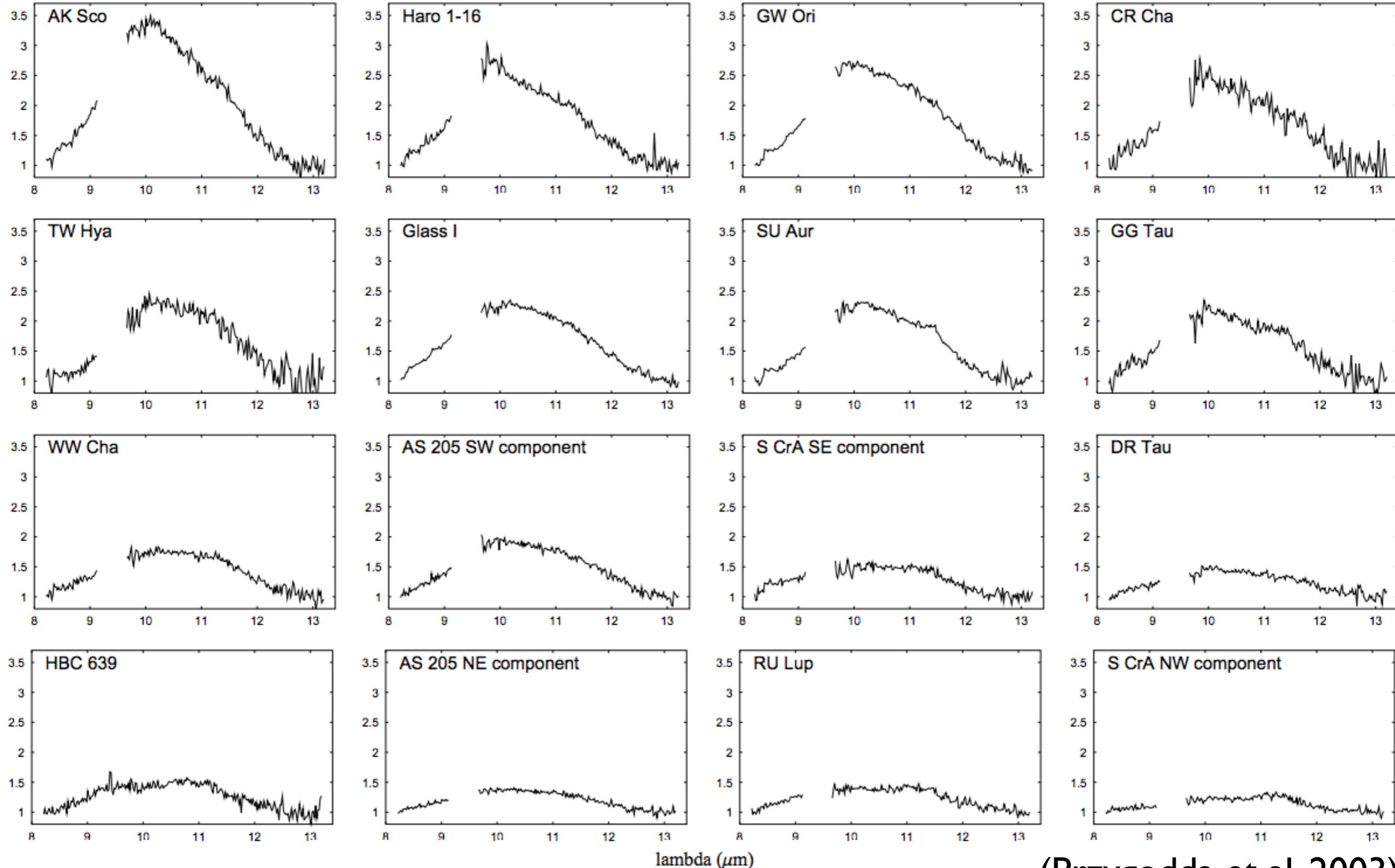


## Crystalline silicates



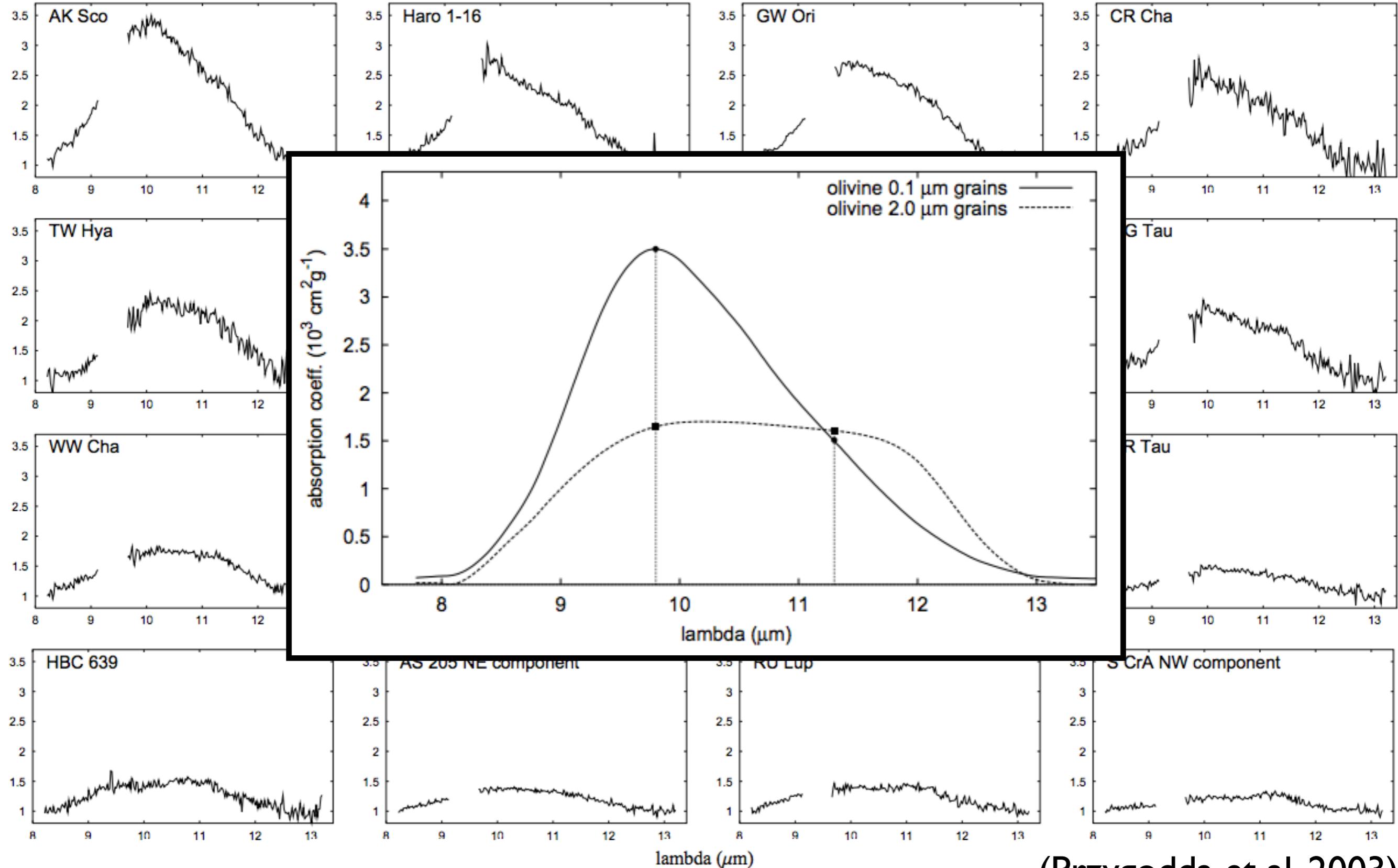
(Sargent et al. 2009)

# Grain growth



(Przygoda et al. 2003)

# Grain growth

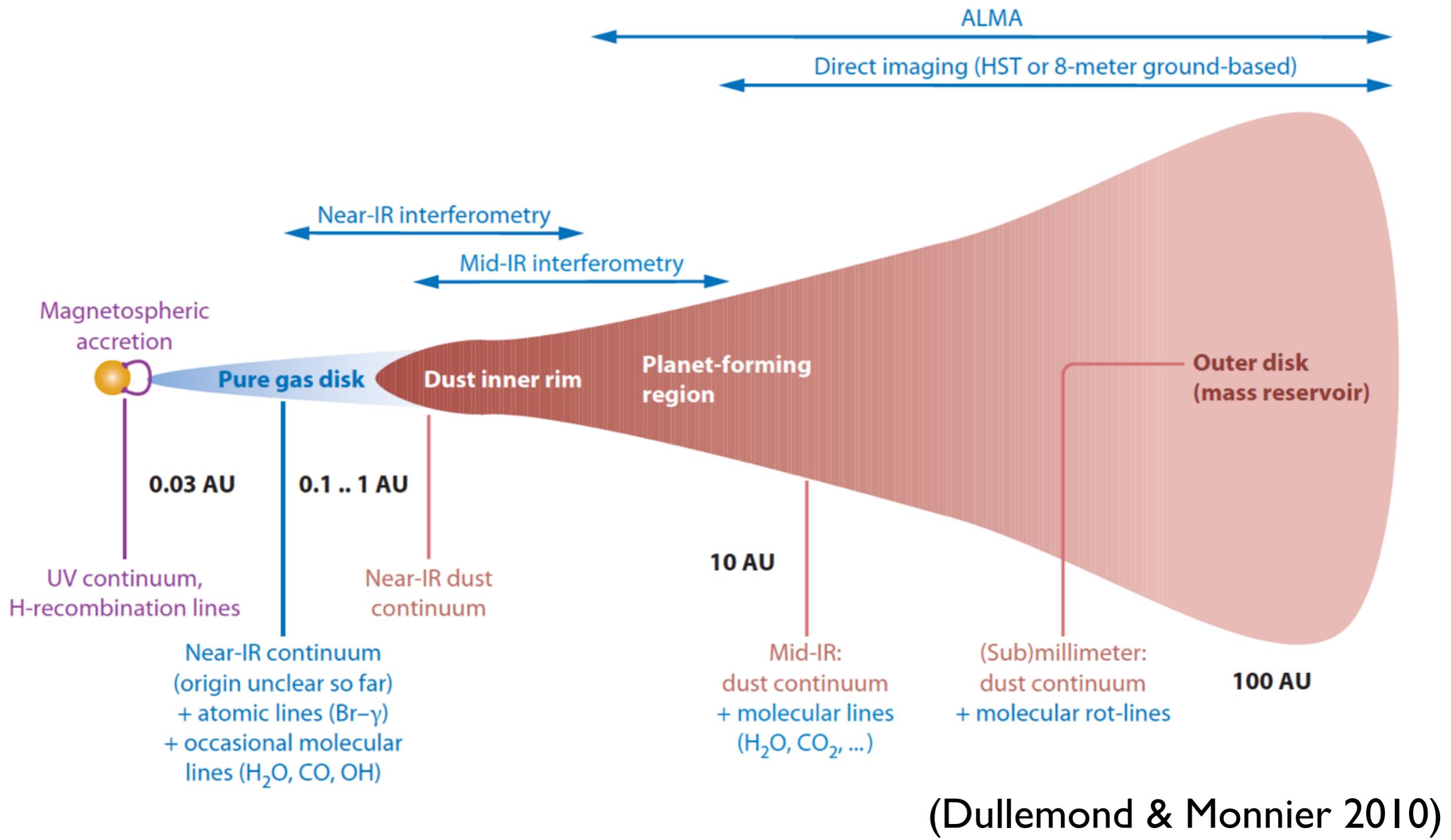


(Przygoda et al. 2003)

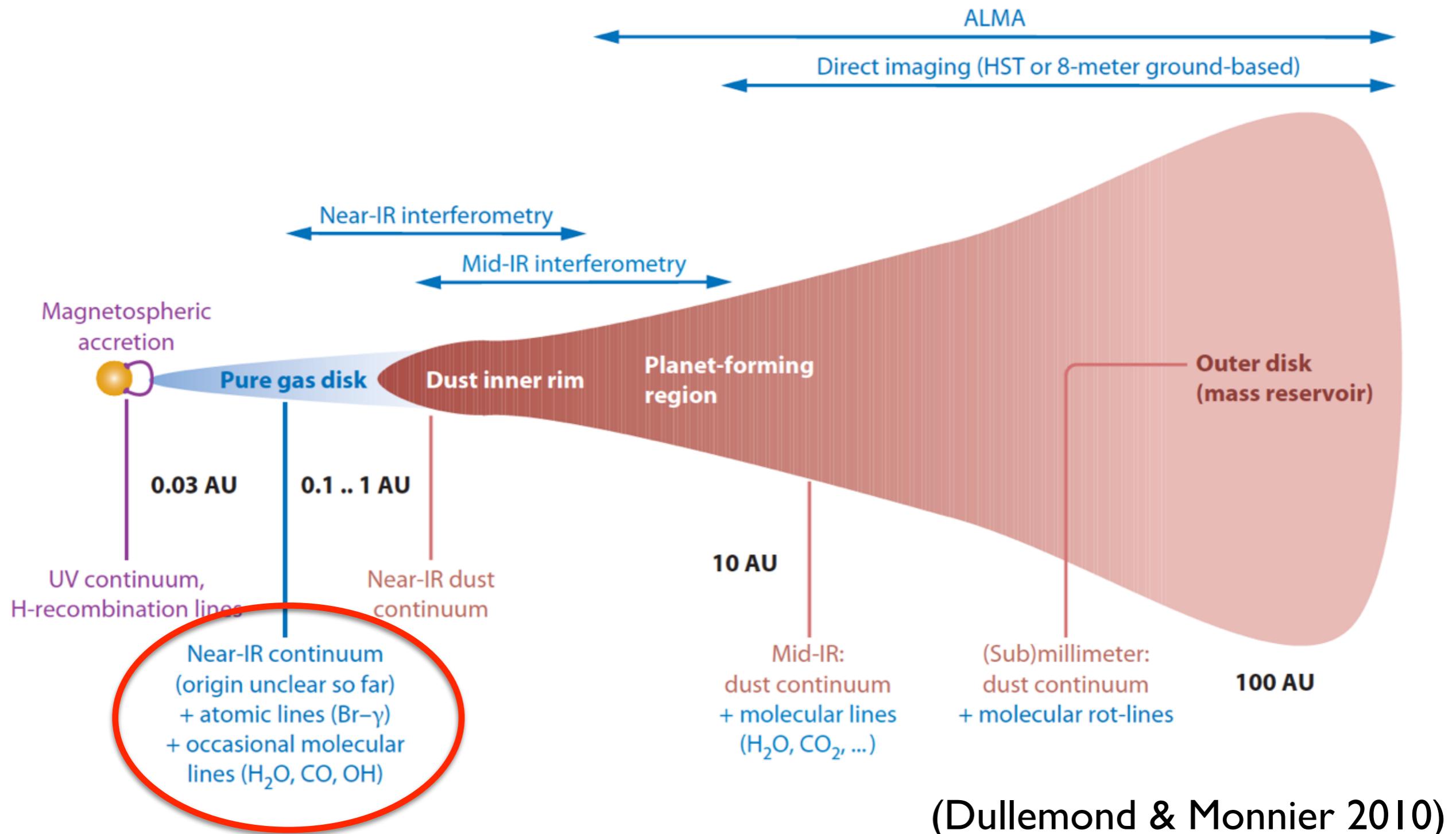
# Disk composition – gas

- Interstellar gas-to-dust mass ratio: 100
- 99% of the total mass of ISM
- 99% of the total mass of disks (at least initially)
- Difficult to detect ( $H_2$  has no easily observable lines)
- Ways to observe the gas:
  - Disk accretion (recombination lines, excess hot continuum)
  - MIR molecular lines
  - FIR molecular lines

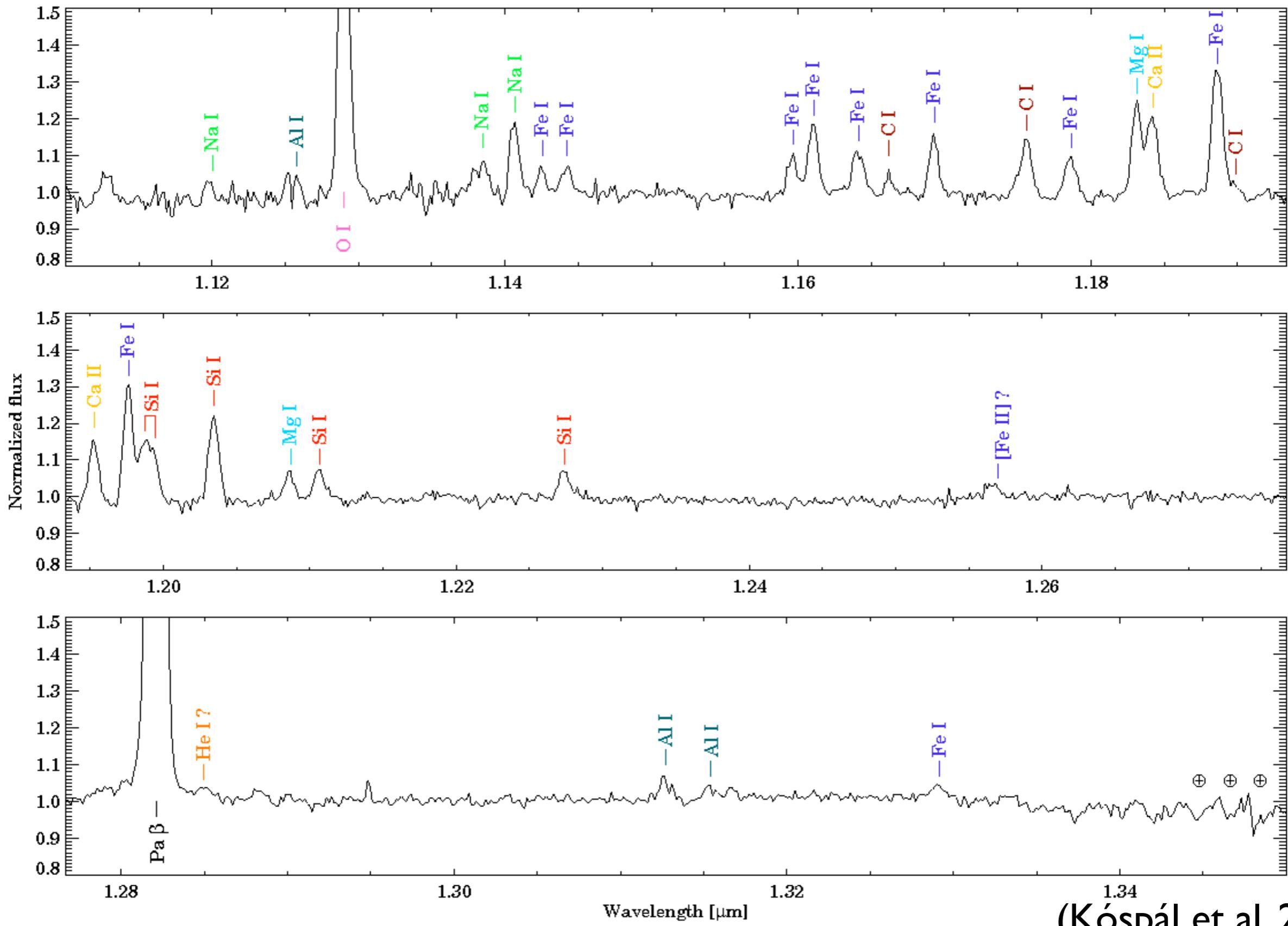
# Disk composition – gas



# Disk composition – gas

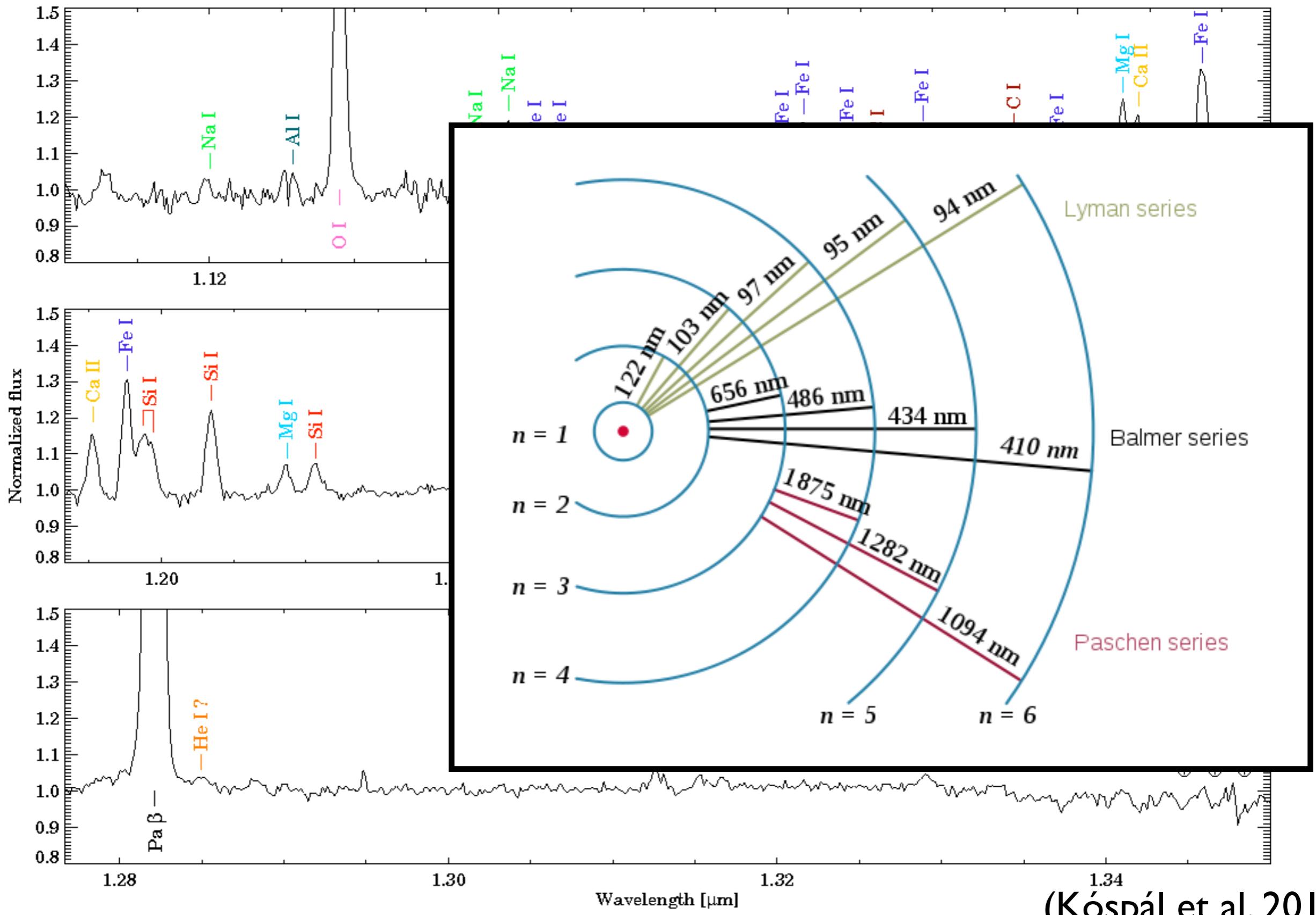


# Near infrared lines

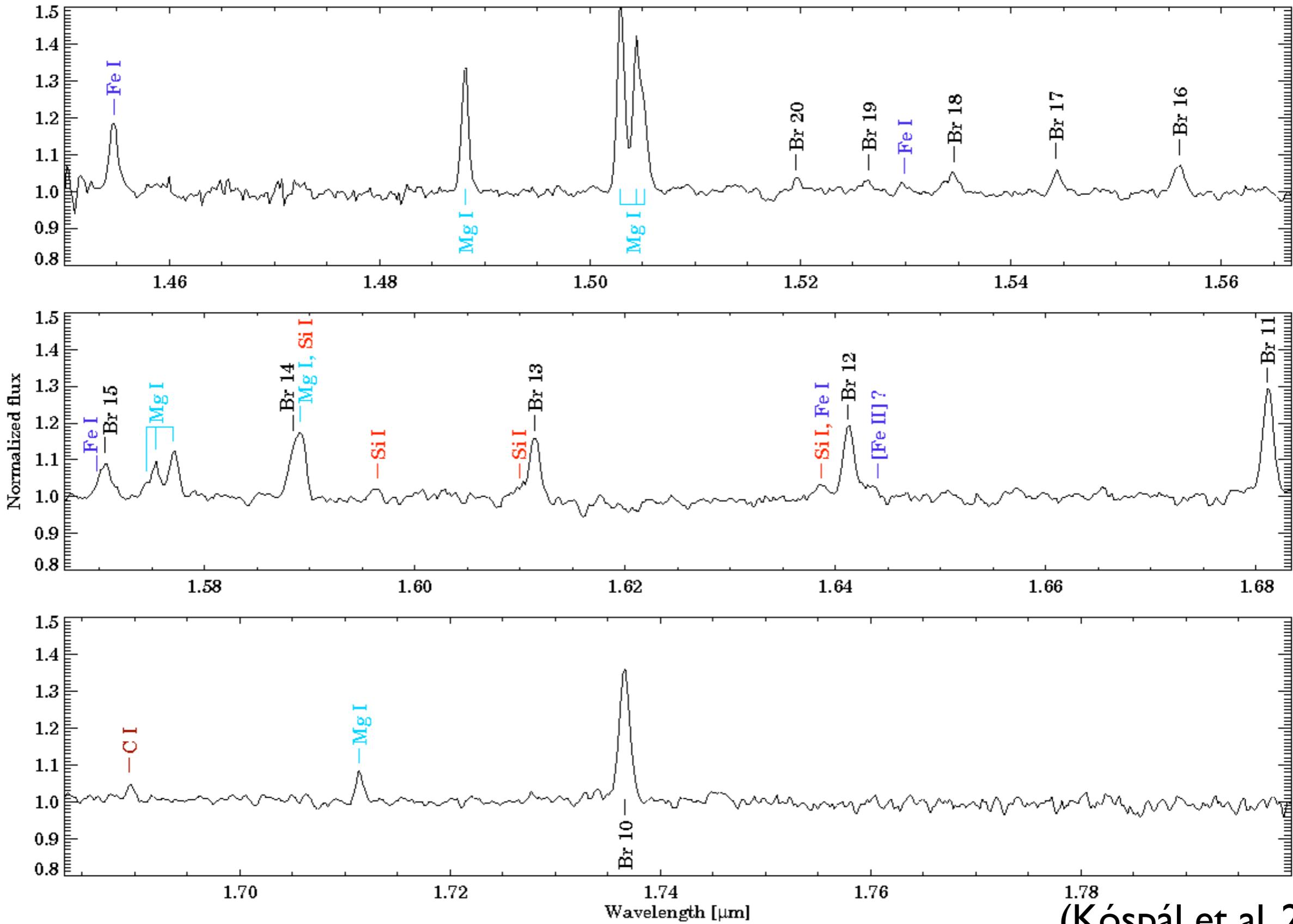


(Kóspál et al. 2012)

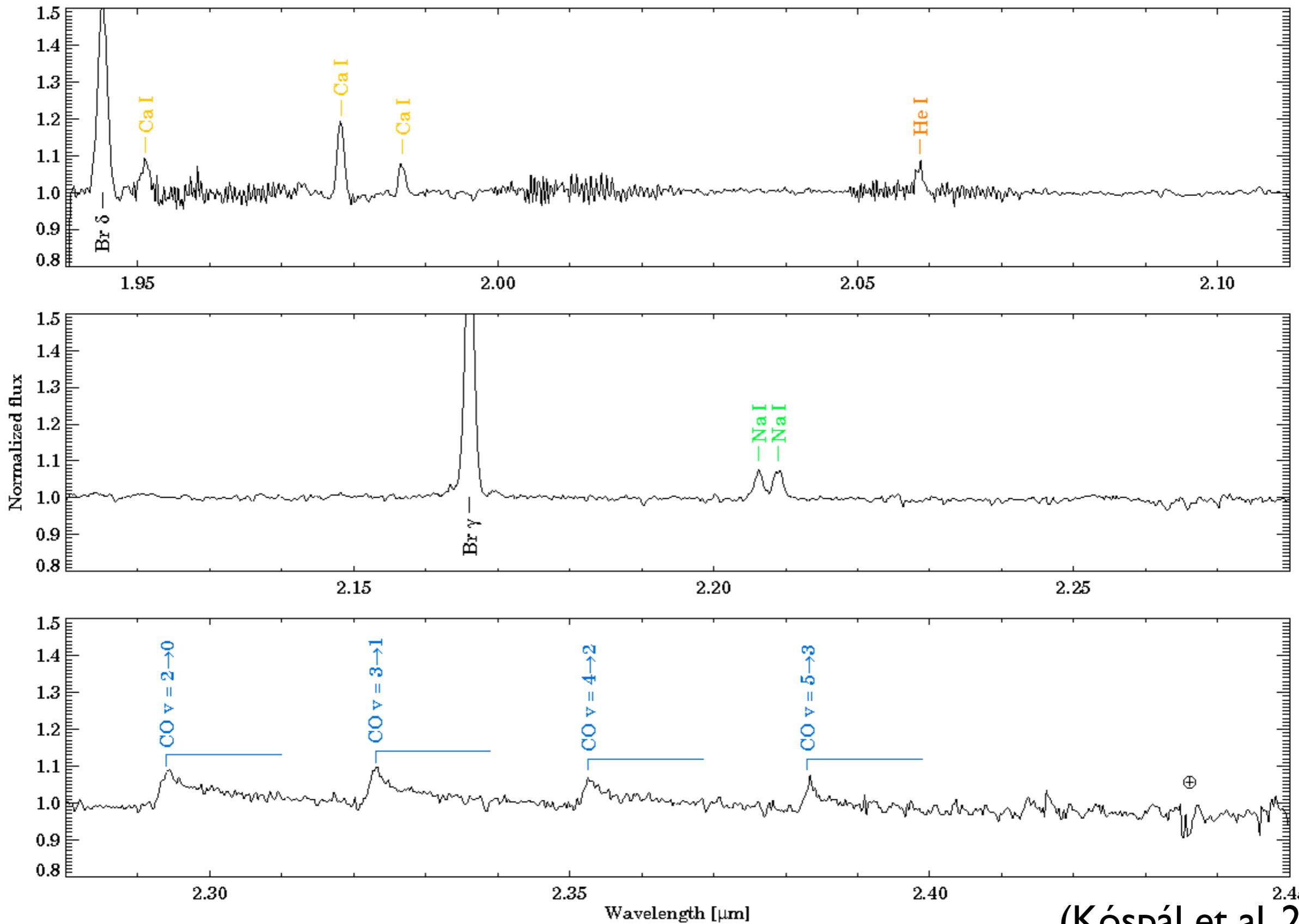
# Near infrared lines



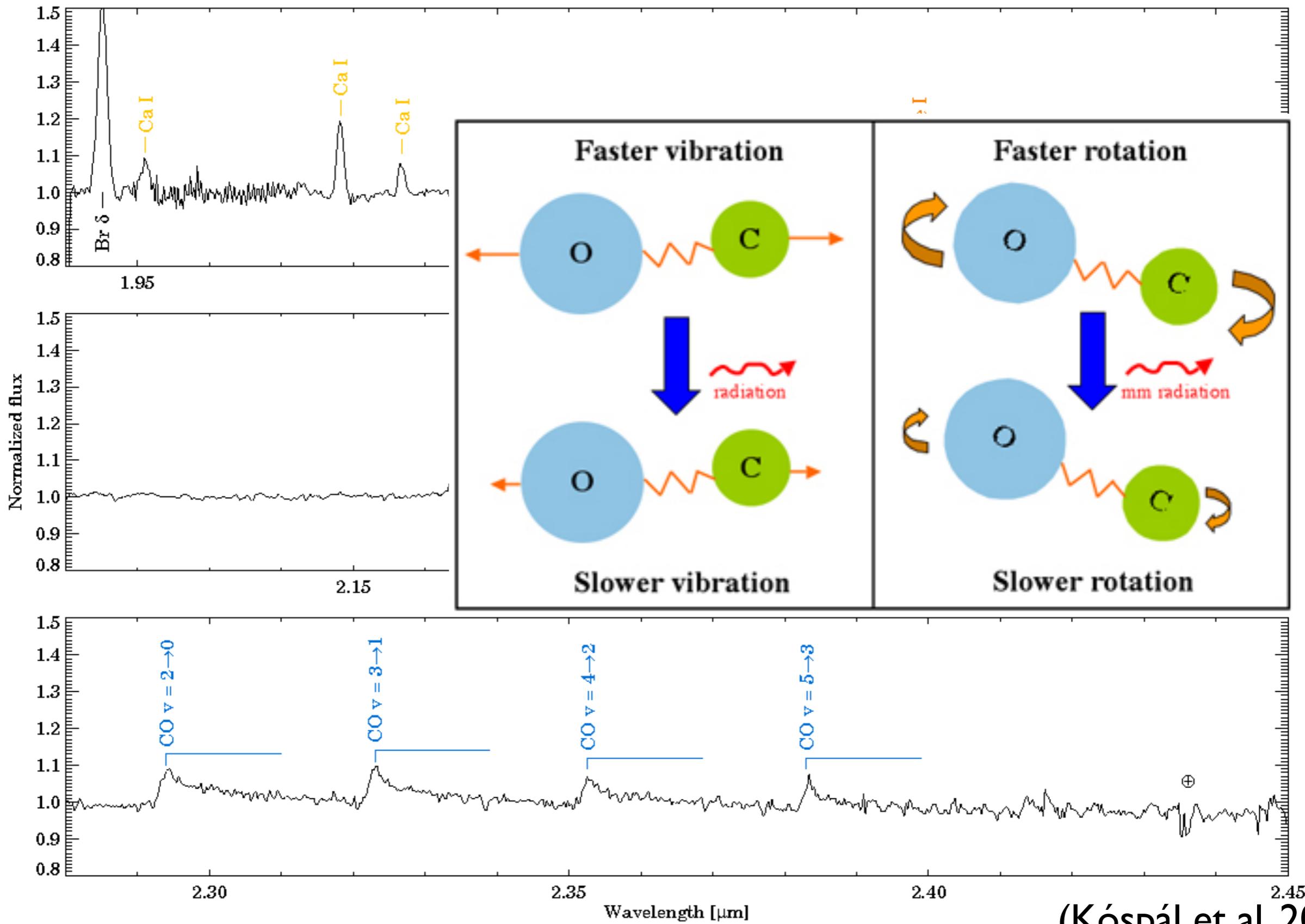
# Near infrared lines



# Near infrared lines

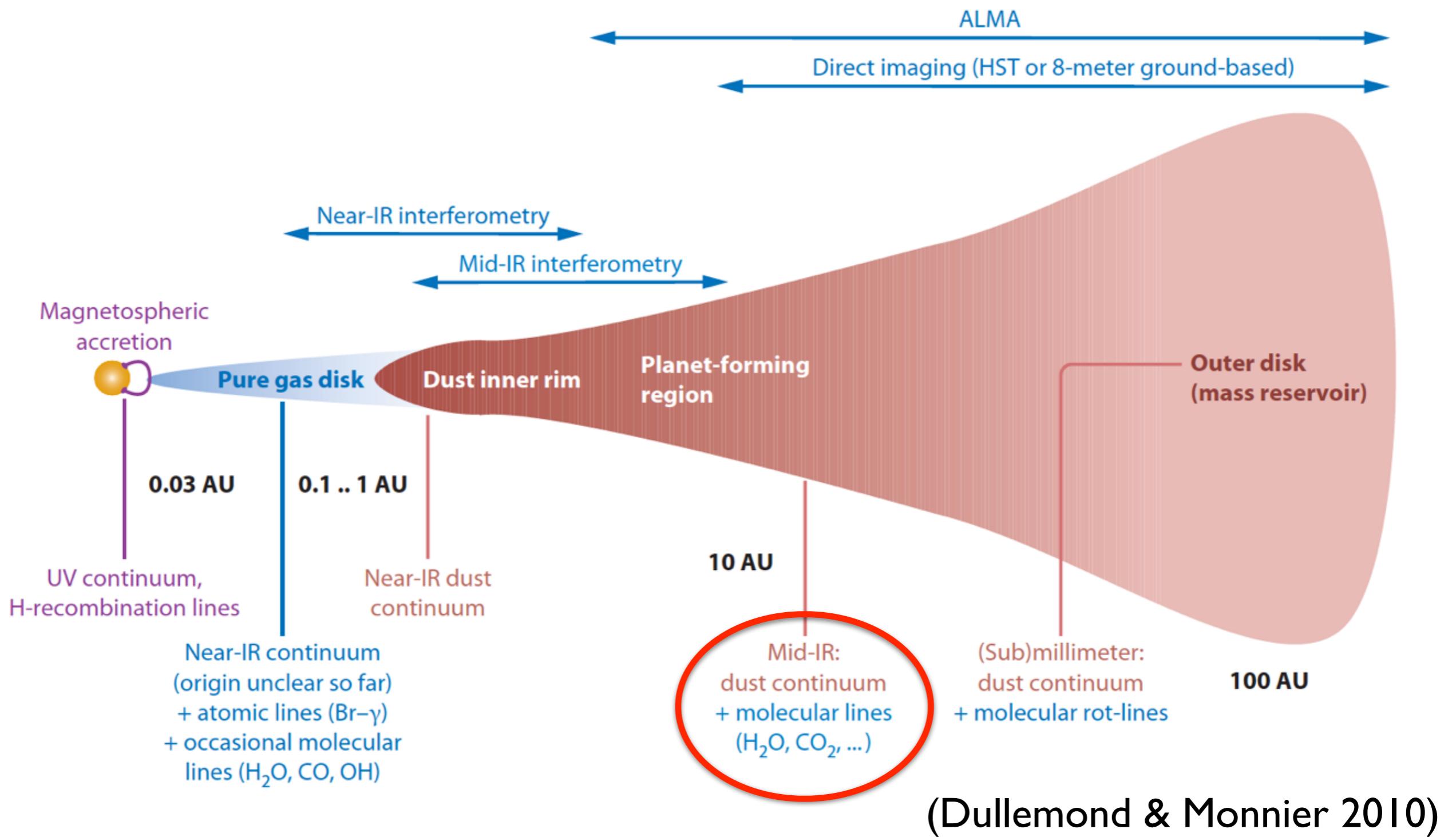


# Near infrared lines

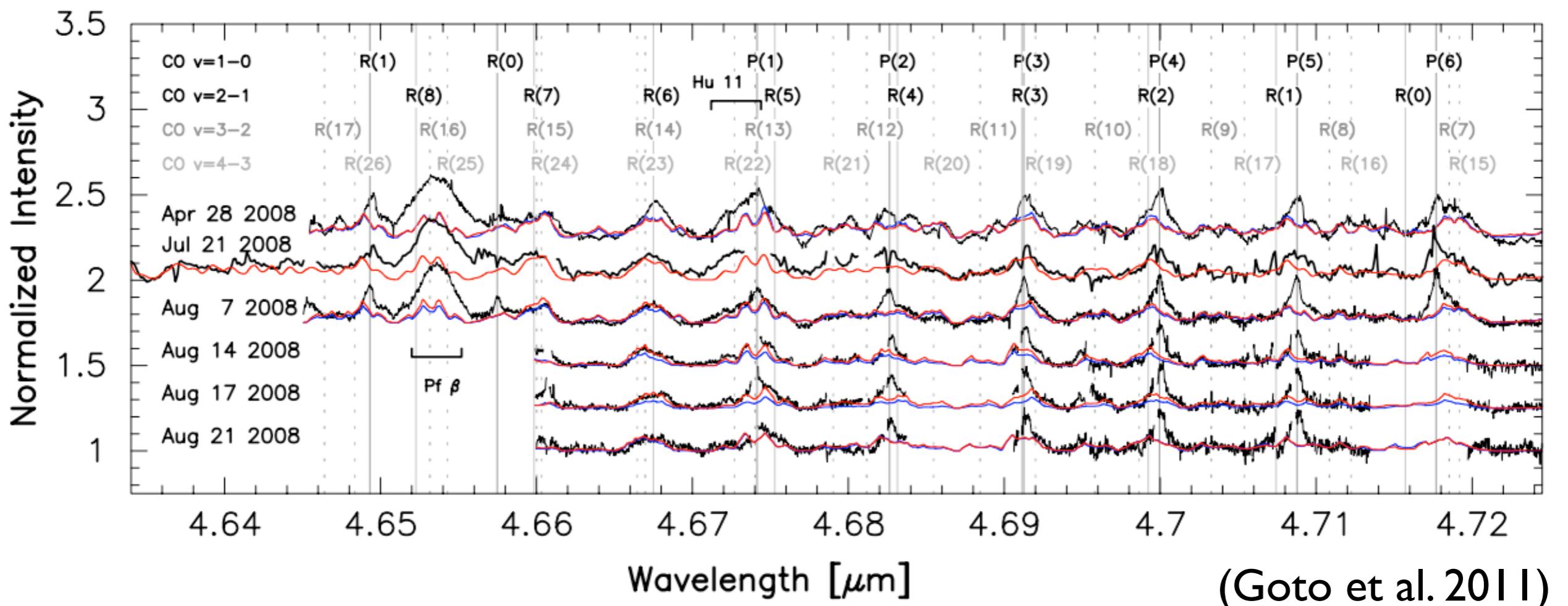


(Kóspál et al. 2012)

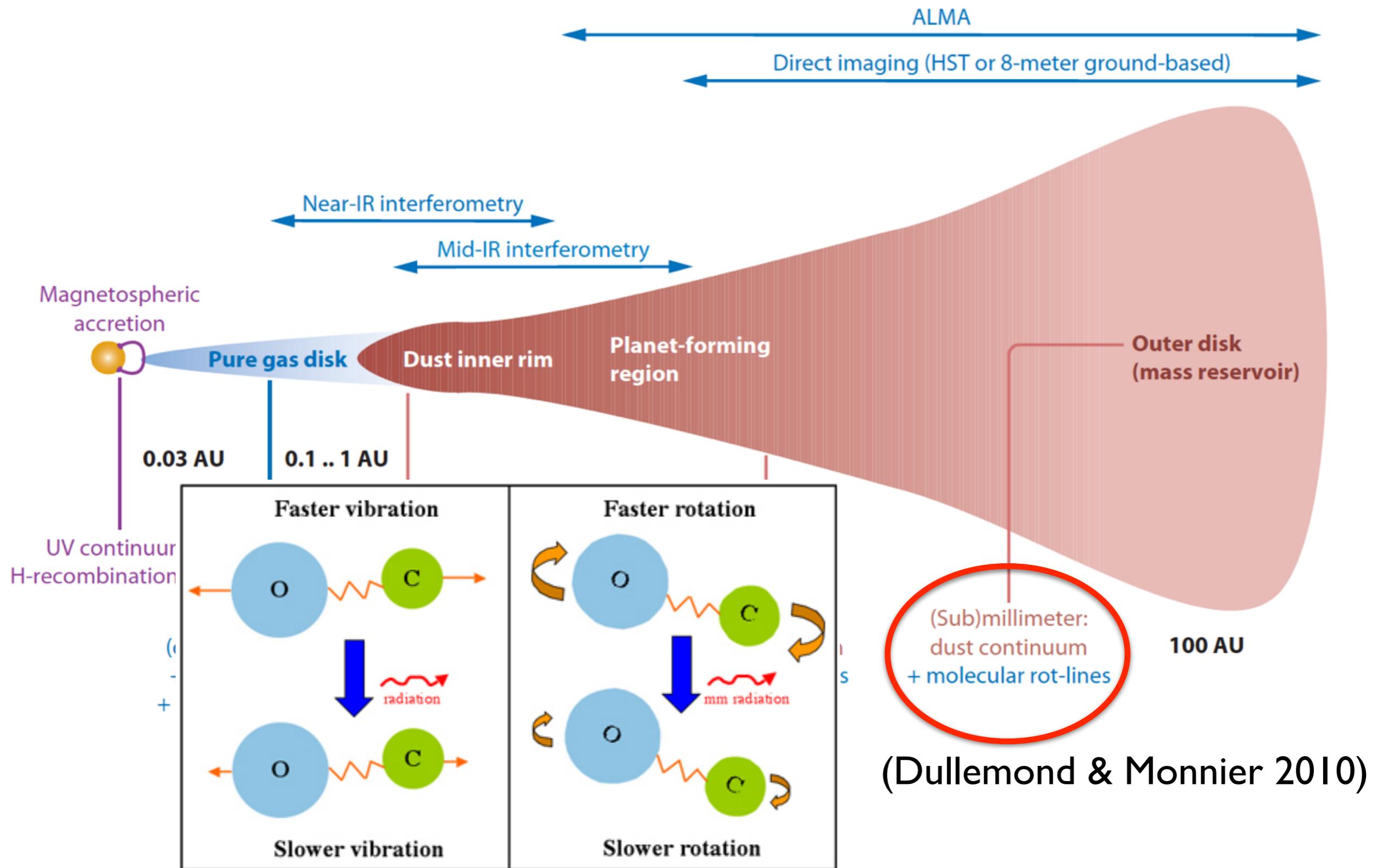
# Disk composition – gas



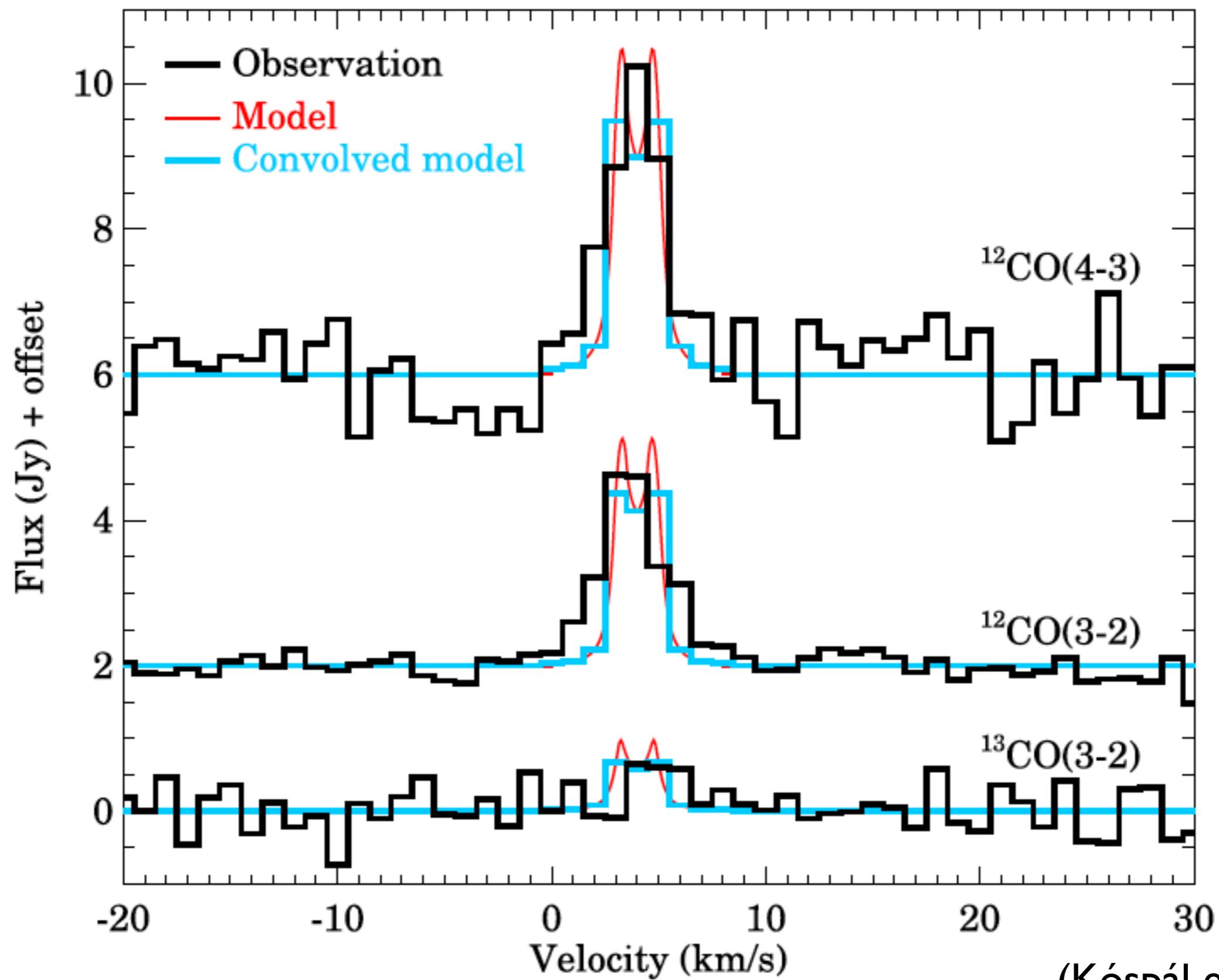
# Mid-infrared lines



# Disk composition – gas



# Millimeter lines



(Kóspál et al. 2016)

# Disk composition – gas

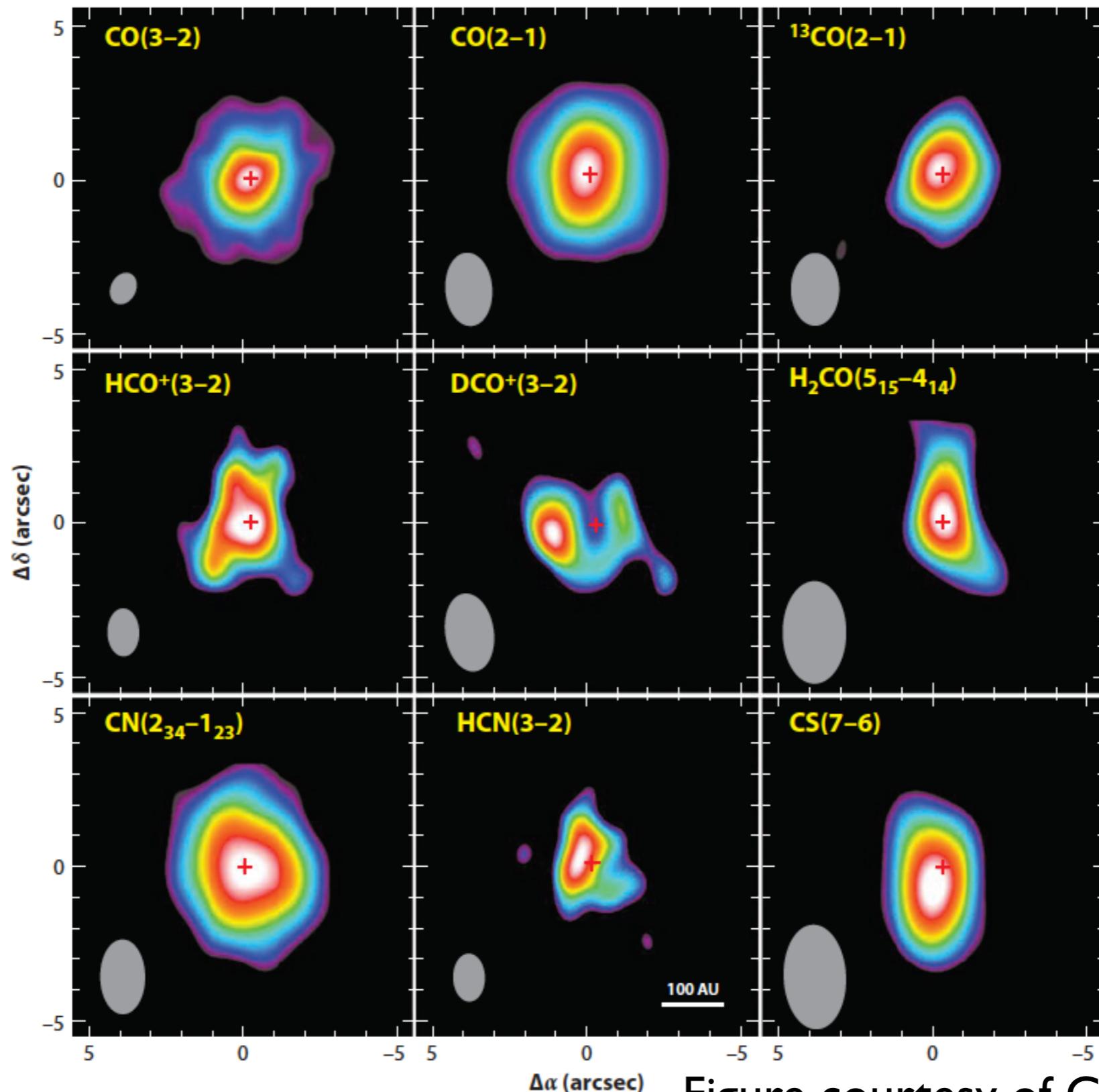
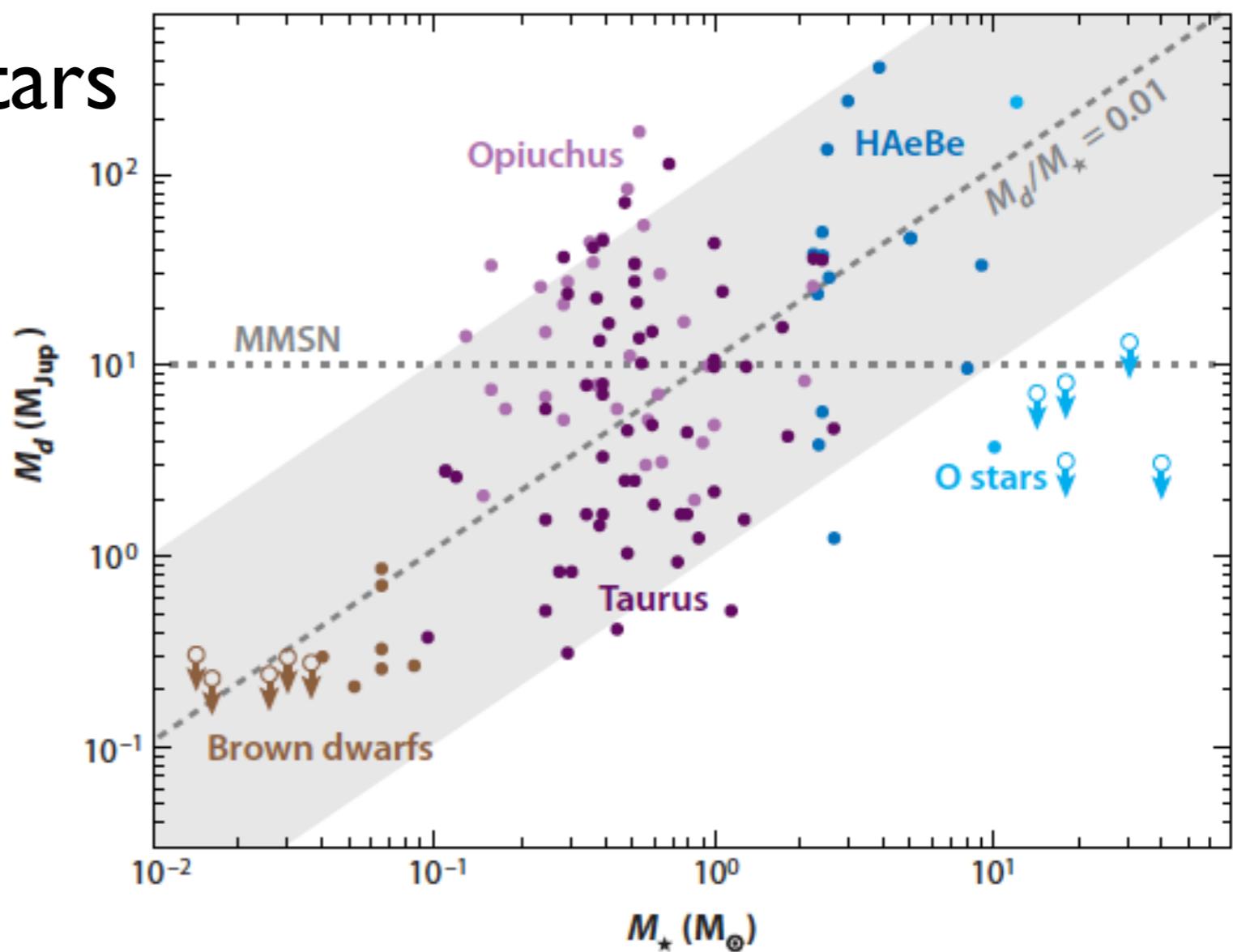


Figure courtesy of Charlie Qi

# Dependence on stellar mass

- Disks have been detected around
  - Brown dwarfs
  - T Tauri stars of various masses
  - Herbig Ae/Be stars
- Expectation: higher mass stars require more mass to pass through their disks
- $M_{\text{disk}} / M_{\text{star}} \sim 0.01$



# More massive stars?

- $M_{\text{disk}} / M_{\text{star}} < 10^{-4}$  for  $M_{\text{star}} > 10 M_{\odot}$
- No disks around optically visible O stars? Why?
  - High photoevaporation rate (disk disappears by the time the star becomes visible)
  - Different star formation mechanism than for lower-mass stars
- Cause?
- Some new results: a Keplerian-like disk around AFGL 4176 (Johnston et al. 2015)

